

Univariate/ MonoPhenotype Modeling

Boulder Workshop 2020

Hermine H. Maes

with credit to Nick Martin, Elizabeth Prom-Wormley,
Tim Bates, Katrina Grasby & many others

hmaes/2020/maes/twinModeling

hmaes/2020/maes/twinModeling

- oneSATc.R
- oneACEvc.R
- oneADEvc.R
- oneACEc.R
- oneADEc.R
- miFunctions.R
- miFunctionsDocs.pdf
- twinModeling2020.pdf

Questions

- Does a trait of interest run in families?
- Can **familial** resemblance be explained by genetic and/or environmental effects?
- **Which** sources of variance contribute significantly to the variance of the trait?
- **How much** of the variation in the trait is accounted for by genetic and environmental effects?

Roadmap for Univariate Analysis

- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
 - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
 - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
 - AE / CE / E Only Model

Practical Example

- Dataset: NH&MRC Twin Register
- 1981 Questionnaire
- **BMI** (body mass index): weight/height squared
 - kg/m², transformed: $7 \cdot \log(\text{BMI})$, simulated based on real data
- Young Female Cohort: 18-30 years
- Sample Size:
 - MZf: 534 pairs (zyg=1; zygosity='MZFF' & cohort='younger')
 - DZf: 328 pairs (zyg=3; zygosity='DZFF' & cohort='younger')

Dataset

```
> head(twinData)
```

```
   fam age zyg part wt1 wt2   ht1   ht2  htwt1  htwt2   bmi1   bmi2
1    1  21   1    2  58  57 1.7000 1.7000 20.0692 19.7232 20.9943 20.8726
2    2  24   1    2  54  53 1.6299 1.6299 20.3244 19.9481 21.0828 20.9519
3    3  21   1    2  55  50 1.6499 1.6799 20.2020 17.7154 21.0405 20.1210
4    4  21   1    2  66  76 1.5698 1.6499 26.7759 27.9155 23.0125 23.3043
5    5  19   1    2  50  48 1.6099 1.6299 19.2894 18.0662 20.7169 20.2583
6    6  26   1    2  60  60 1.5999 1.5698 23.4375 24.3418 22.0804 22.3454
....
```

My Naming Conventions

name of variable(s)	<code>vars</code>	<code><- 'bmi'</code>
number of variables	<code>nv</code>	<code><- 1</code>
number of twin variables	<code>ntv</code>	<code><- nv*2</code>
variables per twin pair	<code>selVars</code>	<code><-c('bmi1', 'bmi2')</code>
definition variables	<code>covVars</code>	
number of factors	<code>nf</code>	<code><- 2</code>
number of thresholds	<code>nth</code>	<code><- 3</code>
starting values	<code>sv</code>	
lower bound / upper bound	<code>lb / ub</code>	
labels	<code>lab</code>	
built model	<code>modelNAME</code>	
fitted model	<code>fitNAME</code>	
summary of fitted model	<code>sumNAME</code>	

Classical Twin Study Background

- The Classical Twin Study (CTS) uses MZ and DZ twins reared together
 - MZ twins share 100% of their genes
 - DZ twins share **on average** 50% of their genes
- Expectation: Genetic factors are assumed to contribute to a phenotype when MZ twins are more similar than DZ twins

Classical Twin Study Assumptions

- Equal Environments of MZ and DZ pairs
- Random Mating
- No GE Correlation
- No G x E Interaction
- No Sex Limitation
- No G x Age Interaction

Classical Twin Study Basic Data Assumptions

- MZ and DZ twins are sampled from the same population, therefore we **expect** :
 - Equal means/variances in Twin 1 and Twin 2
 - Equal means/variances in MZ and DZ twins
- Further assumptions would need to be tested if we introduce male twins and opposite sex twin pairs

Observed Values

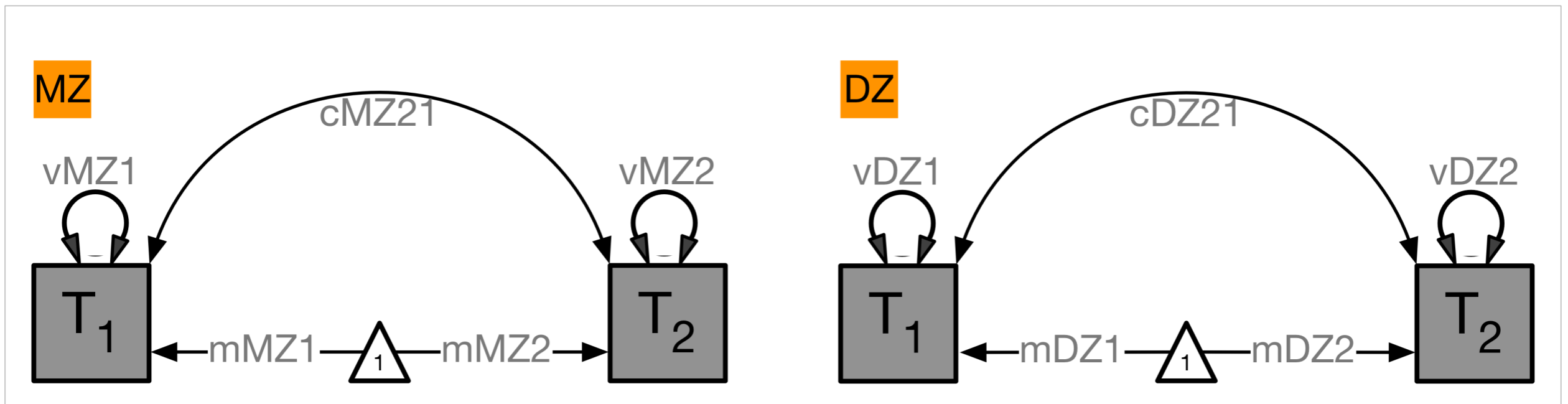
	Descriptive Statistics					
	MZ twins			DZ twins		
		T1	T2		T1	T2
mean	MZ	21.34	21.35	DZ	21.45	21.46
		T1	T2		T1	T2
cov	T1	0.73		T1	0.77	
	T2	0.59	0.79	T2	0.24	0.82

'Old Fashioned' Data Checking

Nice, but how can we actually be sure that these means and variances are truly the same?

Saturated Model

SAT model
oneSATc.R



Intuition behind Maximum Likelihood (ML)

- Likelihood: probability that an observation (data point) is predicted by specified model
- Maximum Likelihood Estimates (MLE): most likely values of population parameter values (e.g, μ , σ , β) given observed sample values
 - Define model
 - Define probability of observing a given event conditional on a particular set of parameters
 - Choose a set of parameters which are most likely to have produced observed results

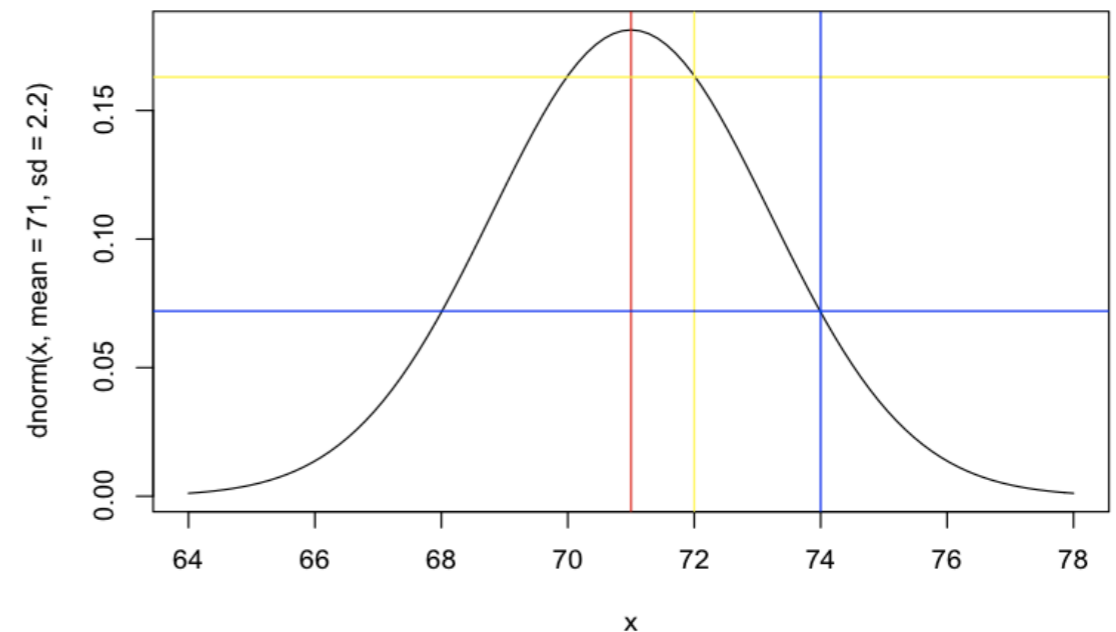
Likelihood Ratio Test

- Likelihood Ratio (LR) test: simple comparison of Log-Likelihoods under 2 separate models:
 - Model **Mu**: Unconstrained (has more parameters)
 - Model **Mc**: Constrained (has fewer parameters)
- LR statistic equals:
 - $LR (Mc | Mu) = 2\ln(L(Mu)) - 2\ln(L(Mc))$
- LR is asymptotically distributed as χ^2 with df equal to number of constraints

Probability Density Function $\Phi(x_i)$

- $\Phi(x_i)$: likelihood of data point x_i for particular mean and variance estimates
- Univariate: height of probability density function

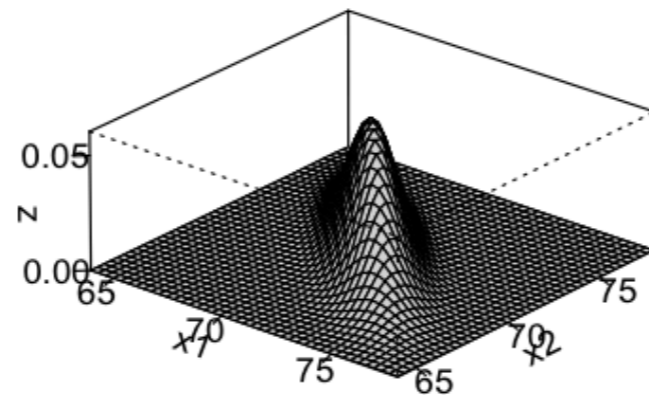
$$\Phi(x_i) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-5((x_i-\mu)^2/\sigma^2)}$$



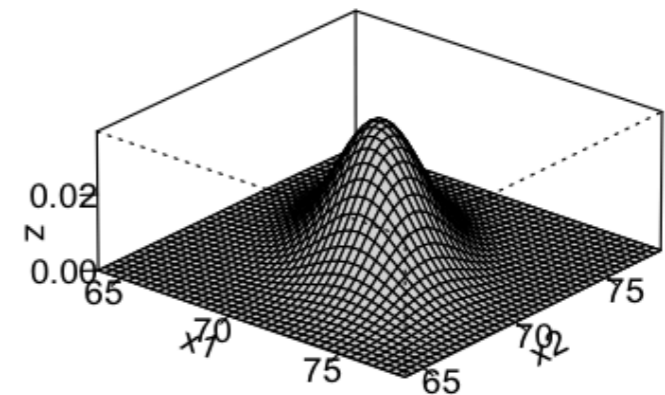
π : $\pi=3.14$; x_i : observed value of variable i ; μ : expected mean; σ : expected variance

Multinormal Probability Function

- $\Phi(x_i)$: likelihood of pair of data points x_i and y_i for particular means, variances & correlation estimates
- Multivariate: height of multinormal probability density function



rMZ=.85



rDZ=.49

$$\Phi(x_i) = \frac{1}{\sqrt{|2\pi\Sigma|}^{n/2}} e^{-5((x_i-\mu)\Sigma^{-1}(x_i-\mu)')}$$

$\pi = 3.14$; x_i : value of variable i ; μ : expected mean; Σ : expected covariance matrix

OpenMx Scripts

■ oneSATc.R

- Saturated model estimating means & variances for continuous data in MZ & DZ twins

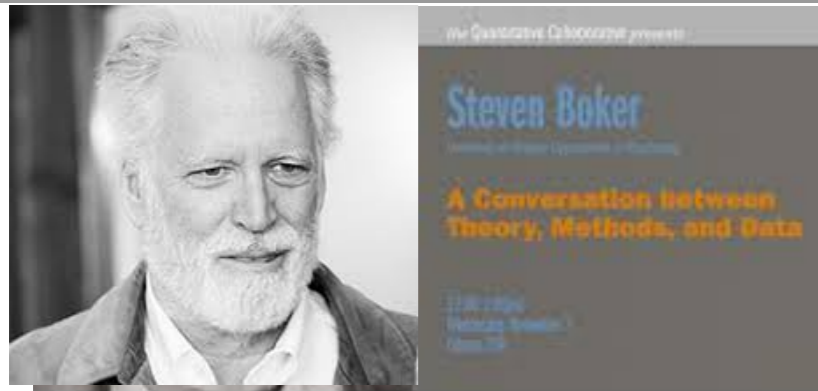
■ oneACEvc.R

- Univariate/Monophenotype model estimating A, C & E components for continuous data in MZ & DZ twins

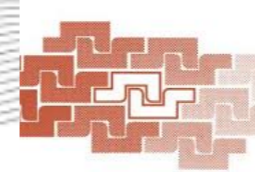
■ oneADEvc.R

- Univariate/Monophenotype model estimating A, D & E components for continuous data in MZ & DZ twins

OpenMx Development Team (most active ones)



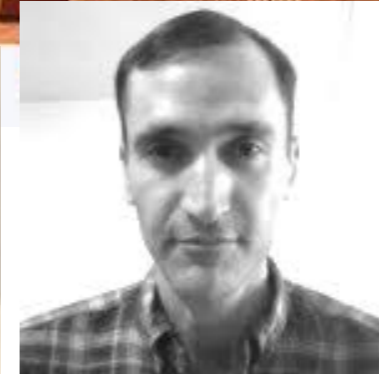
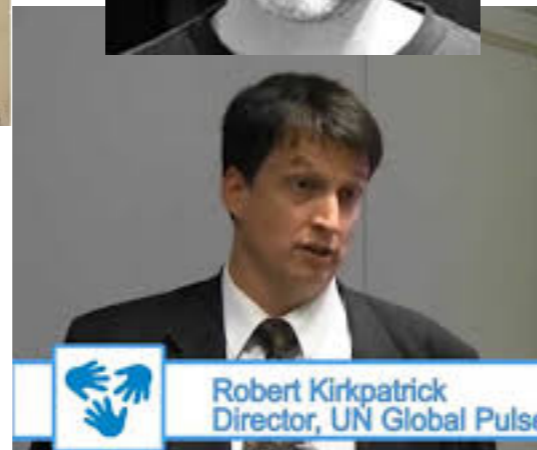
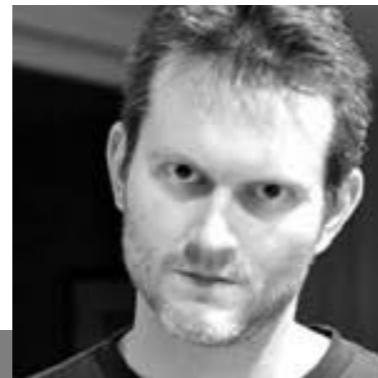
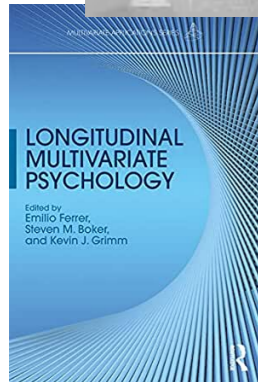
WORSHIP
TOGETHER
WHAT MORE COULD I WANT
MICHAEL NEALE



Methodology for
Genetic Studies of
Twins and Families

Michael C. Neale and Lon R. Cardon

PRITIKIN
WEIGHT LOSS



Tim Bates
and the
Wonnangatta
Murders



OpenMx Development Team (most active ones)



Steve Boker



Mike Neale



Mike Hunter



Rob Kirkpatrick



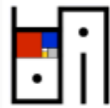
Joshua Pritikin



Tim Bates

<https://hermine-maes.squarespace.com>

hermine-maes.squarespace.com



HOME OPENMX ISGW

genetic epidemiology
helper functions

HELP

classical twin study
MZ & DZ twins
ONE phenotype
continuous/binary/ordinal
SAT | ACE | ADE

ONE

classical twin study
MZ & DZ twins
ONE phenotype
continuous/binary/ordinal
+covariate age
SAT | ACE | ADE

ONEA

classical twin study
MZ & DZ twins
MZf MZm DZf DZm DZo
ONE phenotype
continuous/binary/ordinal
+covariate age
heterogeneity
SAT | ACE | ADE

ONEA5

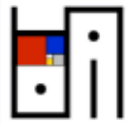
classical twin study
MZ & DZ twins
TWO phenotypes
continuous/binary/ordinal
SAT | ACE | ADE

TWO

classical twin study
MZ & DZ twins
TWO phenotypes
continuous
biv25

TWO+

helper functions



[HOME](#) [OPENMX](#) [ISGW](#)

Parallel standard OpenMx scripts & matching umx versions

This site offers [OpenMx](#) and matching [umx](#) scripts to fit standard biometrical models to data collected in MZ and DZ twins. The models can be used to estimate the role of genetic (A: additive genetic factors; D: dominance genetic factors) and environmental factors (C: common/shared environmental factors, E: unique environmental factors) to the variance of phenotypes of interest and covariances between phenotypes of interest.

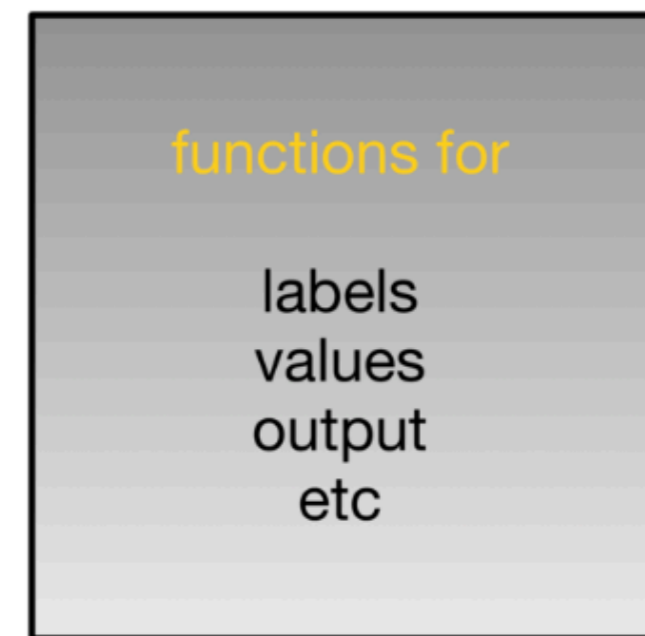
Scripts are organized in pages by number of phenotypes, addition of covariates etc. Within each page, scripts are organized by type of model in rows (Saturated, ACE estimating variance components, ADE estimating variance components, ACE estimating path coefficients, ADE estimating path coefficients) and by type of data in columns (continuous, binary, ordinal (estimating all thresholds), ordinal (fixing two thresholds and estimating means/variances) using standard code, and using umx (for different data types) in the last column. All scripts source the R code attached here that includes a number of functions that automate various aspects of the models such as labels, starting values, output generated etc.

Note that each of the scripts is represented by a path diagram. If you click on the diagram, a PDF of the associated script will be displayed in a separate window. If you click on the filename.R below the diagram, the R script will be downloaded.

Comments, suggestions, corrections welcome!! **Email hmaes@vcu.edu.**

New pages/scripts will be added as they are ready to go! If you have scripts that you'd like to add, send them my way!

Last updated: 02/28/2020



miFunctions.R

miFunctions.R

```
# -----  
# Program: miFunctions.R  
# Author: Hermine Maes  
# Date: 02 28 2020  
#  
# Set of my options & functions used in basic twin methodology scripts  
# Email: hmaes@vcu.edu  
# -----|-----|-----|-----|-----|-----|-----|-----|  
  
# Options  
mxOption( NULL, "Default optimizer", "NPSOL" )  
#mxOption( NULL, "Checkpoint Prefix", filename )  
mxOption( NULL, "Checkpoint Units", "iterations" )  
mxOption( NULL, "Checkpoint Count", 1 )  
options(width=120)  
options(digits=8)  
mxVersion()  
  
# Functions to assign labels  
# -----  
labLower  <- function(lab,nv) { paste(lab,rev(nv+1-sequence(1:nv)),rep(1:nv,nv:1),sep="") }  
labSdiag  <- function(lab,nv) { paste(lab,rev(nv+1-sequence(1:(nv-1))),rep(1:(nv-1),(nv-1):1),sep="") }  
lab0diag  <- function(lab,nv) { paste(lab,c(rev(nv+1-sequence(1:(nv-1))),rep(1:(nv-1),(nv-1):1)),c(rep(1:(nv-1),  
(nv-1):1),rev(nv+1-sequence(1:(nv-1))))),sep="") }  
  
....
```

one

classical twin study
MZ & DZ twins

ONE phenotype
continuous/binary/ordinal

SAT | ACE | ADE

SAT

estimating means/thresholds, variances & covariances

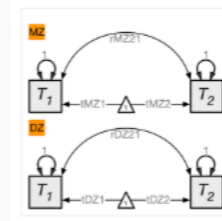
* > 2 categories

One Phenotype
CONTINUOUS c



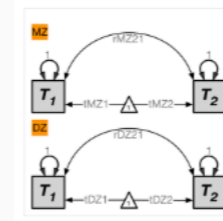
oneSATc.R

One Phenotype
BINARY b



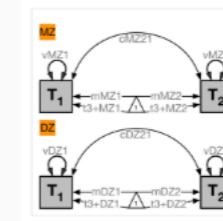
oneSATb.R

One Phenotype
ORDINAL o



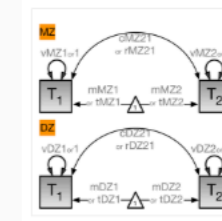
oneSATo.R

One Phenotype
ORDINAL m*



oneSATm.R

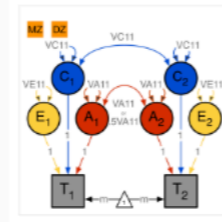
One Phenotype
UMX c/b/m



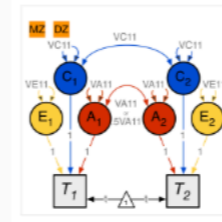
oneSATu.R

ACE

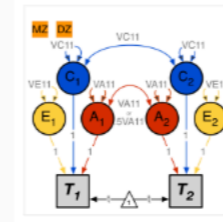
estimating variance components



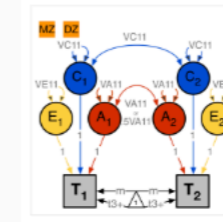
oneACEvc.R



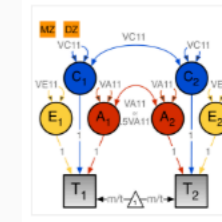
oneACEvb.R



oneACEvo.R



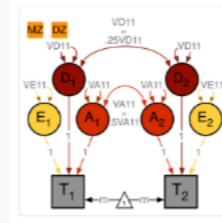
oneACEvm.R



oneACEvu.R

ADE

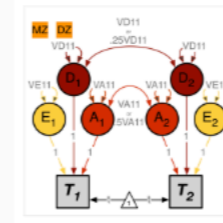
estimating variance components



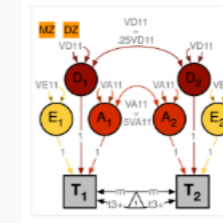
oneADEvc.R



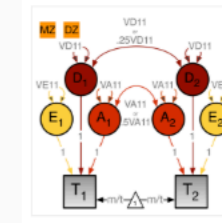
oneADEvb.R



oneADEvo.R



oneADEvm.R

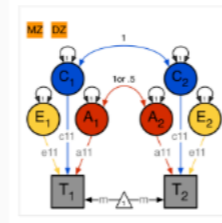


oneADEvu.R

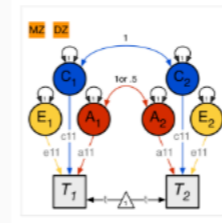
NOTE! Models below estimating path coefficients may provide biased estimates of the parameters. Use of these scripts is discouraged.

ACE

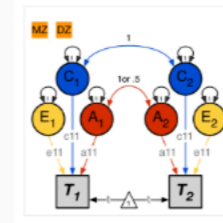
estimating path coefficients



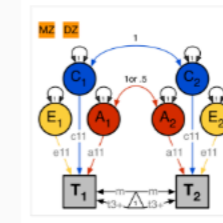
oneACEc.R



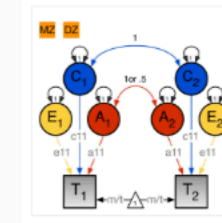
oneACEb.R



oneACEo.R



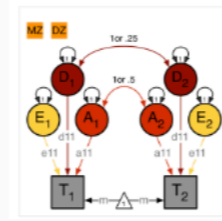
oneACEm.R



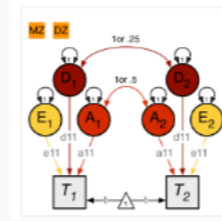
oneACEu.R

ADE

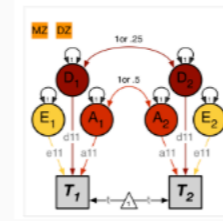
estimating path coefficients



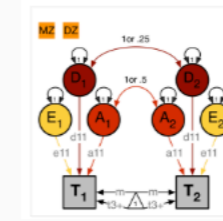
oneADEc.R



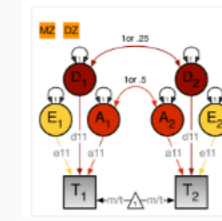
oneADEb.R



oneADEo.R



oneADEm.R



oneADEu.R

one

classical twin study
MZ & DZ twins

ONE phenotype
continuous/binary/ordinal

SAT | ACE | ADE

SAT

estimating means/thresholds, variances & covariances

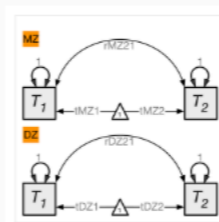
* > 2 categories

One Phenotype
CONTINUOUS c



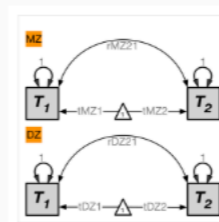
oneSATc.R

One Phenotype
BINARY b



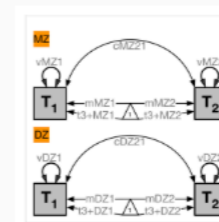
oneSATb.R

One Phenotype
ORDINAL o



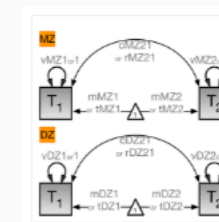
oneSATo.R

One Phenotype
ORDINAL m *



oneSATm.R

One Phenotype
UMX c/b/m



oneSATu.R

ACE

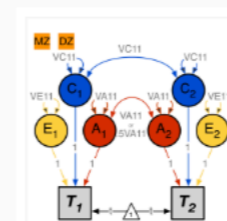
estimating variance components



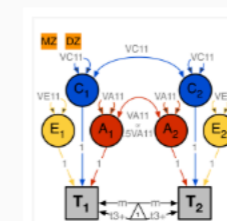
oneACEvc.R



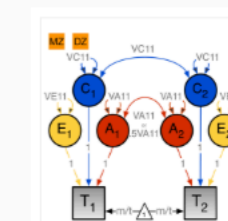
oneACEvb.R



oneACEvo.R



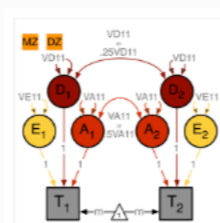
oneACEvm.R



oneACEvu.R

ADE

estimating variance components



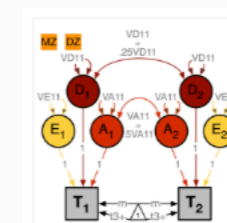
oneADEvc.R



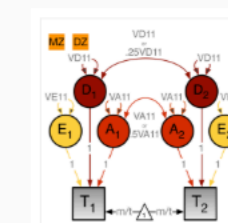
oneADEvb.R



oneADEvo.R



oneADEvm.R

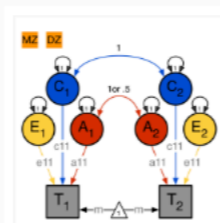


oneADEvu.R

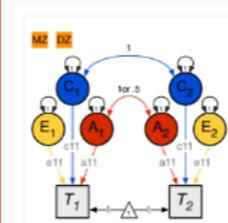
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ACE

estimating path coefficients



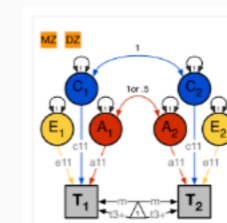
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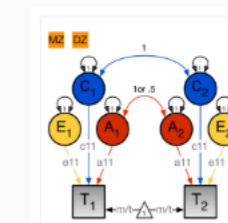
oneACEb.R



oneACEo.R



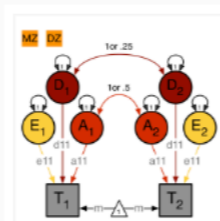
oneACEm.R



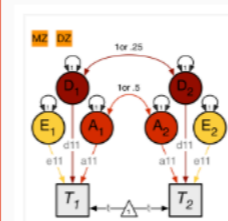
oneACEu.R

ADE

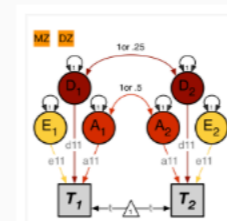
estimating path coefficients



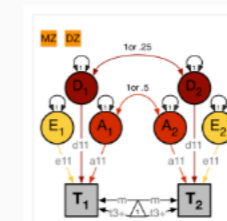
oneADEc.R



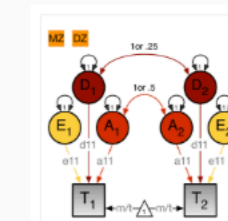
oneADEb.R



oneADEo.R



oneADEm.R



oneADEu.R

Univariate Saturated Model

oneSATc.R

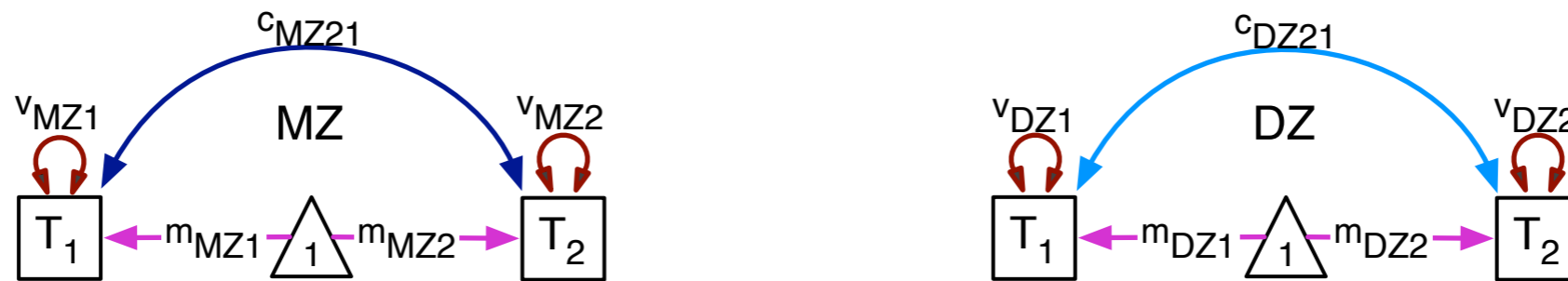
```
# -----  
# Program: oneSATc.R  
# Author: Hermine Maes  
# Date: 10 22 2018  
#  
# Twin Univariate Saturated model to estimate means and (co)variances across multiple groups  
# Matrix style model - Raw data - Continuous data  
# -----|-----|-----|-----|-----|-----|-----|-----|  
  
# Load Libraries & Options  
rm(list=ls())  
library(OpenMx) → load OpenMx  
library(psych); library(polycor)  
source("miFunctions.R") → my functions which you can edit as you like  
  
# Create Output  
filename <- "oneSATc"  
sink(paste(filename, ".Ro", sep=""), append=FALSE, split=TRUE) → creates output file with extension .Ro
```

Preparing Data

oneSATc.R

```
# -----  
# PREPARE DATA  
  
# Load Data  
data(twinData) → load 'twinData' or read in your own  
dim(twinData)  
describe(twinData[,1:12], skew=F)  
  
# Select Variables for Analysis  
vars      <- 'bmi'           # list of variables names  
nv        <- 1               # number of variables  
ntv       <- nv*2            # number of total variables  
selVars   <- paste(vars,c(rep(1,nv),rep(2,nv)),sep="") → analyzing c('bmi1','bmi2')  
# Select Data for Analysis  
mzData    <- subset(twinData, zyg==1, selVars) # zygosity='MZFF' & cohort='younger'  
dzData    <- subset(twinData, zyg==3, selVars) → get right codes for zygosity  
  
# Generate Descriptive Statistics  
colMeans(mzData,na.rm=TRUE)  
colMeans(dzData,na.rm=TRUE)  
cov(mzData,use="complete")  
cov(dzData,use="complete")  
  
# Set Starting Values  
svMe      <- 20              # start value for means  
svVa      <- .8              # start value for variance  
lbVa      <- .0001           # lower bound for variance
```

SAT Deconstructed: Covariance Matrices & Means



```
meanMZ  <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=c("mMZ1", "mMZ2"), name="meanMZ" )
meanDZ  <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=c("mDZ1", "mDZ2"), name="meanDZ" )
```

mMZ1	mMZ2
------	------

meanMZ 1x2

mDZ1	mDZ2
------	------

meanDZ 1x2

```
covMZ   <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv,
  free=TRUE, values=svVas, lbound=lbVas,
  labels=c("vMZ1", "cMZ21", "vMZ2"), name="covMZ" )
```

vMZ1	cMZ21
cMZ21	vMZ2

covMZ 2x2

```
covDZ   <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv,
  free=TRUE, values=svVas, lbound=lbVas,
  labels=c("vDZ1", "cDZ21", "vDZ2"), name="covDZ" )
```

vDZ1	cDZ21
cDZ21	vDZ2

covDZ 2x2

Preparing Model

oneSATc.R

```
# -----  
# PREPARE MODEL  
  
# Create Algebra for expected Mean Matrices  
meanMZ <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=c("mMZ1", "mMZ2"), name="meanMZ" )  
meanDZ <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=c("mDZ1", "mDZ2"), name="meanDZ" )  
full matrix for means  
  
# Create Algebra for expected Variance/Covariance Matrices  
covMZ <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv, free=TRUE, values=valDiag(svVa,ntv), lbound=valDiag(lbVa,ntv),  
labels=c("vMZ1", "cMZ21", "vMZ2"), name="covMZ" )  
covDZ <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv, free=TRUE, values=valDiag(svVa,ntv), lbound=valDiag(lbVa,ntv),  
labels=c("vDZ1", "cDZ21", "vDZ2"), name="covDZ" )  
symmetric matrix for covariances  
  
# Create Data Objects for Multiple Groups  
dataMZ <- mxData( observed=mzData, type="raw" )  
dataDZ <- mxData( observed=dzData, type="raw" )  
fitting to raw data  
  
# Create Expectation Objects for Multiple Groups  
expMZ <- mxExpectationNormal( covariance="covMZ", means="meanMZ", dimnames=selVars )  
expDZ <- mxExpectationNormal( covariance="covDZ", means="meanDZ", dimnames=selVars )  
link to data  
funML <- mxFitFunctionML()  
using FIML: full information maximum likelihood
```

Run Model

oneSATc.R

```
# Create Model Objects for Multiple Groups model object contains all matrices etc.
modelMZ <- mxModel( meanMZ, covMZ, dataMZ, expMZ, funML, name="MZ" )
modelDZ <- mxModel( meanDZ, covDZ, dataDZ, expDZ, funML, name="DZ" )
multi <- mxFitFunctionMultigroup( c("MZ","DZ") ) evaluating 2 groups simultaneously

# Create Confidence Interval Objects
ciCov <- mxCI( c('MZ.covMZ','DZ.covDZ') )
ciMean <- mxCI( c('MZ.meanMZ','DZ.meanDZ') )

# Build Saturated Model with Confidence Intervals
modelSAT <- mxModel( "oneSATc", modelMZ, modelDZ, multi, ciCov, ciMean ) built model

# -----
# RUN MODEL

# Run Saturated Model fitted model
fitSAT <- mxRun( modelSAT, intervals=F )
sumSAT <- summary( fitSAT ) standard summary function in OpenMx

# Print Goodness-of-fit Statistics & Parameter Estimates
fitGofs( fitSAT ) my short summary function in miFunctions.R
fitEsts( fitSAT )
mxGetExpected( fitSAT, c("means","covariance") )
```

Model Building - Model Fitting

```
modelSAT <- mxModel(..
```

built model

```
  name="oneSATc",  
  modelMZ,      modelDZ,  
  name="MZ",    name="DZ",  
  meanMZ,      meanDZ,  
  covMZ,       covDZ,  
  dataMZ,      dataDZ,  
  expMZ,       expDZ,  
  funML        funML,  
  multi,  
  ciCov, ciMean
```

model objects

name of model used in summary
model for means, with start values
model for covariances, with start values
data
expectation (combines models & data)
fit function, here FIML

multigroup, evaluate all groups simultaneously
confidence intervals specified

```
fitSAT <- mxRun(modelSAT)
```

fit model

```
  name="oneSATc",  
  modelMZ,      modelDZ,  
  name="MZ",    name="DZ",  
  meanMZ,      meanDZ,  
  covMZ,       covDZ,  
  dataMZ,      dataDZ,  
  expMZ,       expDZ,  
  funML        funML,  
  multi,  
  ciCov, ciMean
```

model for means, with parameter estimates
model for covariances, with parameter estimates

more of miFunctions.R

```
# Functions to generate output
```

```
fitGofs <- function(fit) {  
  summ <- summary(fit)  
  cat(paste("Mx:", fit$name, " os=", summ$ob, " ns=", summ$nu, " ep=", summ$es,  
           " co=", sum(summ$cons), " df=", summ$de, " ll=", round(summ$Mi,4),  
           " cpu=", round(summ$cpu,4), " opt=", summ$op, " ver=", summ$mx,  
           " stc=", fit$output$status$code, "\n", sep=""))  
}
```

```
fitEsts <- function(fit) {  
  print(round(fit$output$estimate,4))  
}
```

```
fitEstCis <- function(fit) {  
  print(round(fit$output$estimate,4))  
  print(round(fit$output$confidenceIntervals,4))  
}
```

Print Goodness-of-Fit Statistics

```
> summary(fitSAT)
```

```
Model Statistics:
```

	Parameters	Degrees of Freedom	Fit (-2lnL units)
Model:	10	1767	4055.9346
Saturated:	NA	NA	NA
Independence:	NA	NA	NA

```
Number of observations/statistics: 920/1777
```

```
Information Criteria:
```

	df Penalty	Parameters Penalty	Sample-Size Adjusted
AIC:	521.93461	4075.9346	NA
BIC:	-8002.73367	4124.1783	4092.4195

```
CFI: NA
```

```
TLI: 1 (also known as NNFI)
```

```
RMSEA: 0 [95% CI (NA, NA)]
```

```
Prob(RMSEA <= 0.05): NA
```

```
To get additional fit indices, see help(mxRefModels)
```

```
timestamp: 2020-03-01 16:55:41
```

```
Wall clock time: 0.095155001 secs
```

```
optimizer: NPSOL
```

```
OpenMx version number: 2.17.2
```

```
Need help? See help(mxSummary)
```

```
> fitGofs(fitSAT)
```

```
Mx:oneSATc os=1777 ns=920 ep=10 co=0 df=1767 ll=4055.9346 cpu=0.0952 opt=NPSOL ver=2.17.2 stc=0
```


Print Estimates

```
> summary(fitSAT)$parameters
```

```
free parameters:
```

	name	matrix	row	col	Estimate	Std.Error	A	lbound	ubound
1	mMZ1	MZ.meanMZ	1	bmi1	21.34437690	0.036061832			
2	mMZ2	MZ.meanMZ	1	bmi2	21.34901242	0.037650856			
3	vMZ1	MZ.covMZ	bmi1	bmi1	0.72766891	0.043658984		1e-04	
4	cMZ21	MZ.covMZ	bmi1	bmi2	0.59163768	0.040794161		0	
5	vMZ2	MZ.covMZ	bmi2	bmi2	0.79319915	0.047647906		1e-04	
6	mDZ1	DZ.meanDZ	1	bmi1	21.44752035	0.047571928			
7	mDZ2	DZ.meanDZ	1	bmi2	21.45784215	0.049233334			
8	vDZ1	DZ.covDZ	bmi1	bmi1	0.76919130	0.059007266		1e-04	
9	cDZ21	DZ.covDZ	bmi1	bmi2	0.24004049	0.045201541		0	
10	vDZ2	DZ.covDZ	bmi2	bmi2	0.82163163	0.063154677		1e-04	

```
> fitEsts(fitSAT)
```

mMZ1	mMZ2	vMZ1	cMZ21	vMZ2	mDZ1	mDZ2	vDZ1	cDZ21	vDZ2
21.3444	21.3490	0.7277	0.5916	0.7932	21.4475	21.4578	0.7692	0.2400	0.8216

Estimated Values

	Saturated Model					
	MZ twins			DZ twins		
		T1	T2		T1	T2
mean	MZ	21.34	21.35	DZ	21.45	21.46
		T1	T2		T1	T2
COV	T1	0.73		T1	0.77	
	T2	0.59	0.79	T2	0.24	0.82

10 parameters estimated:

mMZ1, mMZ2, vMZ1, vMZ2, cMZ21

mDZ1, mDZ2, vDZ1, vDZ2, cDZ21

Goodness-of-Fit Statistics

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	1777	10	4055.93	1767	521.93			

os	observed statistics	
ep	estimated parameters	
-2ll	-2 LogLikelihood	
df	degrees of freedom	os - ep
AIC	Akaike's Information Criterion	-2ll -2df

Fitting Nested Models

oneSATc.R

```
# Constrain expected Means to be equal across twin order
modelEMO <- mxModel(fit, name="oneEMOc" )
modelEMO <- omxSetParameters( modelEMO, label=c("mMZ1", "mMZ2"), free=TRUE, values=svMe, newlabels='mMZ' )
modelEMO <- omxSetParameters( modelEMO, label=c("mDZ1", "mDZ2"), free=TRUE, values=svMe, newlabels='mDZ' )
fitEMO <- mxRun( modelEMO, intervals=F )
fitGofs(fitEMO); fitEsts(fitEMO)
```

changing parameters

existing parameters

new parameters

```
# Constrain expected Means and Variances to be equal across twin order
modelEMVO <- mxModel(fitEMO, name="oneEMV0c" )
modelEMVO <- omxSetParameters( modelEMVO, label=c("vMZ1", "vMZ2"), free=TRUE, values=svVa, newlabels='vMZ' )
modelEMVO <- omxSetParameters( modelEMVO, label=c("vDZ1", "vDZ2"), free=TRUE, values=svVa, newlabels='vDZ' )
fitEMVO <- mxRun( modelEMVO, intervals=F )
fitGofs(fitEMVO); fitEsts(fitEMVO)
```

```
# Constrain expected Means and Variances to be equal across twin order and zygosity
modelEMVZ <- mxModel(fitEMVO, name="oneEMVZc" )
modelEMVZ <- omxSetParameters( modelEMVZ, label=c("mMZ", "mDZ"), free=TRUE, values=svMe, newlabels='mZ' )
modelEMVZ <- omxSetParameters( modelEMVZ, label=c("vMZ", "vDZ"), free=TRUE, values=svVa, newlabels='vZ' )
fitEMVZ <- mxRun( modelEMVZ, intervals=F )
fitGofs(fitEMVZ); fitEsts(fitEMVZ)
```

```
# Print Comparative Fit Statistics
mxCompare( fitSAT, subs <- list(fitEMO, fitEMVO, fitEMVZ) )
```

generate likelihood ratio test

```
# -----
sink()
save.image(paste(filename, ".Ri", sep=""))
```

close .Ro file & save image as file with .Ri extension

Goodness-of-Fit Stats

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	1777	10	4055.93	1767	521.93			
mT1=mT2	1777	8	4056.00	1769	518.00	0.07	2	0.97
mT1=mT2 varT1=varT2	1777	6	4058.94	1771	516.94	3.01	4	0.56
Zyg MZ=DZ	1777	4	4063.45	1773	517.45	7.52	6	0.28

diff -2ll	likelihood ratio Chi-square	
diff df	difference in degrees of freedom	
p	probability of Chi-square	

Conclusions so far

- BMI in young OZ females (age 18-30)
 - means of twin 1 and twin 2 not significantly different from one another in MZ & DZ pairs
 - variances of twin 1 and twin 2 not significantly different from one another in MZ & DZ pairs
 - means and variances of MZs and DZs not significantly different from one another
- basic data assumptions about CTS met

Twin Correlations ~ Sources of Variance

1-rMZ

E +

rMZ > rDZ

E + **A**

rMZ = 2*rDZ

E + only **A**

rMZ = rDZ

E + only **C**

rDZ > 1/2 rMZ

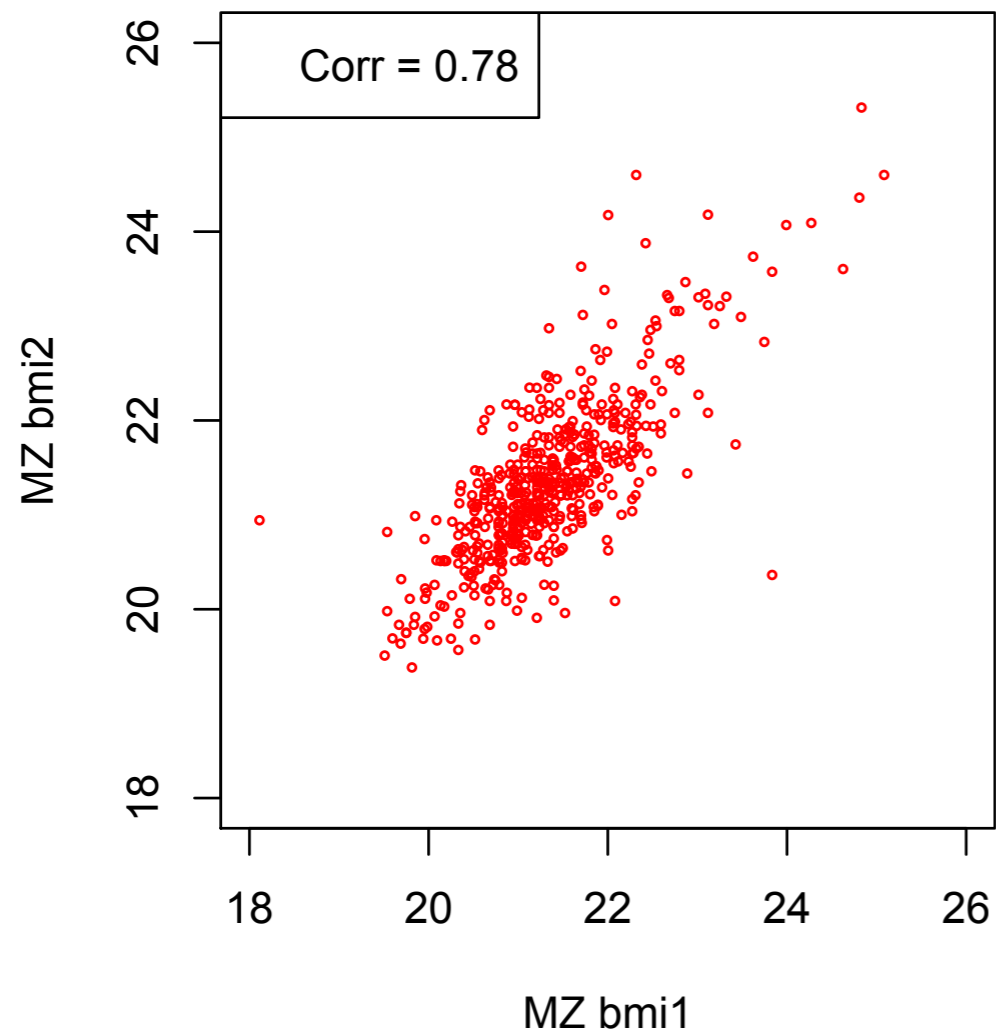
E + **A** & **C**

rDZ < 1/2 rMZ

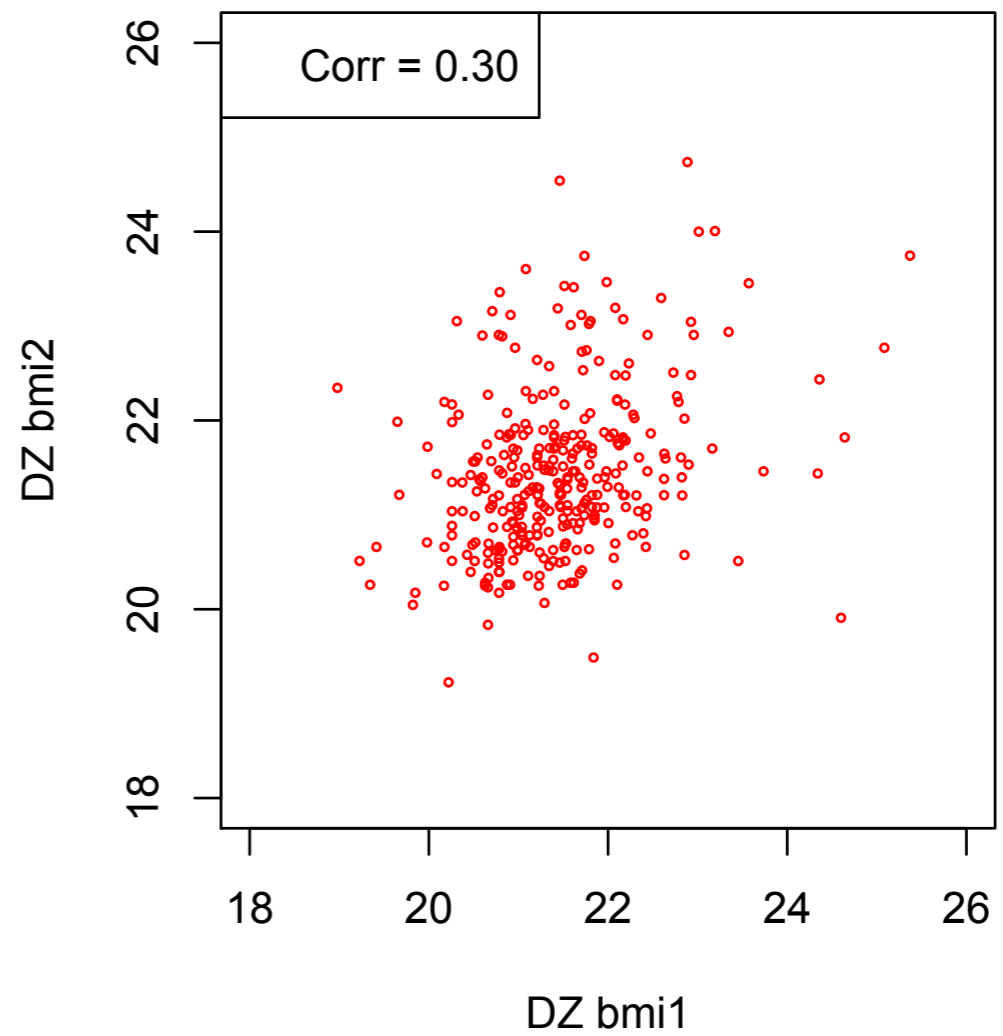
E + **A** & **D**

Example Twin Correlations

MZ BMI



DZ BMI

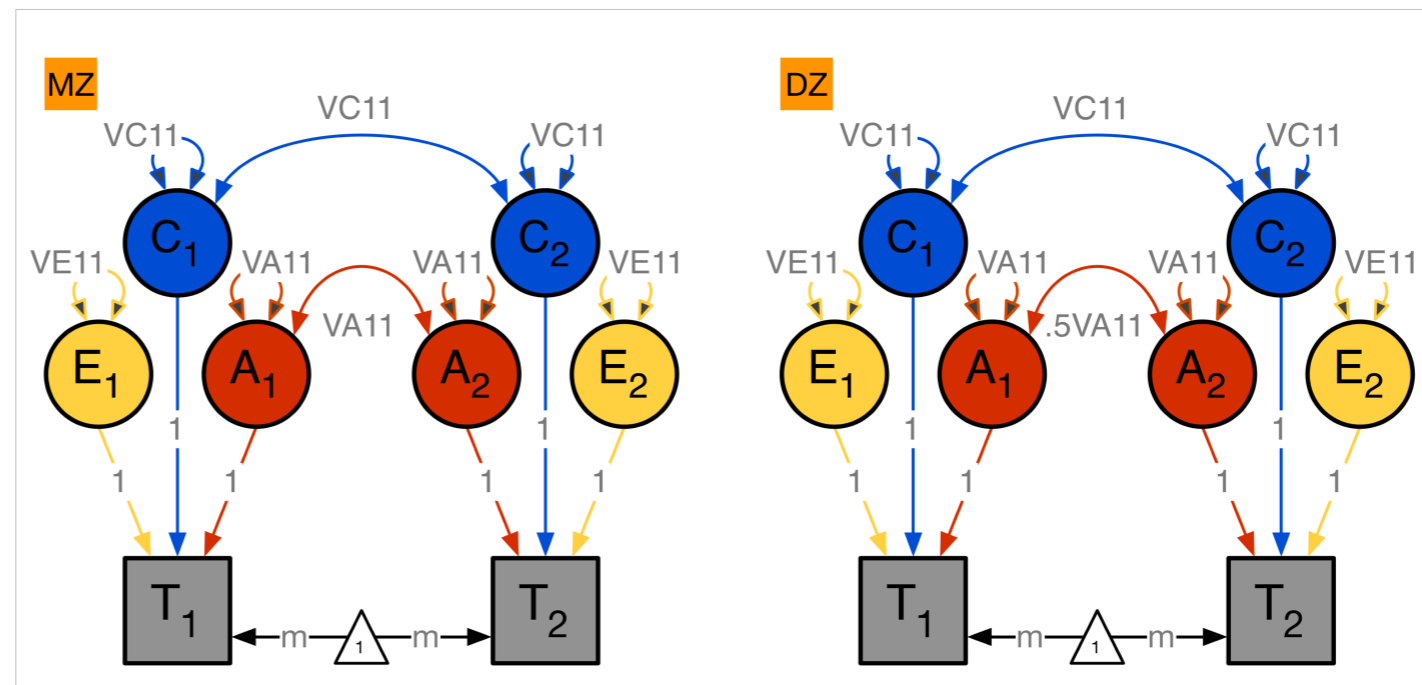


Roadmap for Univariate Analysis

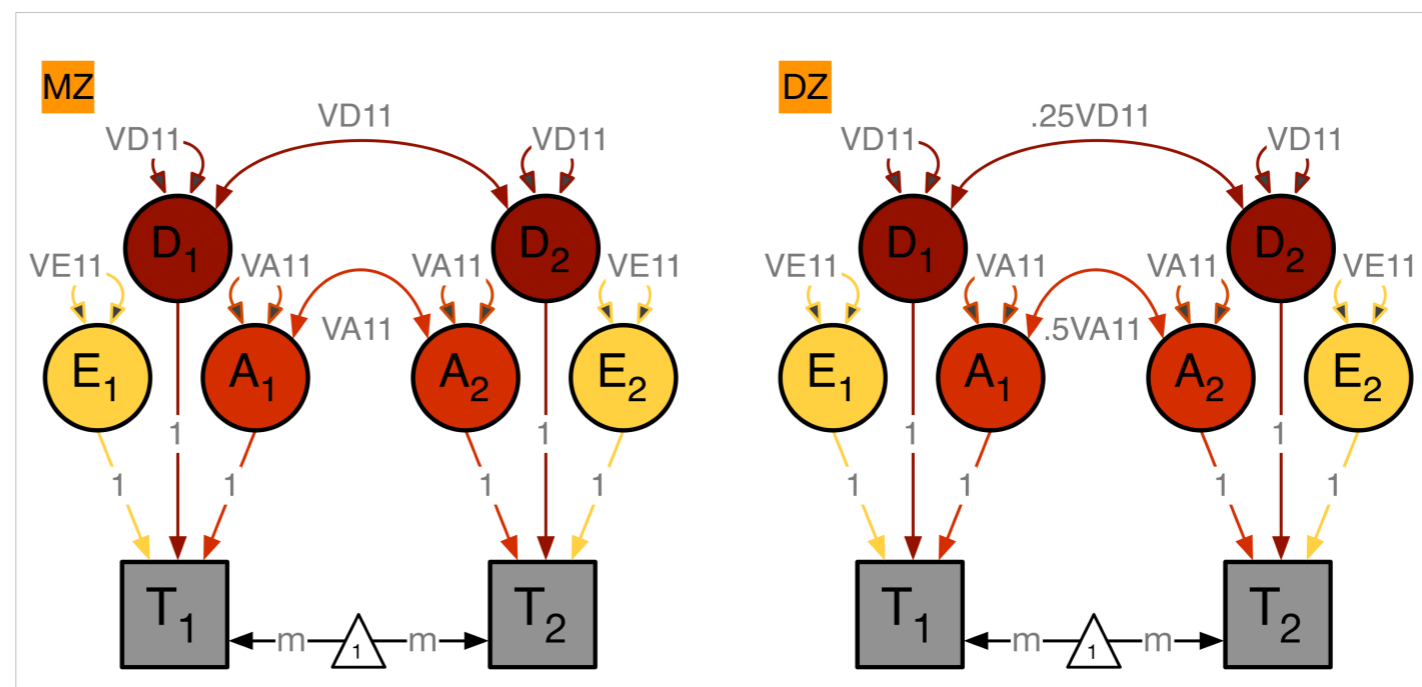
- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
 - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
 - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
 - AE / CE / E Only Models

Univariate ACE / ADE Model **variance estimation**

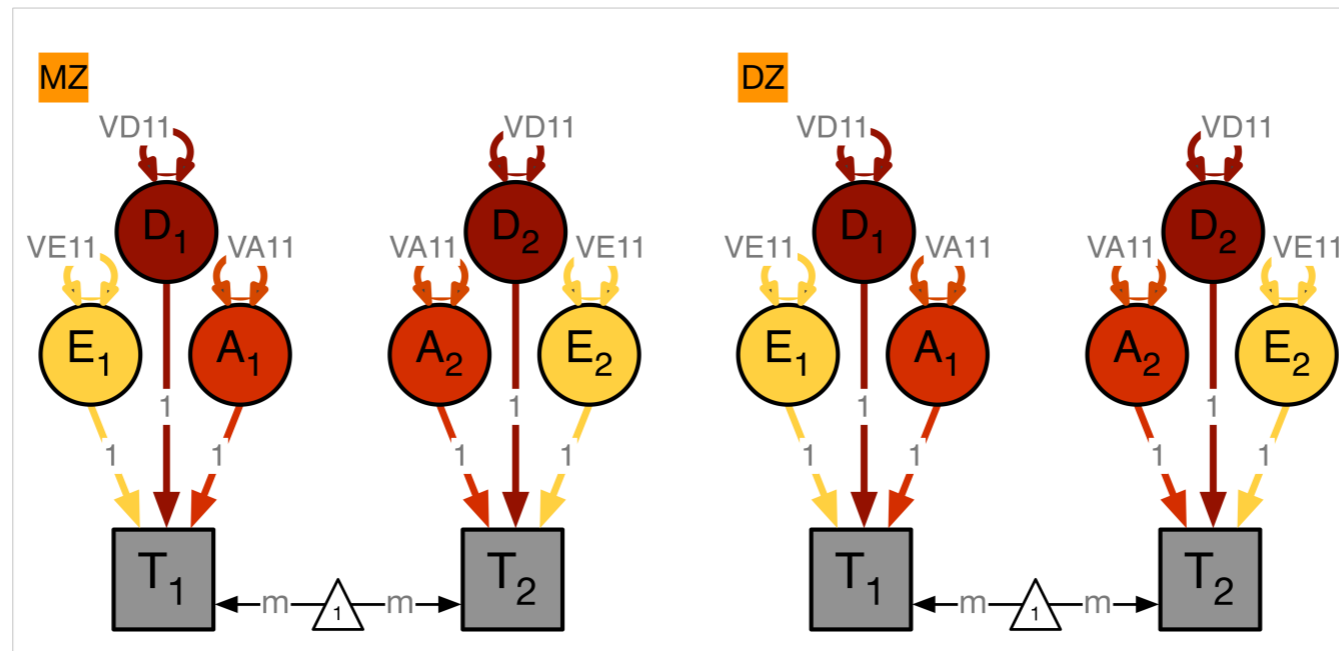
ACE model
`oneACEvc.R`



ADE model
`oneADEvc.R`



ADE Deconstructed: *Variance Components*



```
covA      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPa, label="VA11", name="VA" )
```

VA 1x1

VA11

```
covD      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPa, label="VD11", name="VD" )
```

VD 1x1

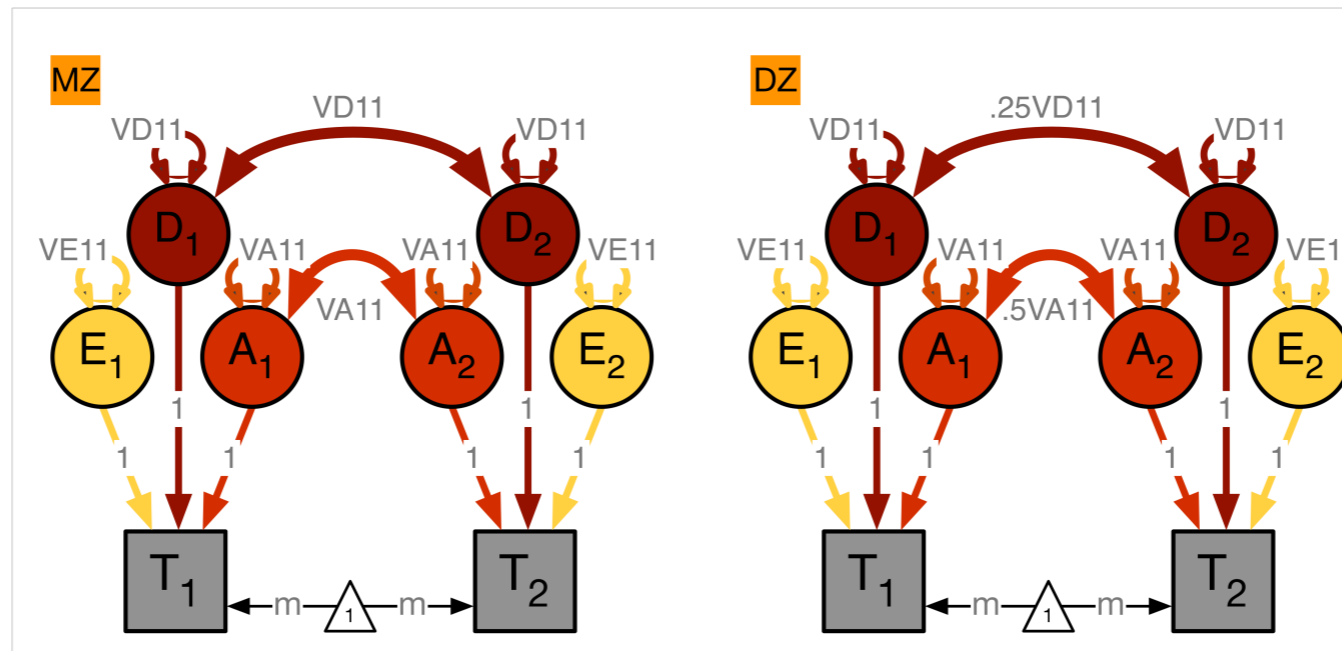
VD11

```
covE      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPe, label="VE11", name="VE" )
```

VE 1x1

VE11

ADE Deconstructed: *Variances + Covariances*



```
covP      <- mxAlgebra( expression= VA+VD+VE,
  name="V" )
```

V	VA+VD+VE
---	----------

V 1x1

```
covMZ     <- mxAlgebra( expression= VA+VD,
  name="cMZ" )
```

cMZ	VA+VD
-----	-------

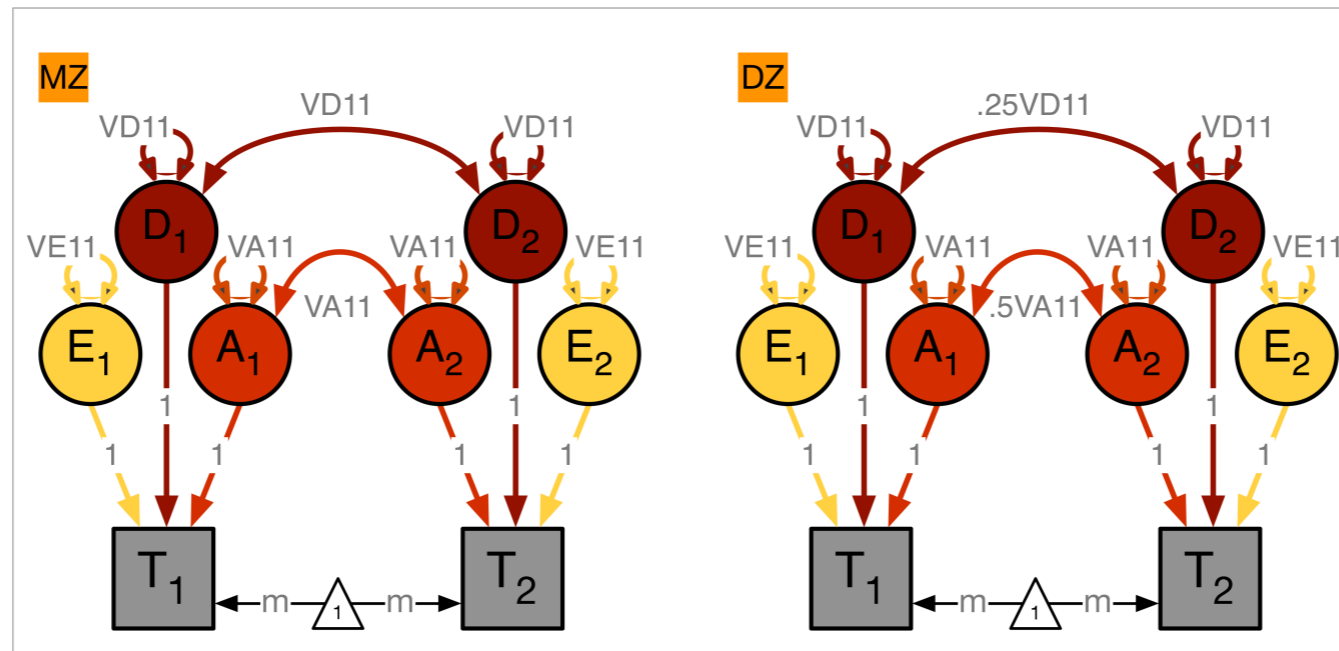
cMZ 1x1

```
covDZ     <- mxAlgebra( expression= 0.5x%VA+ 0.25x%VD,
  name="cDZ" )
```

cDZ	.5VA+.25VD
-----	------------

cDZ 1x1

ADE Deconstructed: Covariance Matrices & Means



```
expCovMZ <- mxAlgebra( expression= rbind(
  cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )
```

```
expCovDZ <- mxAlgebra( expression= rbind(
  cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

```
meanG <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=labVars("mean", vars),
  name="meanG" )
```

V	cMZ
cMZ	V

expCovMZ 2x2

V	cDZ
cDZ	V

expCovDZ 2x2

X1	X1
----	----

meanG 1x2

Model Specification

oneADEvc.R

```
# -----  
# PREPARE MODEL  
  
# Create Algebra for expected Mean Matrices  
meanG      <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=labVars("mean",vars),  
                        name="meanG" )  
  
# Create Matrices for Variance Components  
covA       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPa, label="VA11", name="VA" )  
covD       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPd, label="VD11", name="VD" )  
covE       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPe, label="VE11", name="VE" )  
  
# Create Algebra for expected Variance/Covariance Matrices in MZ & DZ twins  
covP       <- mxAlgebra( expression= VA+VD+VE, name="V" )  
covMZ      <- mxAlgebra( expression= VA+VD, name="cMZ" )  
covDZ      <- mxAlgebra( expression= 0.5%x%VA+ 0.25%x%VD, name="cDZ" )  
expCovMZ   <- mxAlgebra( expression= rbind( cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )  
expCovDZ   <- mxAlgebra( expression= rbind( cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

variance components: VA, VD & VE

Model Specification 2

oneADEvc.R

```
# Create Data Objects for Multiple Groups
```

```
dataMZ <- mxData( observed=mzData, type="raw" )  
dataDZ <- mxData( observed=dzData, type="raw" )
```

```
# Create Expectation Objects for Multiple Groups
```

```
expMZ <- mxExpectationNormal( covariance="expCovMZ", means="meanG", dimnames=selVars )  
expDZ <- mxExpectationNormal( covariance="expCovDZ", means="meanG", dimnames=selVars )  
funML <- mxFitFunctionML()
```

```
# Create Model Objects for Multiple Groups
```

```
pars <- list(meanG, covA, covD, covE, covP) → list of common elements  
modelMZ <- mxModel( pars, covMZ, expCovMZ, dataMZ, expMZ, funML, name="MZ" )  
modelDZ <- mxModel( pars, covDZ, expCovDZ, dataDZ, expDZ, funML, name="DZ" )  
multi <- mxFitFunctionMultigroup( c("MZ", "DZ") )
```

```
# Create Algebra for Variance Components
```

```
rowUS <- rep("US",nv)  
colUS <- rep(c("VA", "VD", "VE", "SA", "SD", "SE"), each=nv)  
estUS <- mxAlgebra( expression=cbind(VA,VD,VE, VA/V,VD/V,VE/V), name="US", dimnames=list(rowUS,colUS))  
→ calculate standardized variance components
```

```
# Create Confidence Interval Objects
```

```
ciADE <- mxCI( "US[1,1:3]" ) → list of matrix elements to calculate confidence intervals (CI)
```

```
# Build Model with Confidence Intervals
```

```
modelADE <- mxModel( "oneADEvc", pars, modelMZ, modelDZ, multi, estUS, ciADE ) → ADE model object
```


summary(fitADE)

free parameters:

	name	matrix	row	col	Estimate	Std.Error	A
1	meanbmi	meanG	1	1	21.39464927	0.025973494	
2	VA11	VA	1	1	0.32092995	0.150909584	
3	VD11	VD	1	1	0.28942518	0.147886812	
4	VE11	VE	1	1	0.16935016	0.010363413	

confidence intervals:

	lbound	estimate	ubound	note
oneADEvc.US[1,1]	0.016290870	0.32092995	0.61208265	
oneADEvc.US[1,2]	0.011924028	0.28942518	0.59556124	
oneADEvc.US[1,3]	0.150553156	0.16935016	0.19139089	

Model Statistics:

	Parameters	Degrees of Freedom	Fit (-2lnL units)
Model:	4	1773	4063.4496
Saturated:	NA	NA	NA
Independence:	NA	NA	NA

Number of observations/statistics: 920/1777

Information Criteria:

	df	Penalty	Parameters	Penalty	Sample-Size Adjusted
AIC:		517.44962		4071.4496	NA
BIC:		-8036.16490		4090.7471	4078.0436

miFunctions: fitGofs & fitEsts

```
> fitGofs(fitADE)
```

```
Mx:oneADEvc  os=1777  ns=920  ep=4  co=0  df=1773  ll=4063.4496  cpu=0.1513  opt=NPSOL  ver=2.17.2  stc=0
```

```
>
```

```
> fitEstCis(fitADE)
```

```
meanbmi  VA11  VD11  VE11  
21.3946  0.3209  0.2894  0.1694
```

```
                lbound estimate ubound  
oneADEvc.US[1,1] 0.0163  0.3209 0.6121  
oneADEvc.US[1,2] 0.0119  0.2894 0.5956  
oneADEvc.US[1,3] 0.1506  0.1694 0.1914
```

```
> round(fitADE$US$result,4)
```

```
      VA      VD      VE      SA      SD      SE  
US 0.3209 0.2894 0.1694 0.4116 0.3712 0.2172
```

Goodness-of-Fit Stats & Estimates

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	1777	10	4055.93	1767	521.93			
ADE	1777	4	4063.45	1773	517.45	7.51	6	0.27

	unstandardized variance components			standardized variance components		
	VA	VD	VE	SA	SD	SE
ADE	0.32	0.29	0.17	0.41	0.37	0.22

Roadmap for Univariate Analysis

- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
 - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
 - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
 - AE / CE / E Only Models

Fitting Nested Models

oneADEvc.R

```
# -----  
# RUN SUBMODELS  
  
# Run AE model  
modelAE <- mxModel( fitADE, name="oneAEc" )  
modelAE <- omxSetParameters( modelAE, labels="VD11", free=FALSE, values=0 )  
fitAE <- mxRun( modelAE, intervals=T )  
fitGofs(fitAE); fitEsts(fitAE)  
  
# Run E model  
modelE <- mxModel( fitAE, name="oneEc" )  
modelE <- omxSetParameters( modelE, labels="VA11", free=FALSE, values=0 )  
fitE <- mxRun( modelE, intervals=T )  
fitGofs(fitE); fitEsts(fitE)  
  
# Print Comparative Fit Statistics  
mxCompare( fitADE, nested <- list(fitAE, fitE) )  
round(rbind(fitADE$US$result, fitAE$US$result, fitE$US$result ),4)
```

dropping parameters

Nested Models

- 'Full' **ADE** Model

- Nested Models

- **AE** Model *vs* **ADE** Model: test significance of **D**

- **E** Model *vs* **AE** Model: test significance of **A**

- **E** Model *vs* **ADE** Model: test significance of both **A & D**

Goodness-of-Fit Statistics **variance estimation**

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	1777	10	4055.93	1767	521.93			
ADE	1777	4	4063.45	1773	517.45	7.51	6	0.27
AE	1777	3	4067.66	1774	519.66	4.21	1	0.04
E	1777	2	4591.79	1775	1041.79	528.34	2	0.00

Under the null hypothesis, test is distributed as a chi-square with 1df



Estimated Values **variance estimation**

	unstandardized variance components			standardized variance components		
	VA	VD	VE	SA	SD	SE
ADE	0.32 0.02-0.61	0.29 0.01-0.60	0.17 0.15-0.19	0.41	0.37	0.22
AE	0.62 0.56-0.68	-	0.17 0.17-0.19	0.78	-	0.22
E	-	-	0.78 0.73-0.83	-	-	1.00

Conclusions

- BMI in young OZ females (age 18-30)
 - **additive** genetic factors: highly significant
 - **dominance**: borderline significant
 - **specific environmental** factors: significant
 - **shared environmental** factors: not

Publications

- Eaves LJ: Inferring the causes of human variation. *J. R. Stat. Soc. Ser. A* 140, 324–355, 1977.
- Neale MC, Cardon LR: *Methodology for Genetic Studies of Twins and Families (NATO ASI Series)*, Dordrecht, The Netherlands: Kluwer Academic Publishers, 496p, 1992.
- Posthuma P, Beem AL, de Geus EJC, van Baal GCM, von Hjelmborg JB, Iachine I, Boomsma DI: Theory and Practice in Quantitative Genetics. *Twin Research* 6:361-376, 2003.
- Eaves LJ, Chen S, Neale M, Maes HH, Silberg J: Questions, Models and Methods in Psychiatric Genetics, in *Psychiatric Genetics (Review of Psychiatry Vol 24)*, Kendler KS & Eaves LJ (Eds). Washington, DC: American Psychiatric Publishing, Inc., 2005.
- Maes HH: The ACE model, in *Encyclopedia for Behavioral Statistics (Wiley Series in Probability and Statistics)*, Purcell S (Volume Editor). John Wiley & Sons, Inc., 2005.
- Neale MC: Biometrical Models in Behavioral Genetics, in *Handbook of Behavior Genetics*, Yong-Kyu, K. (Volume Editor). Springer, 2009.
- Evans DM, Frazer IH, Martin NG: Genetic and environmental causes of variation in basal levels of blood cells, *Twin Research* 2: 250-257, 1999.



Twin Research (1999) 2, 250–257
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<http://www.stockton-press.co.uk/tr>

Genetic and environmental causes of variation in basal levels of blood cells

David M Evans¹, Ian H Frazer² and Nicholas G Martin¹

Calculate Correlations

- add calculations to openMx scripts

- as part of script (calculated with every iteration)

```
# Create Algebra for Maximum Likelihood Estimates of Twin Correlations
```

```
corMZ  <- mxAlgebra( cov2cor(covMZ), name="corMZ" )  
corDZ  <- mxAlgebra( cov2cor(covDZ), name="corDZ" )
```

→ function to calculate correlations from covariances

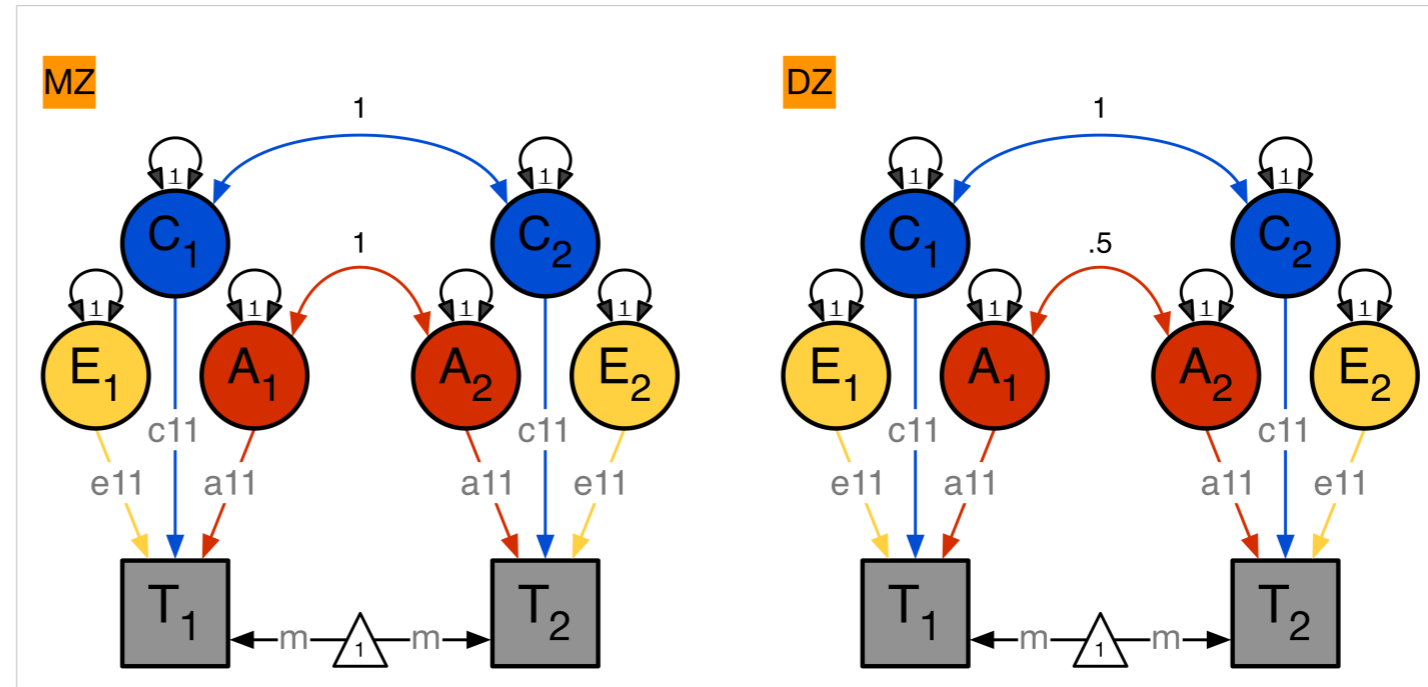
- after script has been run

```
# Create Algebra for Maximum Likelihood Estimates of Twin Correlations
```

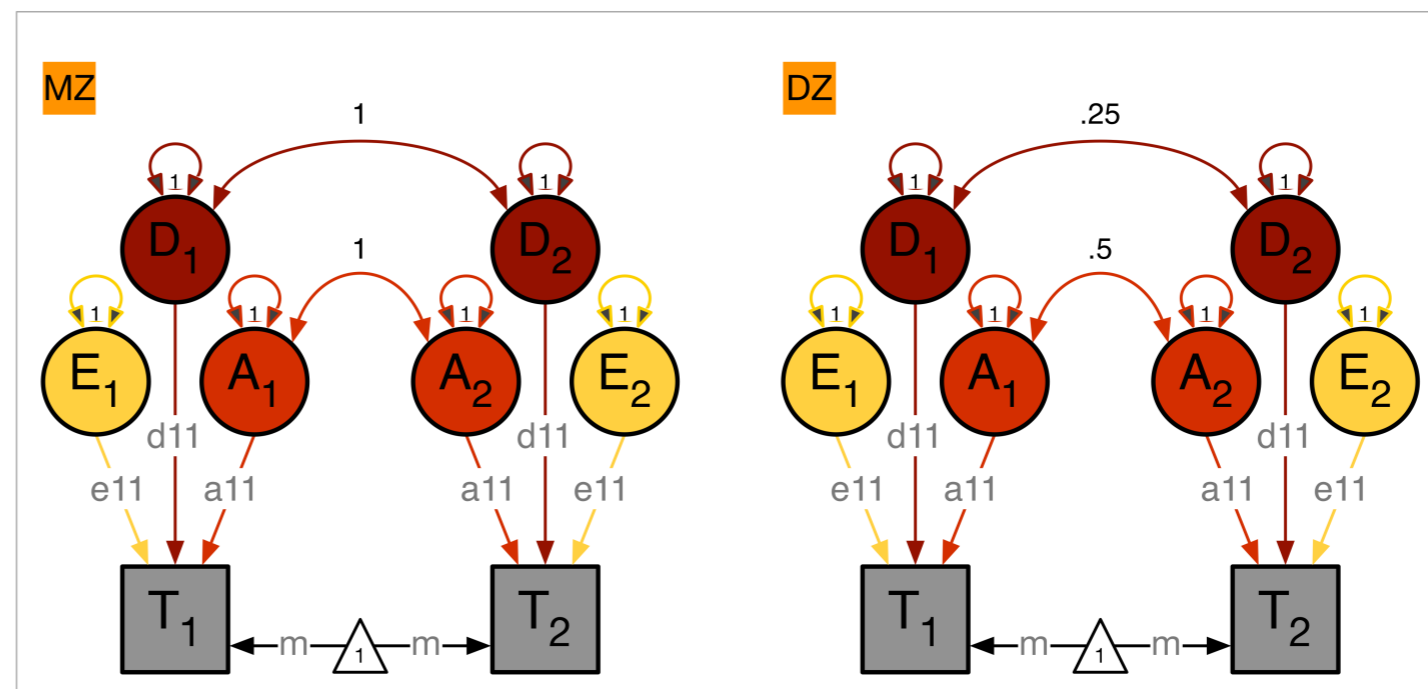
```
corMZ  <- mxEval( cov2cor(covMZ), fitSAT$MZ )  
corDZ  <- mxEval( cov2cor(covDZ), fitSAT$DZ )
```

Univariate ACE / ADE Model - **path estimation**

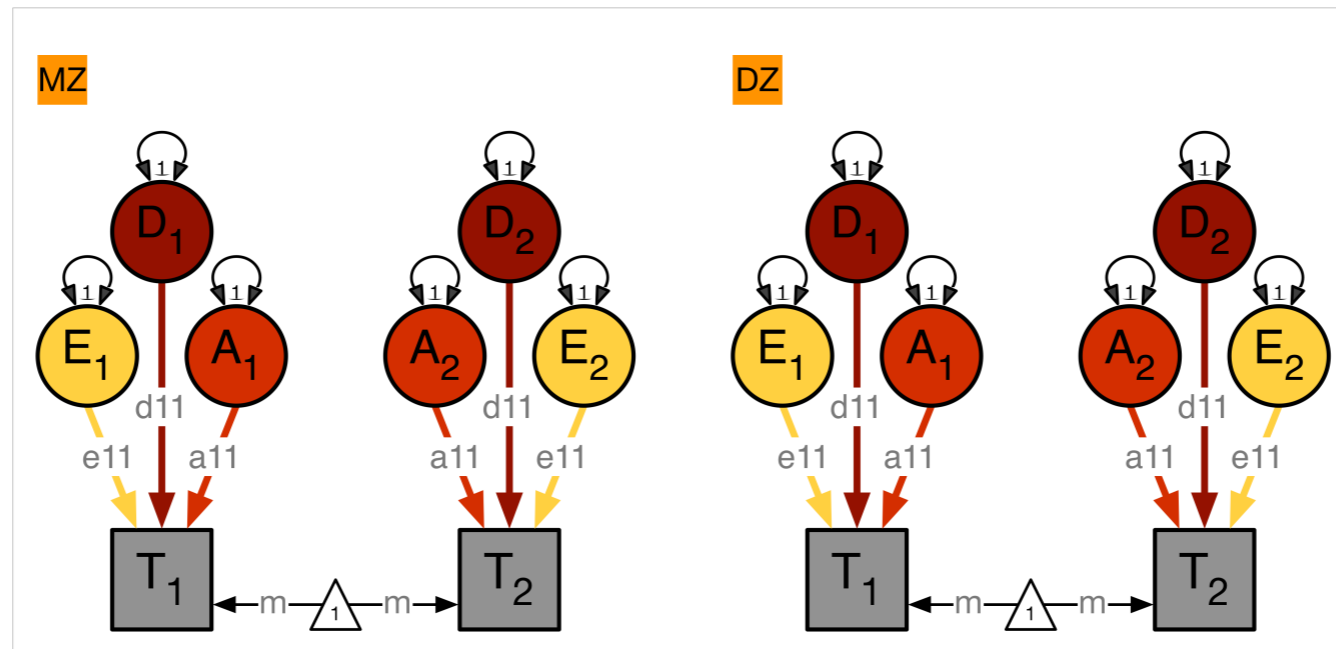
ACE model
`oneACEc.R`



ADE model
`oneADEc.R`



ADE Deconstructed: *Path Coefficients*



```
pathA <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE,
  values=svPa, label="a11", lbound=lbPa, name="a" )
```

a_{11}
a 1x1

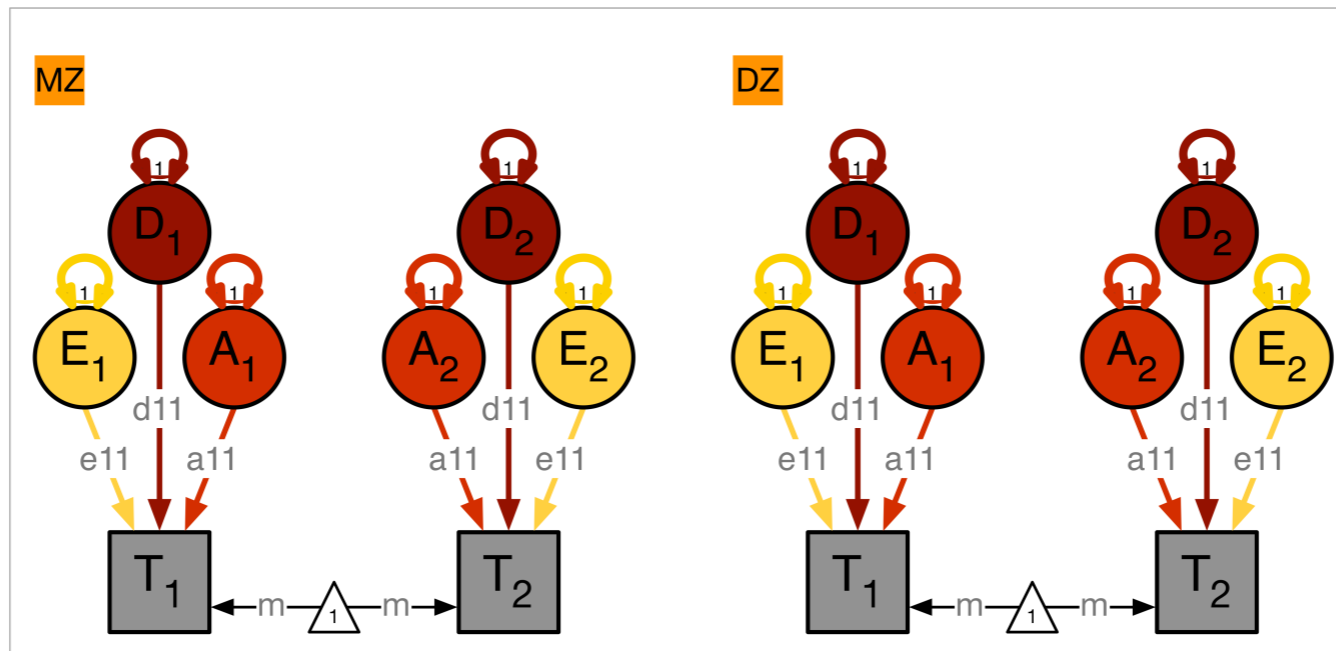
```
pathD <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE,
  values=svPa, label="d11", lbound=lbPa, name="d" )
```

d_{11}
d 1x1

```
pathE <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE,
  values=svPe, label="e11", lbound=lbPa, name="e" )
```

e_{11}
e 1x1

ADE Deconstructed: *Variance Components*



```
covA      <- mxAlgebra( expression=a %*% t(a),
name="A"  )
```

$$\mathbf{A} \begin{matrix} a_{11} \\ 1 \times 1 \end{matrix} * \begin{matrix} t(a_{11}) \end{matrix}$$

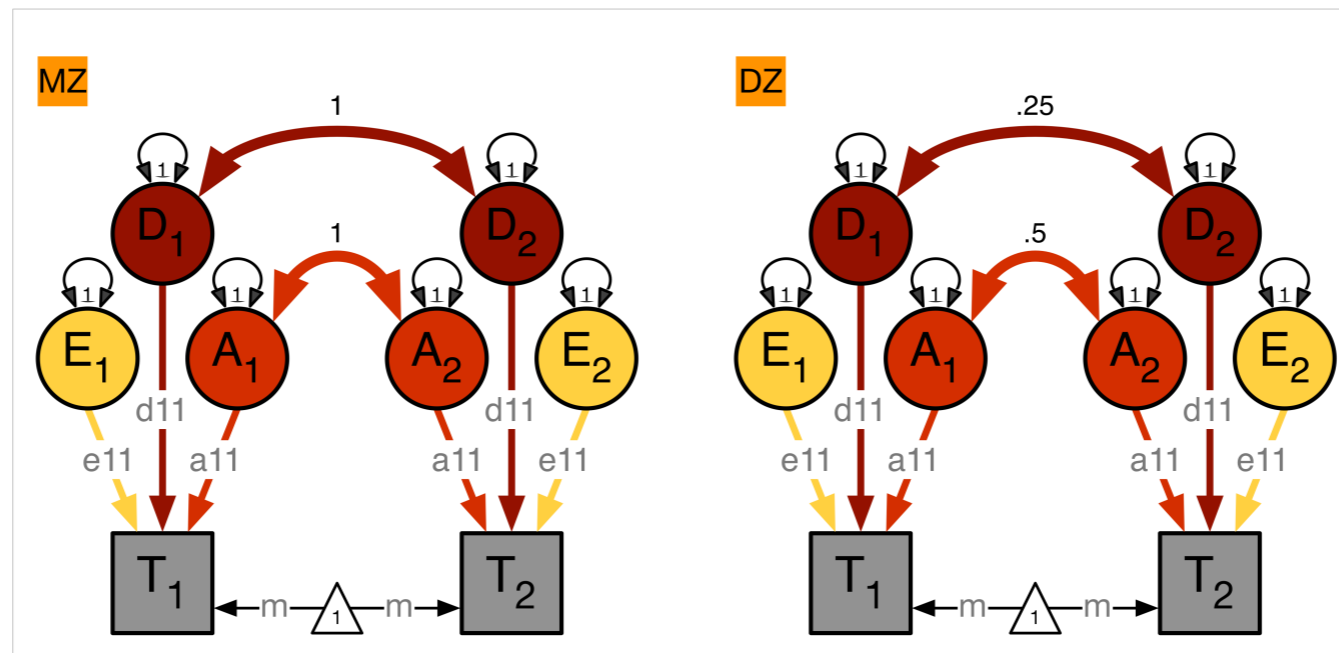
```
covC      <- mxAlgebra( expression=d %*% t(d),
name="D"  )
```

$$\mathbf{D} \begin{matrix} d_{11} \\ 1 \times 1 \end{matrix} * \begin{matrix} t(d_{11}) \end{matrix}$$

```
covE      <- mxAlgebra( expression=e %*% t(e),
name="E"  )
```

$$\mathbf{E} \begin{matrix} e_{11} \\ 1 \times 1 \end{matrix} * \begin{matrix} t(e_{11}) \end{matrix}$$

ADE Deconstructed: *Variances + Covariances*



```
covP      <- mxAlgebra( expression= A+D+E,
  name="V" )
```

V

A+D+E

V 1x1

```
covMZ     <- mxAlgebra( expression= A+D,
  name="cMZ" )
```

cMZ

A+D

cMZ 1x1

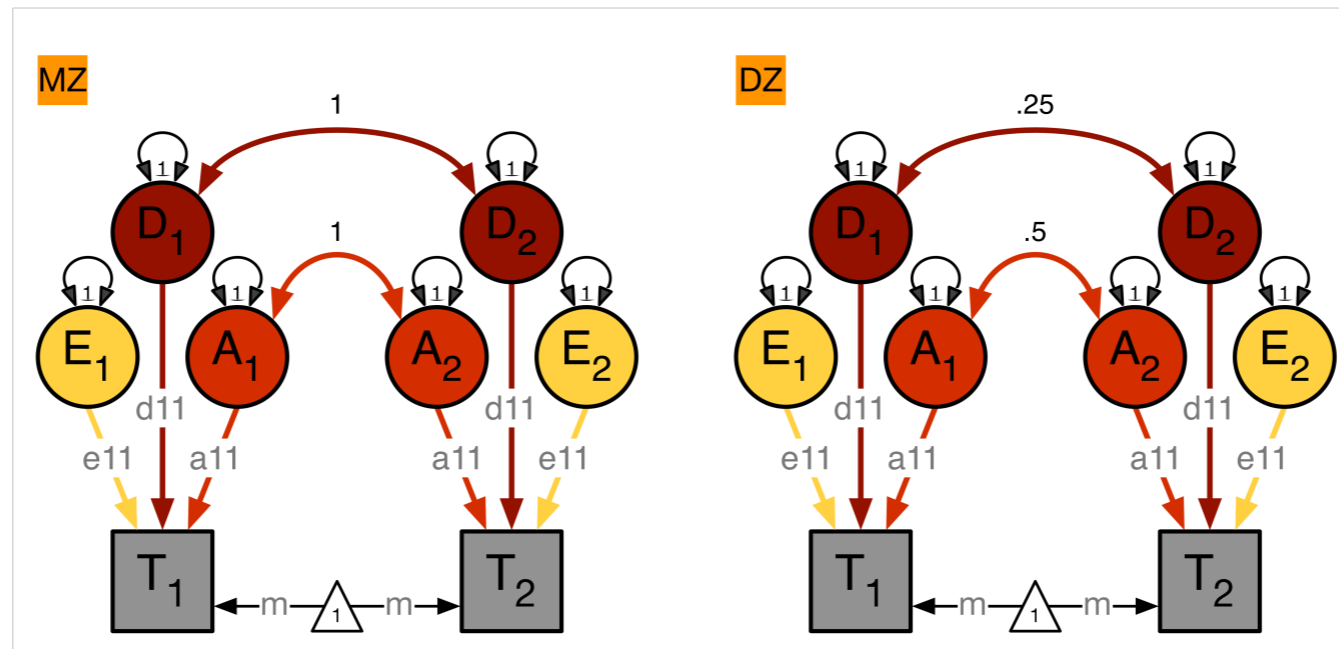
```
covDZ     <- mxAlgebra( expression= 0.5*x%A+ 0.25*x%D,
  name="cDZ" )
```

cDZ

.5A+.25D

cDZ 1x1

ADE Deconstructed: Covariance Matrices & Means



```
expCovMZ <- mxAlgebra( expression= rbind(
  cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )
```

V	cMZ
cMZ	V

expCovMZ 2x2

```
expCovDZ <- mxAlgebra( expression= rbind(
  cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

V	cDZ
cDZ	V

expCovDZ 2x2

```
meanG <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=labVars("mean", vars),
  name="meanG" )
```

X ₁	X ₁
----------------	----------------

meanG 1x2

Model Specification

oneADEc.R

```
# -----  
# PREPARE MODEL  
  
# ADE Model  
# Create Algebra for expected Mean Matrices  
meanG      <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels="x1", name="meanG" )  
  
# Create Matrices for Path Coefficients  
pathA      <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE, values=svPa, label="a11", lbound=lbPa, name="a" )  
pathD      <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE, values=svPa, label="d11", lbound=lbPa, name="d" )  
pathE      <- mxMatrix( type="Lower", nrow=nv, ncol=nv, free=TRUE, values=svPe, label="e11", lbound=lbPa, name="e" )  
                                                    path matrices: a, d & e  
  
# Create Algebra for Variance Components  
covA       <- mxAlgebra( expression=a %*% t(a), name="A" )  
covD       <- mxAlgebra( expression=d %*% t(d), name="D" )  
covE       <- mxAlgebra( expression=e %*% t(e), name="E" )  
                                                    variance components: a2, d2 & e2  
  
# Create Algebra for expected Variance/Covariance Matrices in MZ & DZ twins  
covP       <- mxAlgebra( expression= A+D+E, name="V" )  
covMZ      <- mxAlgebra( expression= A+D, name="cMZ" )  
covDZ      <- mxAlgebra( expression= 0.5x%A+ 0.25x%D, name="cDZ" )  
expCovMZ   <- mxAlgebra( expression= rbind( cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )  
expCovDZ   <- mxAlgebra( expression= rbind( cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

Model Specification 2

oneADEc.R

```
# Create Data Objects for Multiple Groups
```

```
dataMZ  <- mxData( observed=mzData, type="raw" )  
dataDZ  <- mxData( observed=dzData, type="raw" )
```

```
# Create Expectation Objects for Multiple Groups
```

```
expMZ   <- mxExpectationNormal( covariance="expCovMZ", means="meanG", dimnames=selVars )  
expDZ   <- mxExpectationNormal( covariance="expCovDZ", means="meanG", dimnames=selVars )  
funML   <- mxFitFunctionML()
```

```
# Create Model Objects for Multiple Groups
```

```
pars    <- list(meanG, pathA, pathD, pathE, covA, covD, covE, covP)  
modelMZ <- mxModel( pars, covMZ, expCovMZ, dataMZ, expMZ, funML, name="MZ" )  
modelDZ <- mxModel( pars, covDZ, expCovDZ, dataDZ, expDZ, funML, name="DZ" )  
multi   <- mxFitFunctionMultigroup( c("MZ", "DZ") )
```

list of common elements

```
# Create Algebra for Variance Components
```

```
rowUS   <- rep('US',nv)  
colUS   <- rep(c('A','D','E','SA','SD','SE'),each=nv)  
estUS   <- mxAlgebra( expression=cbind(A,D,E,A/V,D/V,E/V), name="US", dimnames=list(rowUS,colUS))
```

ADE variance components

```
# Create Confidence Interval Objects
```

```
ciADE   <- mxCI( "US[1,1:3]" )
```

```
# Build Model with Confidence Intervals
```

```
modelADE <- mxModel( "oneADEc", pars, modelMZ, modelDZ, multi, estUS, ciADE )
```

Fitting Nested Models

oneADEc.R

```
# -----  
# RUN SUBMODELS  
  
# Run AE model  
modelAE <- mxModel( fitADE, name="oneAEc" )  
modelAE <- omxSetParameters( modelAE, labels="d11", free=FALSE, values=0 )  
fitAE <- mxRun( modelAE, intervals=T )  
mxCompare( fitADE, fitAE )  
fitGofs(fitAE)  
fitEsts(fitAE)  
  
# Run E model  
modelE <- mxModel( fitAE, name="oneEc" )  
modelE <- omxSetParameters( modelE, labels="a11", free=FALSE, values=0 )  
fitE <- mxRun( modelE, intervals=T )  
mxCompare( fitAE, fitE )  
fitGofs(fitE)  
fitEsts(fitE)  
  
# Print Comparative Fit Statistics  
mxCompare( fitADE, nested <- list(fitAE, fitE) )  
round(rbind(fitADE$US$result, fitAE$US$result, fitE$US$result ),4)  
  
# -----  
sink()  
save.image(paste(filename, ".Ri", sep=""))
```

dropping path parameters

Goodness-of-Fit Stats **ADE** variance estimation

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p	p/2
Saturated	1777	10	4055.93	1767	521.93				
ADE	1777	4	4063.45	1773	517.45	7.51	6	0.27	
AE	1777	3	4067.66	1774	519.66	4.21	1	0.04	
E	1777	2	4591.79	1775	1041.79	528.34	2	0.00	
path ADE	1777	4	4063.45	1773	517.45	7.51	6	0.27	0.13
path AE	1777	3	4067.66	1774	519.66	4.21	1	0.04	0.02
path E	1777	2	4591.79	1775	1041.79	528.34	2	0.00	0.00

path estimation

Should be divided by 2, as ADE parameters are bounded to be positive

Under the null hypothesis, test is distributed 50:50 as mixture of 0 and a chi-square with 1df

Estimated Values **ADE**

	path coefficients			unstandardized variance components			standardized variance components		
	a	d	e	VA	VD	VE	SA	SD	SE
ADE				0.32 .02-.61	0.29 .01-.60	0.17 .15-.19	0.41	0.37	0.22
AE				0.62	-	0.17	0.78	-	0.22
E				-	-	0.78	-	-	1.00
path ADE	0.57	0.44	0.41	0.32 .02-.61	0.29 .01-.60	0.17 .15-.19	0.41	0.37	0.22
path AE	0.77	-	0.41	0.62	-	0.17	0.78	-	0.22
path E	-	-	0.87	-	-	0.79	-	-	1.00

Goodness-of-Fit Stats **ACE variance estimation**

	os	ep	-2ll	df	AIC	diff -2ll	diff df	p	p/2
Saturated	1777	10	4055.93	1767	521.93				
ACE	1777	4	4063.45	1773	517.45	7.51	6	0.27	
AE	1777	3	4067.66	1774	519.66	4.21	1	0.04	
CE	1777	3	4220.31	1774	672.31	156.86	1	0.00	
E	1777	2	4591.79	1775	1041.79	528.34	2	0.00	
path ACE	1777	4	4067.66	1773	519.66	4.21	6	0.27	0.13
path AE	1777	3	4067.66	1774	519.66	0	1	0.04	0.02
path CE	1777	3	4220.31	1774	672.31	152.65	1	0.00	0.00
path E	1777	2	4591.79	1775	1041.79	524.13	2	0.00	0.00

path estimation

Estimated Values **ACE**

	path coefficients			unstandardized variance components			standardized variance components		
	a	c	e	VA	VC	VE	SA	SC	SE
ACE				0.75	-0.14	0.17	0.97	-0.19	0.22
AE				0.62	-	0.17	0.78	-	0.22
CE				-	0.46	0.32	-	0.59	0.41
E				-	-	0.78	-	-	1.00
path ACE	0.79	0.00	0.41	0.62	0.29	0.17	0.41	0.37	0.22
path AE	0.77	-	0.41	0.62	-	0.17	0.78	-	0.22
path CE	-	0.68	0.56	-	0.46	0.32	-	0.59	0.41
path E	-	-	0.87	-	-	0.79	-	-	1.00

Courtesy of Matt Keller

■ When **D' is negative** in ADE model, then estimates you *would* get in ACE model are:

■ **$C' = -1/2 D'$** & **$A' = \text{covMZ} + 1/2 D'$**

■ So i.e., if D' estimate = -.20 & covMZ = .50 in ADE, then in ACE you'll get C'=.10 & A'=.40

■ Similarly, when **C' is negative** in ACE model, estimates you *would* get in ADE model are:

■ **$D' = -2C'$** & **$A' = \text{covMZ} + 2C'$**

■ So i.e., if C' estimate = -.20 & covMZ = .50 in ACE, then in ADE you'll get A'=.10 & D'=.40

Publications 2

- Hao Wu, Michael C Neale: On the Likelihood Ratio Tests in Bivariate ACDE Models. *Psychometrika* 78 (3), 441-63 Jul 2013.
- Brad Verhulst, Elizabeth Prom-Wormley, Matthew Keller, Sarah Medland, Michael C Neale: Type I Error Rates and Parameter Bias in Multivariate Behavioral Genetic Models. *Behav Genet* 49 (1), 99-111 Jan 2019.

Thank you !

- functions to run saturated / ADE / ACE models

- **umx**

- Tim Bates