

# Univariate/ MonoPhenotype Modeling

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Boulder Workshop 2018

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with credit to Nick Martin, Elizabeth Prom-Wormley,  
Tim Bates & many others

# Questions

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- Does a trait of interest cluster among related individuals?
- Can clustering be explained by genetic or environmental effects?
- Which sources of variance contribute significantly to the variance of the trait?
- How much of the variation in the trait is accounted for by genetic and environmental effects?

# Roadmap for Univariate Analysis

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- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
  - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
  - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
  - AE / CE / E Only Model

# Practical Example

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- Dataset: NH&MRC Twin Register
- 1981 Questionnaire
- BMI (body mass index): weight/height squared
  - kg/m<sup>2</sup>, transformed:  $7 \cdot \log(\text{BMI})$ , simulated based on real data
- Young Female Cohort: 18-30 years
- Sample Size:
  - MZf: 534 pairs (zyg=1; zygosity='MZFF' & cohort='younger')
  - DZf: 328 pairs (zyg=3; zygosity='DZFF' & cohort='younger')

# Dataset

---

```
> head(twinData)
```

```
   fam age zyg part wt1 wt2   ht1   ht2  htwt1  htwt2   bmi1   bmi2
1    1  21   1    2  58  57 1.7000 1.7000 20.0692 19.7232 20.9943 20.8726
2    2  24   1    2  54  53 1.6299 1.6299 20.3244 19.9481 21.0828 20.9519
3    3  21   1    2  55  50 1.6499 1.6799 20.2020 17.7154 21.0405 20.1210
4    4  21   1    2  66  76 1.5698 1.6499 26.7759 27.9155 23.0125 23.3043
5    5  19   1    2  50  48 1.6099 1.6299 19.2894 18.0662 20.7169 20.2583
6    6  26   1    2  60  60 1.5999 1.5698 23.4375 24.3418 22.0804 22.3454
....
```

# My Naming Conventions

---

name of variable(s)	vars	<- 'bmi'
number of variables	nv	<- 1
number of twin variables	ntv	<- nv*2
variables per twin pair	selVars	<-c('bmi1', 'bmi2')
definition variables	covVars	
number of factors	nf	<- 2
number of thresholds	nth	<- 3
starting values	sv	
lower bound / upper bound	lb / ub	
labels	lab	
built model	modelNAME	
fitted model	fitNAME	
summary of fitted model	sumNAME	

# Classical Twin Study Background

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- The Classical Twin Study (CTS) uses MZ and DZ twins reared together
  - MZ twins share 100% of their genes
  - DZ twins share **on average** 50% of their genes
- Expectation: Genetic factors are assumed to contribute to a phenotype when MZ twins are more similar than DZ twins

# Classical Twin Study Assumptions

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- Equal Environments of MZ and DZ pairs
- Random Mating
- No GE Correlation
- No G x E Interaction
- No Sex Limitation
- No G x Age Interaction



# Classical Twin Study Basic Data Assumptions

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- MZ and DZ twins are sampled from the same population, therefore we expect :
  - Equal means/variances in Twin 1 and Twin 2
  - Equal means/variances in MZ and DZ twins
- Further assumptions would need to be tested if we introduce male twins and opposite sex twin pairs

# 'Old Fashioned' Data Checking

---

	MZ		DZ	
	T1	T2	T1	T2
mean	21.34	21.35	21.45	21.46
variance	0.73	0.79	0.77	0.82
covariance	0.59		0.24	

Nice, but how can we actually be sure that these means and variances are truly the same?

# Intuition behind Maximum Likelihood (ML)

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- Likelihood: probability that an observation (data point) is predicted by specified model
- For MLE, determine most likely values of population parameter values (e.g,  $\mu$ ,  $\sigma$ ,  $\beta$ ) given observed sample values
  - Define model
  - Define probability of observing a given event conditional on a particular set of parameters
  - Choose a set of parameters which are most likely to have produced observed results

# Likelihood Ratio Test

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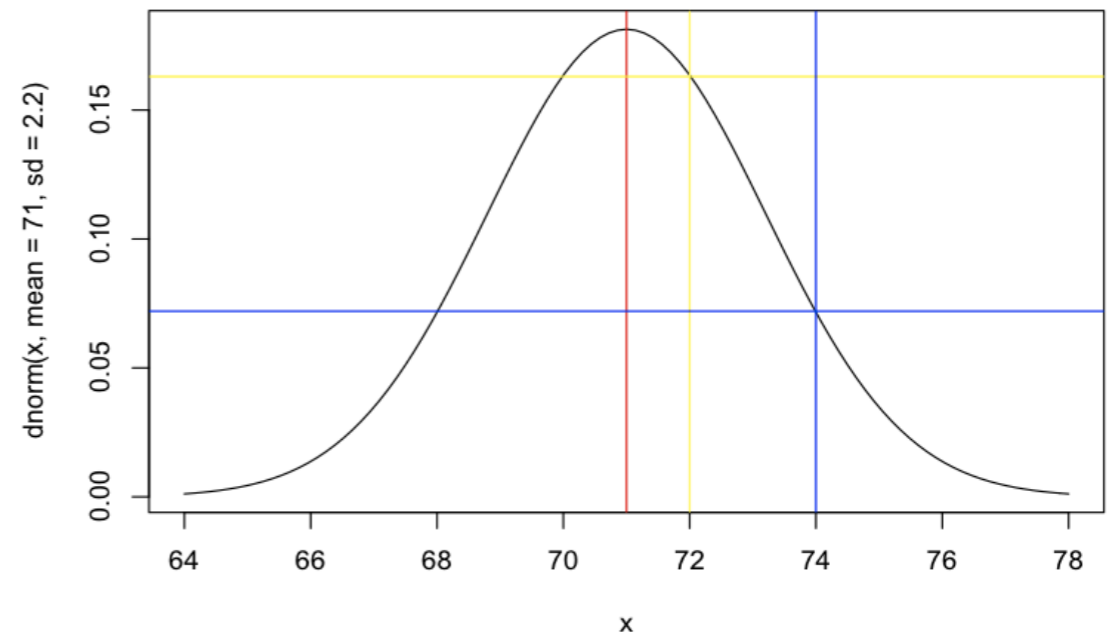
- Likelihood Ratio test is a simple comparison of Log Likelihoods under 2 separate models:
  - Model  $M_u$  is Unconstrained (has more parameters)
  - Model  $M_c$  is Constrained (has fewer parameters)
- LR statistic equals:
  - $LR(M_c | M_u) = 2\ln(L(M_u)) - 2\ln(L(M_c))$
- LR is asymptotically distributed as  $\chi^2$  with the df equal to the number of constraints

# Probability Density Function $\Phi(x_i)$

---

- $\Phi(x_i)$  is likelihood of data point  $x_i$  for particular mean and variance estimates
- Univariate: height of probability density function

$$\Phi(x_i) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-5((x_i-\mu)^2/\sigma^2)}$$

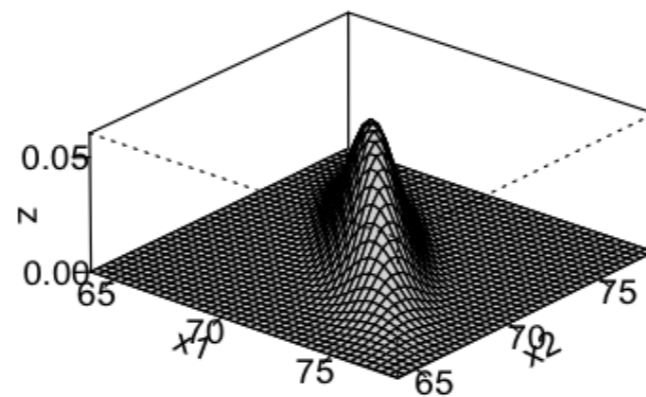


$\pi$ :  $\pi=3.14$ ;  $x_i$ : observed value of variable  $i$ ;  $\mu$ : expected mean;  $\sigma$ : expected variance

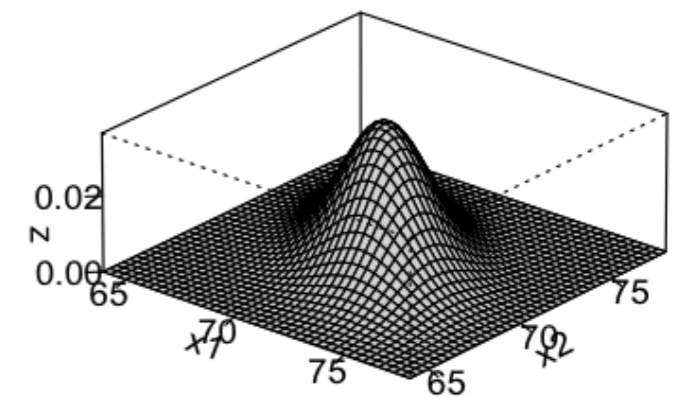
# Multinormal Probability Function

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- $\Phi(x_i)$  is likelihood of pair of data points  $x_i$  and  $y_i$  for particular means, variances and correlation estimates
- Multivariate: height of multinormal probability density function



rMZ=.85



rDZ=.49

$$\Phi(x_i) = - |2\pi\Sigma|^{-n/2} e^{-5((x_i-\mu)\Sigma^{-1}(x_i-\mu)')}$$

$\pi = 3.14$ ;  $x_i$ : value of variable  $i$ ;  $\mu$ : expected mean;  $\Sigma$ : expected covariance matrix

# OpenMx Scripts

---

## ■ oneSATc.R

- Saturated model estimating means & variances for continuous data in MZ & DZ twins

## ■ oneACEvc.R

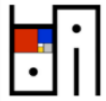
- Univariate/Monophenotype model estimating A, C & E components for continuous data in MZ & DZ twins

## ■ oneADEvc.R

- Univariate/Monophenotype model estimating A, D & E components for continuous data in MZ & DZ twins

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<https://hermine-maes.squarespace.com>



[HOME](#) [OPENMX](#)

genetic epidemiology  
helper functions

HELP

classical twin study  
MZ & DZ twins

**ONE** phenotype  
continuous/binary/ordinal

SAT | ACE | ADE

ONE

classical twin study  
MZ & DZ twins

**ONE** phenotype  
continuous/binary/ordinal  
+covariate

SAT | ACE | ADE

ONEA

classical twin study  
MZ & DZ twins

**TWO** phenotypes  
continuous/binary/ordinal

SAT | ACE | ADE

TWO



<https://hermine-maes.squarespace.com>

HOME OPENMX

	One Phenotype CONTINUOUS (c)	One Phenotype BINARY (b)	One Phenotype ORDINAL (o)	One Phenotype ORDINAL (m) *	One Phenotype UMX c/b/m
<b>SAT</b> estimating means/thresholds, variances & covariances * > 2 categories	 oneSATc.R	 oneSATb.R	 oneSATo.R	 oneSATm.R	 oneSATu.R
<b>ACE</b> estimating variance components	 oneACEvc.R	 oneACEvb.R	 oneACEvo.R	 oneACEvm.R	 oneACEvu.R
<b>ADE</b> estimating variance components	 oneADEvc.R	 oneADEvb.R	 oneADEvo.R	 oneADEvm.R	 oneADEvu.R
NOTE! Models below estimating path coefficients may provide biased estimates of the parameters.					
<b>ACE</b> estimating path coefficients	 oneACEc.R	 oneACEb.R	 oneACEo.R	 oneACEm.R	 oneACEu.R
<b>ADE</b> estimating path coefficients	 oneADEc.R	 oneADEb.R	 oneADEo.R	 oneADEm.R	 oneADEu.R

Back to OpenMx prev / next

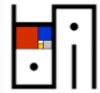
genetic epidemiology  
helper functions

classical twin study  
MZ & DZ twins  
**ONE** phenotype  
continuous/binary/ordinal  
SAT | ACE | ADE

classical twin study  
MZ & DZ twins  
**ONE** phenotype  
continuous/binary/ordinal  
+covariate  
SAT | ACE | ADE

classical twin study  
MZ & DZ twins  
**TWO** phenotypes  
continuous/binary/ordinal  
SAT | ACE | ADE

HELP ONE ONEA TWO



One Phenotype  
CONTINUOUS (c)

One Phenotype  
BINARY (b)

One Phenotype  
ORDINAL (o)

One Phenotype  
ORDINAL (m) \*

One Phenotype  
**UMX** c/b/m

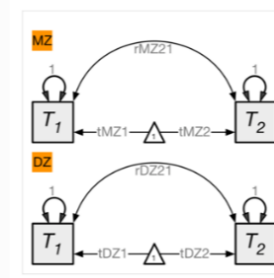
## SAT

estimating means/thresholds, variances & covariances

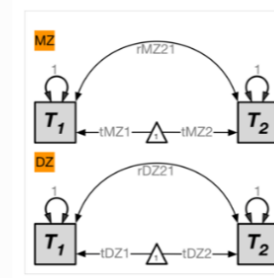
\* > 2 categories



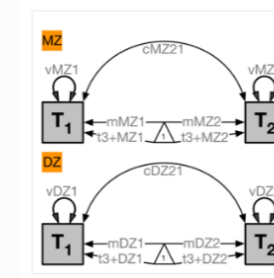
oneSATc.R



oneSATb.R



oneSATo.R



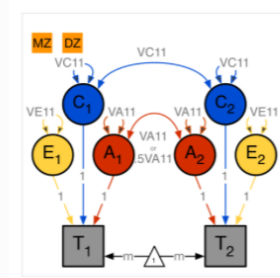
oneSATm.R



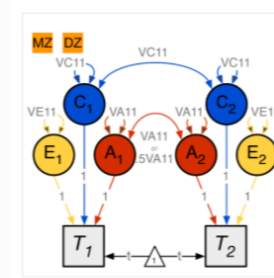
oneSATu.R

## ACE

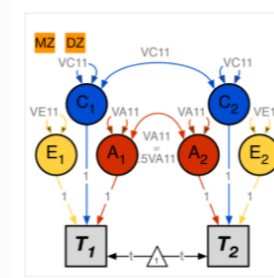
estimating variance components



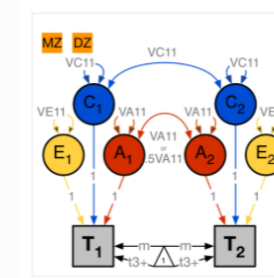
oneACEvc.R



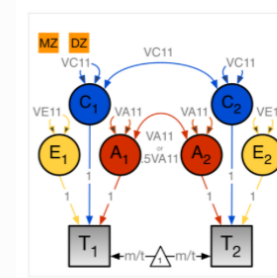
oneACEvb.R



oneACEvo.R



oneACEvm.R



oneACEvu.R



# miFunctions.R

---

```
# -----  
# Program: miFunctions.R  
# Author: Hermine Maes  
# Date: 02 21 2018  
#  
# Set of my options & functions used in basic twin methodology scripts  
# Email: hmaes@vcu.edu  
# -----|-----|-----|-----|-----|-----|-----|-----|  
  
# Options  
mxOption( NULL, "Default optimizer", "NPSOL" )  
#mxOption( NULL, "Checkpoint Prefix", filename )  
mxOption( NULL, "Checkpoint Units", "iterations" )  
mxOption( NULL, "Checkpoint Count", 1 )  
options(width=120)  
options(digits=8)  
mxVersion()  
  
# Functions to assign labels  
labLower <- function(lab,nv) { paste(lab,rev(nv+1-sequence(1:nv)),rep(1:nv,nv:1),sep="") }  
labSdiag <- function(lab,nv) { paste(lab,rev(nv+1-sequence(1:(nv-1))),rep(1:(nv-1),(nv-1):1),sep="") }  
lab0diag <- function(lab,nv) { paste(lab,c(rev(nv+1-sequence(1:(nv-1))),rep(1:(nv-1),(nv-1):1)),c(rep(1:(nv-1),  
(nv-1):1),rev(nv+1-sequence(1:(nv-1))))),sep="") }  
  
...  

```

# Univariate Saturated Model

# oneSATc.R

```
# -----  
# Program: oneSATc.R  
# Author: Hermine Maes  
# Date: 02 25 2016  
#  
# Twin Univariate Saturated model to estimate means and (co)variances across multiple groups  
# Matrix style model - Raw data - Continuous data  
# -----|-----|-----|-----|-----|-----|-----|-----|  
  
# Load Libraries & Options  
rm(list=ls())  
library(OpenMx) → load OpenMx  
library(psych); library(polycor)  
source("miFunctions.R") → my functions which you can edit as you like  
  
# Create Output  
filename <- "oneSATc"  
sink(paste(filename, ".Ro", sep=""), append=FALSE, split=TRUE) → creates output file with extension .Ro
```

# Preparing Data

## oneSATc.R

```
# -----  
# PREPARE DATA  
  
# Load Data  
data(twinData) → load 'twinData' or read in your own  
dim(twinData)  
describe(twinData[,1:12], skew=F)  
  
# Select Variables for Analysis  
vars      <- 'bmi'           # list of variables names  
nv        <- 1               # number of variables  
ntv       <- nv*2            # number of total variables  
selVars   <- paste(vars,c(rep(1,nv),rep(2,nv)),sep="") → analyzing c('bmi1','bmi2')  
# Select Data for Analysis  
mzData    <- subset(twinData, zyg==1, selVars) # zygosity='MMFF' & cohort='younger'  
dzData    <- subset(twinData, zyg==3, selVars) → get right codes for zygosity  
  
# Set Starting Values  
svMe      <- 20              # start value for means  
svVa      <- .8              # start value for variance  
lbVa      <- .0001           # lower bound for variance
```

# SAT Deconstructed: Covariance Matrices & Means



```
meanMZ   <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=c("mMZ1", "mMZ2"), name="meanMZ" )
meanDZ   <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels=c("mDZ1", "mDZ2"), name="meanDZ" )
```

mMZ1	mMZ2
------	------

**meanMZ** 1x2

mDZ1	mDZ2
------	------

**meanDZ** 1x2

```
covMZ    <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv,
  free=TRUE, values=svVas, lbound=lbVas,
  labels=c("vMZ1", "cMZ21", "vMZ2"), name="covMZ" )
```

vMZ1	cMZ21
cMZ21	vMZ2

**covMZ** 2x2

```
covDZ    <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv,
  free=TRUE, values=svVas, lbound=lbVas,
  labels=c("vDZ1", "cDZ21", "vDZ2"), name="covDZ" )
```

vDZ1	cDZ21
cDZ21	vDZ2

**covDZ** 2x2

# Preparing Model

## oneSATc.R

```
# -----  
# PREPARE MODEL  
  
# Create Algebra for expected Mean Matrices  
meanMZ <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=c("mMZ1", "mMZ2"), name="meanMZ" )  
meanDZ <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=c("mDZ1", "mDZ2"), name="meanDZ" )  
# full matrix for means  
  
# Create Algebra for expected Variance/Covariance Matrices  
covMZ <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv, free=TRUE, values=svVas, lbound=lbVas, labels=c("vMZ1", "cMZ21", "vMZ2"), name="covMZ" )  
covDZ <- mxMatrix( type="Symm", nrow=ntv, ncol=ntv, free=TRUE, values=svVas, lbound=lbVas, labels=c("vDZ1", "cDZ21", "vDZ2"), name="covDZ" )  
# symmetric matrix for covariances  
  
# Create Data Objects for Multiple Groups  
dataMZ <- mxData( observed=mzData, type="raw" )  
dataDZ <- mxData( observed=dzData, type="raw" )  
# fitting to raw data  
  
# Create Expectation Objects for Multiple Groups  
expMZ <- mxExpectationNormal( covariance="covMZ", means="meanMZ", dimnames=selVars )  
expDZ <- mxExpectationNormal( covariance="covDZ", means="meanDZ", dimnames=selVars )  
funML <- mxFitFunctionML()  
# link to data  
# using FIML: full information maximum likelihood
```

# Run Model

# oneSATc.R

```
# Create Model Objects for Multiple Groups → model object contains all matrices etc.
modelMZ <- mxModel( meanMZ, covMZ, matI, corMZ, dataMZ, expMZ, funML, name="MZ" )
modelDZ <- mxModel( meanDZ, covDZ, matI, corDZ, dataDZ, expDZ, funML, name="DZ" )
multi <- mxFitFunctionMultigroup( c("MZ","DZ") ) → evaluating 2 groups simultaneously

# Create Confidence Interval Objects
ciCov <- mxCI( c('MZ.covMZ','DZ.covDZ') )
ciMean <- mxCI( c('MZ.meanMZ','DZ.meanDZ') )

# Build Saturated Model with Confidence Intervals
modelSAT <- mxModel( "oneSATc", modelMZ, modelDZ, multi, ciCov, ciMean ) → built model

# -----
# RUN MODEL

# Run Saturated Model → fitted model
fitSAT <- mxRun( modelSAT, intervals=F )
sumSAT <- summary( fitSAT ) → standard summary function in OpenMx

# Print Goodness-of-fit Statistics & Parameter Estimates
fitGofs( fitSAT ) → my short summary function in miFunctions.R
fitEsts( fitSAT )
mxGetExpected( fitSAT, c("means","covariance") )
```



# Model Building - Model Fitting

```
modelSAT <- mxModel(..
```

built model

```
  name="oneSATc",  
  modelMZ,      modelDZ,  
  name="MZ",    name="DZ",  
  meanMZ,      meanDZ,  
  covMZ,       covDZ,  
  dataMZ,      dataDZ,  
  expMZ,       expDZ,  
  funML        funML,  
  multi,  
  ciCov, ciMean
```

model objects

name of model used in summary  
model for means, with start values  
model for covariances, with start values  
data  
expectation (combines models & data)  
fit function, here FIML

multigroup, evaluate all groups simultaneously  
confidence intervals specified

```
fitSAT <- mxRun(modelSAT)
```

fit model

```
  name="oneSATc",  
  modelMZ,      modelDZ,  
  name="MZ",    name="DZ",  
  meanMZ,      meanDZ,  
  covMZ,       covDZ,  
  dataMZ,      dataDZ,  
  expMZ,       expDZ,  
  funML        funML,  
  multi,  
  ciCov, ciMean
```

model for means, with parameter estimates  
model for covariances, with parameter estimates

# more of miFunctions.R

---

```
# Functions to generate output
```

```
fitGofs <- function(fit) {  
  summ <- summary(fit)  
  cat(paste("Mx:", fit$name, " os=", summ$obj, " ns=", summ$nu, " ep=", summ$es,  
           " co=", sum(summ$cons), " df=", summ$de, " ll=", round(summ$Mi,4),  
           " cpu=", round(summ$cpu,4), " opt=", summ$op, " ver=", summ$mx,  
           " stc=", fit$output$status$code, "\n", sep=""))  
}
```

```
fitEsts <- function(fit) {  
  print(round(fit$output$estimate,4))  
}
```

```
fitEstCis <- function(fit) {  
  print(round(fit$output$estimate,4))  
  print(round(fit$output$confidenceIntervals,4))  
}
```

# Print Estimates

---

```
> summary(fitSAT)$parameters
```

```
free parameters:
```

	name	matrix	row	col	Estimate	Std.Error	A	lbound	ubound
1	mMZ1	MZ.meanMZ	1	bmi1	21.34437690	0.036061833			
2	mMZ2	MZ.meanMZ	1	bmi2	21.34901242	0.037650856			
3	vMZ1	MZ.covMZ	bmi1	bmi1	0.72766891	0.043659075		1e-04	
4	cMZ21	MZ.covMZ	bmi1	bmi2	0.59163768	0.040794223		0	
5	vMZ2	MZ.covMZ	bmi2	bmi2	0.79319915	0.047647955		1e-04	
6	mDZ1	DZ.meanDZ	1	bmi1	21.44752035	0.047571928			
7	mDZ2	DZ.meanDZ	1	bmi2	21.45784215	0.049233334			
8	vDZ1	DZ.covDZ	bmi1	bmi1	0.76919130	0.059007408		1e-04	
9	cDZ21	DZ.covDZ	bmi1	bmi2	0.24004048	0.045201686		0	
10	vDZ2	DZ.covDZ	bmi2	bmi2	0.82163163	0.063154276		1e-04	

```
> fitEsts(fitSAT)
```

mMZ1	mMZ2	vMZ1	cMZ21	vMZ2	mDZ1	mDZ2	vDZ1	cDZ21	vDZ2
21.3444	21.3490	0.7277	0.5916	0.7932	21.4475	21.4578	0.7692	0.2400	0.8216

# Print Goodness-of-Fit Statistics

---

```
> summary(fitSAT)
```

```
Model Statistics:
```

	Parameters	Degrees of Freedom	Fit (-2lnL units)
Model:	10	1767	4055.9346
Saturated:	NA	NA	NA
Independence:	NA	NA	NA

```
Number of observations/statistics: 920/1777
```

```
Information Criteria:
```

	df Penalty	Parameters Penalty	Sample-Size Adjusted
AIC:	521.93461	4075.9346	NA
BIC:	-8002.73367	4124.1783	4092.4195

```
CFI: NA
```

```
TLI: 1 (also known as NNFI)
```

```
RMSEA: 0 [95% CI (NA, NA)]
```

```
Prob(RMSEA <= 0.05): NA
```

```
To get additional fit indices, see help(mxRefModels)
```

```
timestamp: 2018-03-04 17:12:56
```

```
Wall clock time: 0.061913013 secs
```

```
optimizer: NPSOL
```

```
OpenMx version number: 2.8.3
```

```
Need help? See help(mxSummary)
```

```
> fitGofs(fitSAT)
```

```
Mx:oneSATc os=1777 ns=920 ep=10 co=0 df=1767 ll=4055.9346 cpu=0.0619 opt=NPSOL ver=2.8.3 stc=0
```

# Estimated Values

---

	Saturated Model					
		T1	T2		T1	T2
mean	MZ	21.34	21.35	DZ	21.45	21.46
		T1	T2		T1	T2
cov	T1	0.73		T1	0.77	
	T2	0.59	0.79	T2	0.24	0.82

10 parameters estimated:  
mMZ1, mMZ2, vMZ1, vMZ2, cMZ21  
mDZ1, mDZ1, vDZ1, vDZ2, cDZ21

# Goodness-of-Fit Statistics

---

	ep	-2ll	df	AIC			
Sat	10	4055.94	1767	521.93			

os	observed statistics		
ep	estimated parameters		
-2ll	-2 LogLikelihood		
df	degrees of freedom		os - ep
AIC	Akaike's Information Criterion		-2ll -2df

# Fitting Nested Models

## oneSATc.R

```
# Constrain expected Means to be equal across twin order
modelEMO <- mxModel(fit, name="oneEMOc" )
modelEMO <- omxSetParameters( modelEMO, label=c("mMZ1", "mMZ2"), free=TRUE, values=svMe, newlabels='mMZ' )
modelEMO <- omxSetParameters( modelEMO, label=c("mDZ1", "mDZ2"), free=TRUE, values=svMe, newlabels='mDZ' )
fitEMO <- mxRun( modelEMO, intervals=F )
fitGofs(fitEMO); fitEsts(fitEMO)
```

changing parameters

```
# Constrain expected Means and Variances to be equal across twin order
modelEMVO <- mxModel(fitEMO, name="oneEMV0c" )
modelEMVO <- omxSetParameters( modelEMVO, label=c("vMZ1", "vMZ2"), free=TRUE, values=svVa, newlabels='vMZ' )
modelEMVO <- omxSetParameters( modelEMVO, label=c("vDZ1", "vDZ2"), free=TRUE, values=svVa, newlabels='vDZ' )
fitEMVO <- mxRun( modelEMVO, intervals=F )
fitGofs(fitEMVO); fitEsts(fitEMVO)
```

```
# Constrain expected Means and Variances to be equal across twin order and zygosity
modelEMVZ <- mxModel(fitEMVO, name="oneEMVZc" )
modelEMVZ <- omxSetParameters( modelEMVZ, label=c("mMZ", "mDZ"), free=TRUE, values=svMe, newlabels='mZ' )
modelEMVZ <- omxSetParameters( modelEMVZ, label=c("vMZ", "vDZ"), free=TRUE, values=svVa, newlabels='vZ' )
fitEMVZ <- mxRun( modelEMVZ, intervals=F )
fitGofs(fitEMVZ); fitEsts(fitEMVZ)
```

```
# Print Comparative Fit Statistics
mxCompare( fitSAT, subs <- list(fitEMO, fitEMVO, fitEMVZ) )
```

generate likelihood ratio test

```
# -----
sink()
save.image(paste(filename, ".Ri", sep=""))
```

close .Ro file & save image as file with .Ri extension

# Goodness-of-Fit Stats

---

	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	10	4055.93	1767	521.93			
mT1=mT2	8	4056.00	1769	518.00	0.07	2	0.97
mT1=mT2 varT1=varT2	6	4058.94	1771	516.94	3.01	4	0.56
Zyg MZ=DZ	4	4063.45	1773	517.45	7.52	6	0.28

diff -2ll	likelihood ratio Chi-square	
diff df	difference in degrees of freedom	
p	probability of Chi-square	



# Conclusions so far

---

- BMI in young OZ females (age 18-30)
  - means of twin 1 and twin 2 not significantly different from one another in MZ & DZ pairs
  - variances of twin 1 and twin 2 not significantly different from one another in MZ & DZ pairs
  - means and variances of MZs and DZs not significantly different from one another
  - basic data assumptions about CTS met

# Twin Correlations ~ Sources of Variance

---

$1 - r_{MZ}$

E

$r_{MZ} > r_{DZ}$

A

$r_{MZ} = 2 * r_{DZ}$

only A

$r_{MZ} = r_{DZ}$

only C

$r_{MZ} < 1/2 r_{DZ}$

A & C

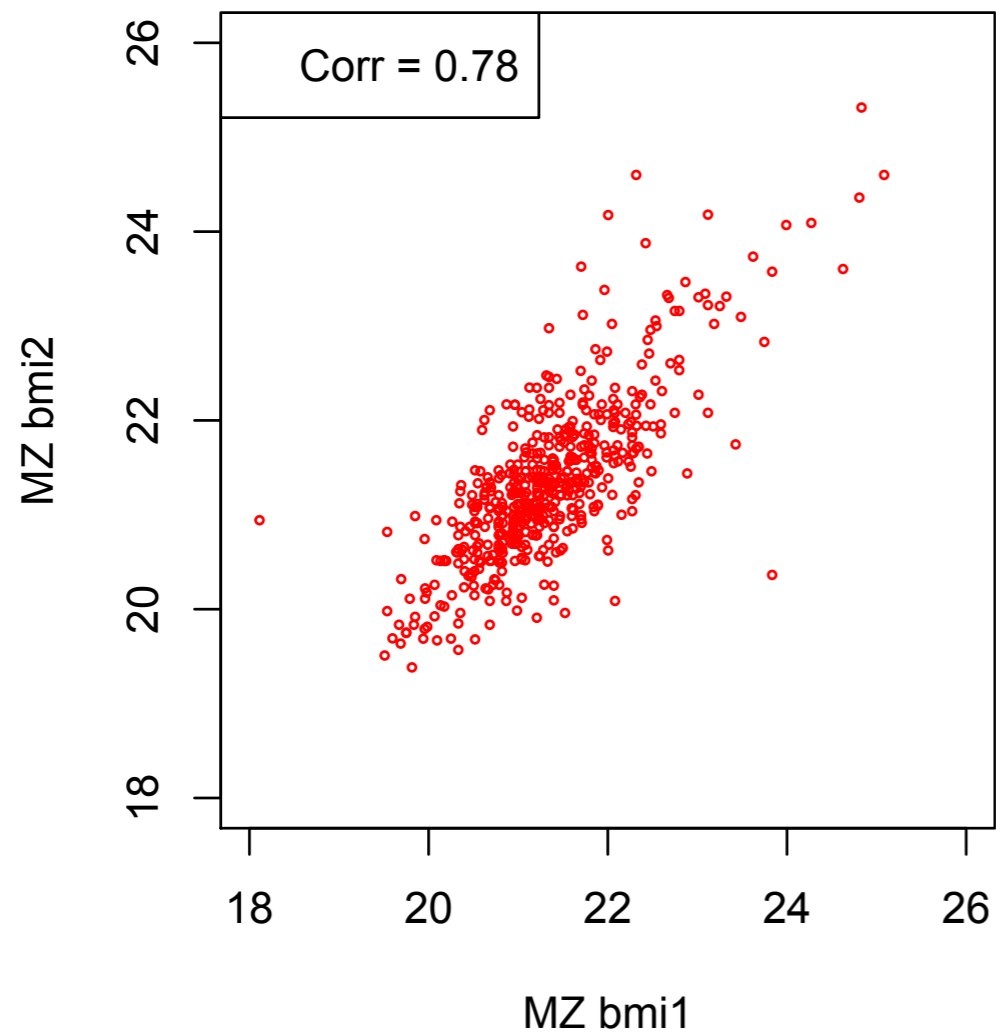
$r_{MZ} > 1/2 r_{DZ}$

A & D

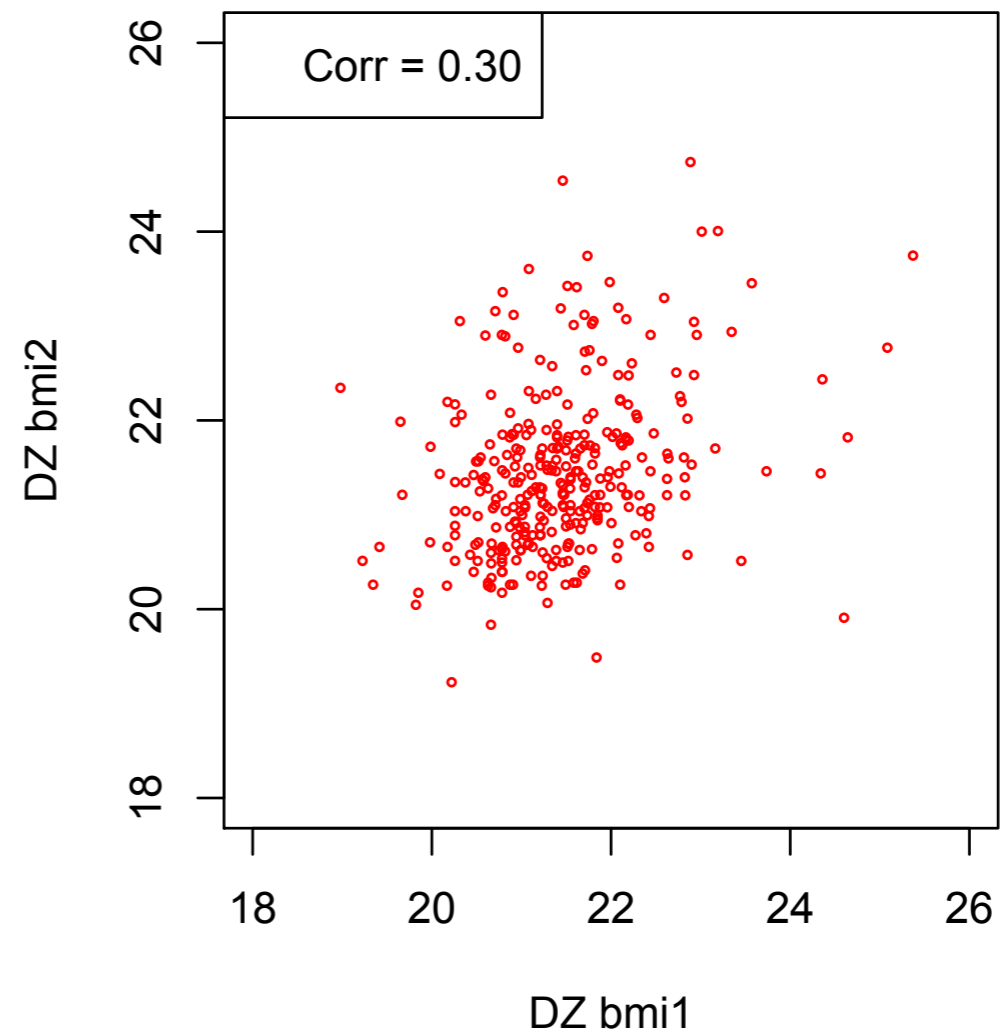
# Example Twin Correlations

---

**MZ BMI**



**DZ BMI**



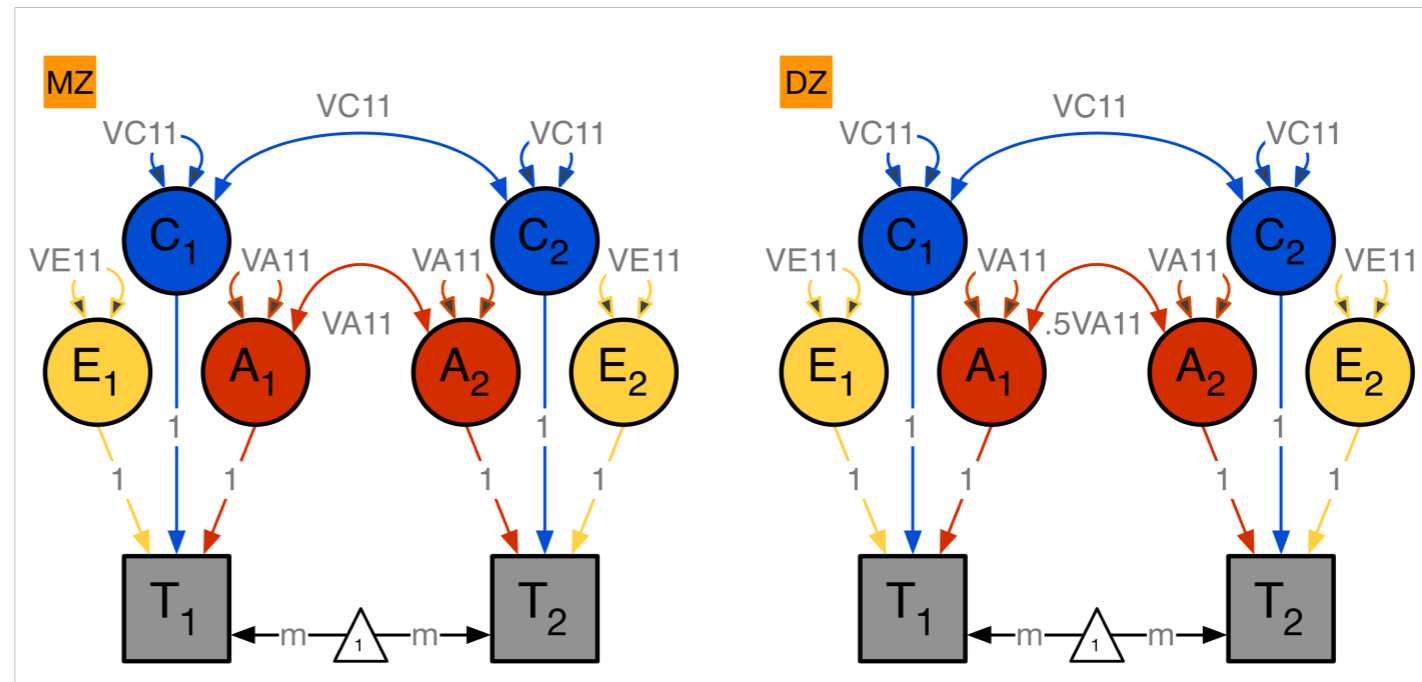
# Roadmap for Univariate Analysis

---

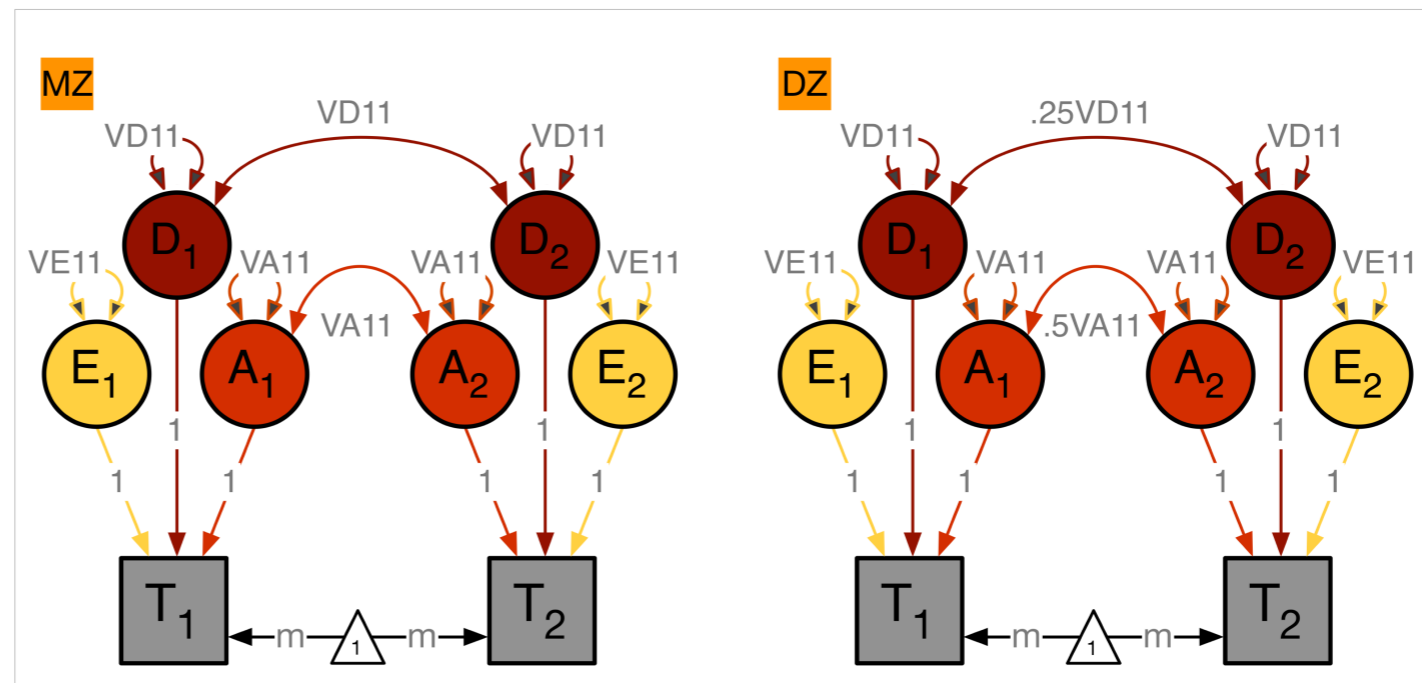
- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
  - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
  - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
  - AE / CE / E Only Models

# Univariate ACE / ADE Model

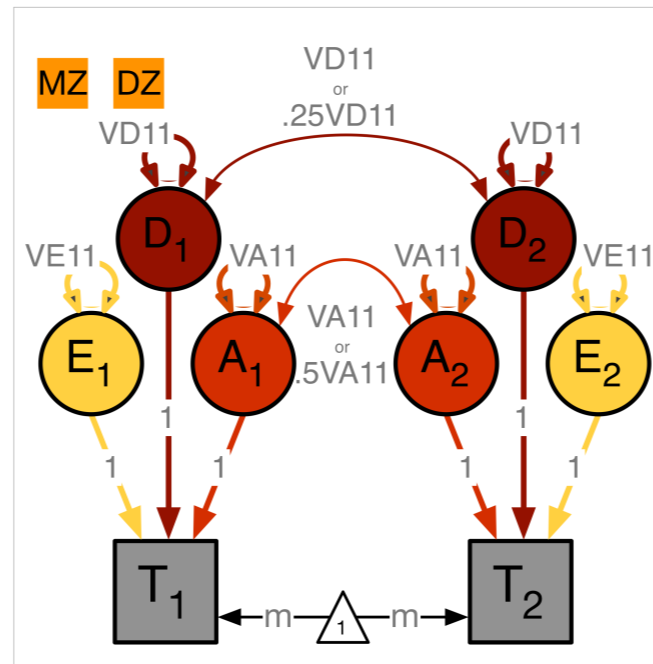
ACE model  
oneACEvc.R



ADE model  
oneADEvc.R



# ADE Deconstructed: *Variance Components*



```
covA      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPa, label="VA11", name="VA" )
```

**VA** 1x1

VA<sub>11</sub>

```
covD      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPa, label="VD11", name="VD" )
```

**VD** 1x1

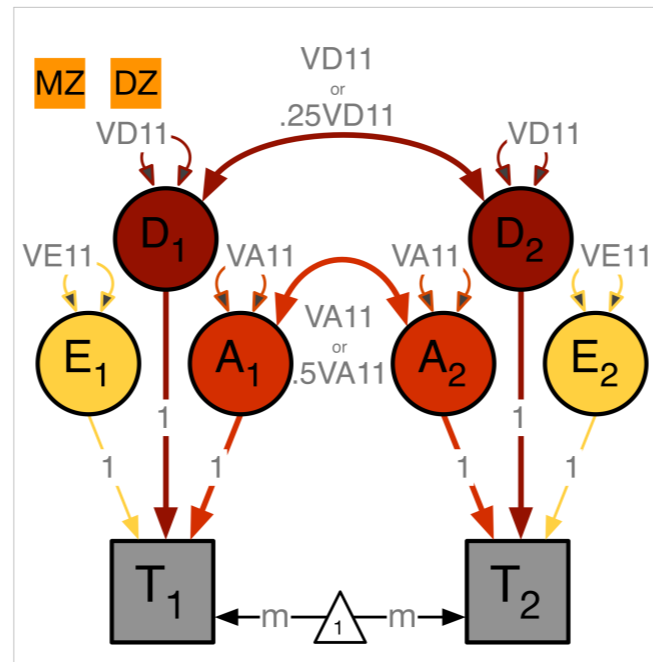
VD<sub>11</sub>

```
covE      <- mxMatrix( type="Symm", nrow=nv, ncol=nv,
free=TRUE, values=svPe, label="VE11", name="VE" )
```

**VE** 1x1

VE<sub>11</sub>

# ADE Deconstructed: *Variances + Covariances*



```
covP      <- mxAlgebra( expression= VA+VD+VE,
  name="V" )
```

V	VA+VD+VE
---	----------

**V** 1x1

```
covMZ     <- mxAlgebra( expression= VA+VD,
  name="cMZ" )
```

cMZ	VA+VD
-----	-------

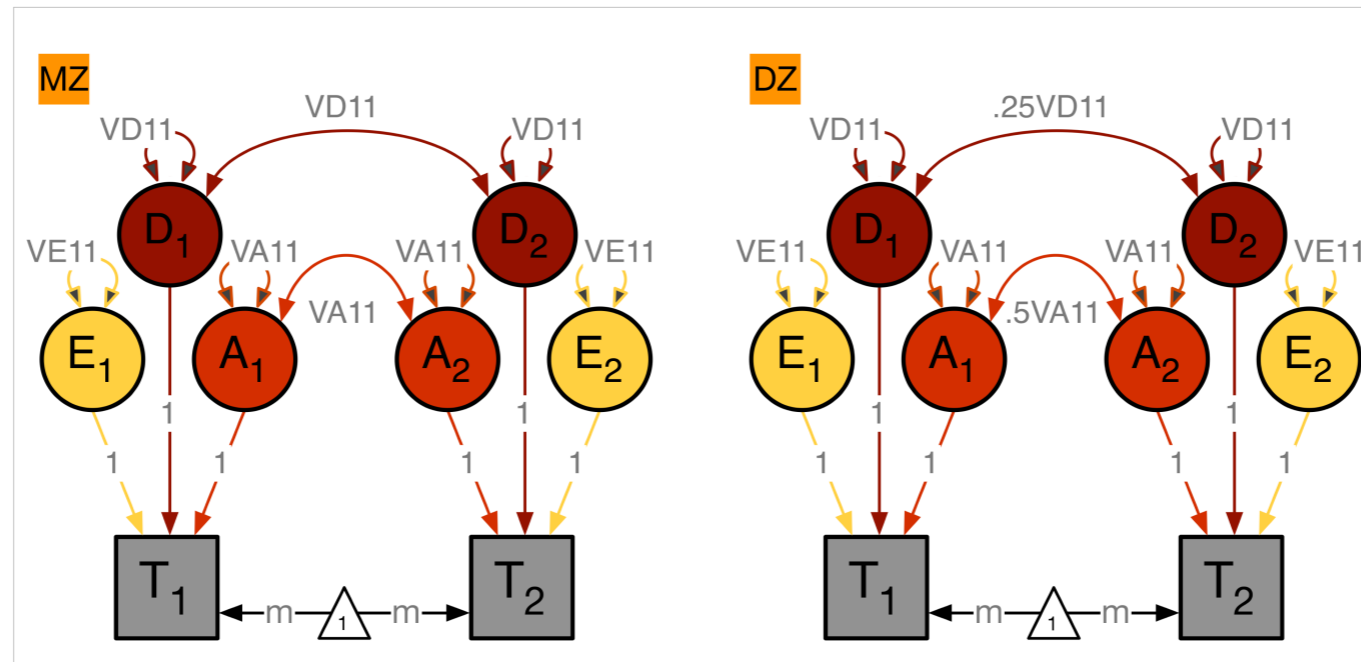
**cMZ** 1x1

```
covDZ     <- mxAlgebra( expression= 0.5xVA+ 0.25xVD,
  name="cDZ" )
```

cDZ	.5VA+.25VD
-----	------------

**cDZ** 1x1

# ADE Deconstructed: Covariance Matrices & Means



```
expCovMZ <- mxAlgebra( expression= rbind(
  cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )
```

V	cMZ
cMZ	V

**expCovMZ** 2x2

```
expCovDZ <- mxAlgebra( expression= rbind(
  cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

V	cDZ
cDZ	V

**expCovDZ** 2x2

```
meanG <- mxMatrix( type="Full", nrow=1, ncol=ntv,
  free=TRUE, values=svMe, labels="x1", name="meanG" )
```

x1	x1
----	----

**meanG** 1x2



# Model Specification

# oneADEvc.R

```
# -----  
# PREPARE MODEL  
  
# Create Algebra for expected Mean Matrices  
meanG      <- mxMatrix( type="Full", nrow=1, ncol=ntv, free=TRUE, values=svMe, labels=labVars("mean",vars),  
                        name="meanG" )  
  
# Create Matrices for Variance Components  
covA       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPa, label="VA11", name="VA" )  
covD       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPd, label="VD11", name="VD" )  
covE       <- mxMatrix( type="Symm", nrow=nv, ncol=nv, free=TRUE, values=svPe, label="VE11", name="VE" )  
  
# Create Algebra for expected Variance/Covariance Matrices in MZ & DZ twins  
covP       <- mxAlgebra( expression= VA+VD+VE, name="V" )  
covMZ      <- mxAlgebra( expression= VA+VD, name="cMZ" )  
covDZ      <- mxAlgebra( expression= 0.5%x%VA+ 0.25%x%VD, name="cDZ" )  
expCovMZ   <- mxAlgebra( expression= rbind( cbind(V, cMZ), cbind(t(cMZ), V)), name="expCovMZ" )  
expCovDZ   <- mxAlgebra( expression= rbind( cbind(V, cDZ), cbind(t(cDZ), V)), name="expCovDZ" )
```

variance components: VA, VD & VE

# Model Specification 2

## oneADEvc.R

```
# Create Data Objects for Multiple Groups
```

```
dataMZ <- mxData( observed=mzData, type="raw" )
dataDZ <- mxData( observed=dzData, type="raw" )
```

```
# Create Expectation Objects for Multiple Groups
```

```
expMZ <- mxExpectationNormal( covariance="expCovMZ", means="meanG", dimnames=selVars )
expDZ <- mxExpectationNormal( covariance="expCovDZ", means="meanG", dimnames=selVars )
funML <- mxFitFunctionML()
```

```
# Create Model Objects for Multiple Groups
```

```
pars <- list(meanG, covA, covD, covE, covP)
modelMZ <- mxModel( pars, covMZ, expCovMZ, dataMZ, expMZ, funML, name="MZ" )
modelDZ <- mxModel( pars, covDZ, expCovDZ, dataDZ, expDZ, funML, name="DZ" )
multi <- mxFitFunctionMultigroup( c("MZ", "DZ") )
```

list of common elements

```
# Create Algebra for Variance Components
```

```
rowVC <- rep('VC',nv)
colVC <- rep(c('VA', 'VD', 'VE', 'SA', 'SD', 'SE'), each=nv)
estVC <- mxAlgebra( expression=cbind(VA,VD,VE, VA/V,VD/V,VE/V), name="VC", dimnames=list(rowVC,colVC))
```

calculate standardized variance components

```
# Create Confidence Interval Objects
```

```
ciADE <- mxCI( "VC[1,1:3]" )
```

list of matrix elements to calculate confidence intervals (CI)

```
# Build Model with Confidence Intervals
```

```
modelADE <- mxModel( "oneADEvc", pars, modelMZ, modelDZ, multi, estVC, ciADE )
```

ADE model

# Run Model

# oneADEvc.R

```
# -----  
# RUN MODEL  
  
# Run ADE Model  
fitADE     <- mxRun( modelADE, intervals=T )  
sumADE     <- summary( fitADE )  
  
# Compare with Saturated Model  
#if saturated model fitted in same session  
mxCompare( fit, fitADE )  
#if saturated model prior to genetic model  
#lrtSAT( fitADE, 4055.9346, 1767 )  
  
# Print Goodness-of-fit Statistics & Parameter Estimates  
fitGofs(fitADE)  
fitEsts(fitADE)  
round(fitADE$VC$result, 4)
```

estimate CI's

function in miFunctions.R to provide -2ll & df of previously fit model

print estimates of variance components

# summary(fitADE)

---

free parameters:

	name	matrix	row	col	Estimate	Std.Error	A
1	meanbmi	meanG	1	1	21.39464927	0.025973494	
2	VA11	VA	1	1	0.32092995	0.150909584	
3	VD11	VD	1	1	0.28942518	0.147886812	
4	VE11	VE	1	1	0.16935016	0.010363413	

confidence intervals:

	lbound	estimate	ubound	note
oneADEvc.VC[1,1]	0.016290870	0.32092995	0.61208265	
oneADEvc.VC[1,2]	0.011924028	0.28942518	0.59556124	
oneADEvc.VC[1,3]	0.150553156	0.16935016	0.19139089	

Model Statistics:

	Parameters	Degrees of Freedom	Fit (-2lnL units)
Model:	4	1773	4063.4496
Saturated:	NA	NA	NA
Independence:	NA	NA	NA

Number of observations/statistics: 920/1777

Information Criteria:

	df	Penalty	Parameters	Penalty	Sample-Size Adjusted
AIC:		517.44962		4071.4496	NA
BIC:		-8036.16490		4090.7471	4078.0436

# miFunctions: fitGofs & fitEsts

---

```
> fitGofs(fitADE)
```

```
Mx:oneADEvc os=1777 ns=920 ep=4 co=0 df=1773 ll=4063.4496 cpu=0.0814 opt=NPSOL ver=2.8.3 stc=0
```

```
>
```

```
> fitEstCis(fitADE)
```

```
meanbmi    VA11    VD11    VE11  
21.3946  0.3209  0.2894  0.1694
```

```
                lbound estimate ubound  
oneADEvc.VC[1,1] 0.0163    0.3209 0.6121  
oneADEvc.VC[1,2] 0.0119    0.2894 0.5956  
oneADEvc.VC[1,3] 0.1506    0.1694 0.1914
```

```
> round(fitADE$VC$result,4)
```

```
      VA    VD    VE    SA    SD    SE  
VC 0.3209 0.2894 0.1694 0.4116 0.3712 0.2172
```

# Goodness-of-Fit Stats & Estimates

---

	ep	-2ll	df	AIC	diff -2ll	diff df	p
Saturated	10	4055.93	1767	521.93			
ADE	4	4063.45	1773	517.45	7.51	6	0.27

	unstandardized variance components			standardized variance components		
	VA	VD	VE	SA	SD	SE
ADE	0.32	0.29	0.17	0.41	0.37	0.22

# Roadmap for Univariate Analysis

---

- Use data to test basic assumptions (equal means & variances for twin 1/twin 2 and MZ/DZ pairs)
  - Saturated Model
- Estimate contributions of genetic/environmental effects on total variance of a phenotype
  - ACE or ADE Models
- Test ACE / ADE submodels to identify and report significant genetic and environmental contributions
  - AE / CE / E Only Models

# Fitting Nested Models

## oneADEvc.R

```
# -----  
# RUN SUBMODELS  
  
# Run AE model  
modelAE <- mxModel( fitADE, name="oneAEc" )  
modelAE <- omxSetParameters( modelAE, labels="VD11", free=FALSE, values=0 )  
fitAE <- mxRun( modelAE, intervals=T )  
fitGofs(fitAE); fitEsts(fitAE)  
  
# Run E model  
modelE <- mxModel( fitAE, name="oneEc" )  
modelE <- omxSetParameters( modelE, labels="VA11", free=FALSE, values=0 )  
fitE <- mxRun( modelE, intervals=T )  
fitGofs(fitE); fitEsts(fitE)  
  
# Print Comparative Fit Statistics  
mxCompare( fitADE, nested <- list(fitAE, fitE) )  
round(rbind(fitADE$VC$result, fitAE$VC$result, fitE$VC$result ),4)
```

dropping parameters



# Nested Models

---

- 'Full' ADE Model

- Nested Models

- AE Model vs ADE Model: test significance of D

- E Model vs AE Model: test significance of A

- E Model vs ADE Model: test significance of both A & D

# Goodness-of-Fit Statistics

---

	ep	-2ll	df	AIC	diff -2ll	diff df	p
ADE	4	4063.45	1773	517.45			
AE	3	4067.66	1774	519.66	4.21	1	0.04
E	2	4591.79	1775	1041.79	528.34	2	0.00



Under the null hypothesis,  
the test is distributed as a chi-square with 1 df

# Estimated Values

---

	unstandardized variance components			standardized variance components		
	VA	VD	VE	SA	SD	SE
ADE	0.32 0.02-0.61	0.29 0.01-0.60	0.17 0.15-0.19	0.41	0.37	0.22
AE	0.62	-	0.17	0.78	-	0.22
E	-	-	0.78	-	-	1.00

# Conclusions

---

- BMI in young OZ females (age 18-30)
  - additive genetic factors: highly significant
  - dominance: borderline significant
  - specific environmental factors: significant
  - shared environmental factors: not

# Thank you

---

- Eaves LJ: Inferring the causes of human variation. *J. R. Stat. Soc. Ser. A* 140, 324–355 (1977).
- Neale MC, Cardon LR: *Methodology for Genetic Studies of Twins and Families* (NATO ASI Series), Dordrecht, The Netherlands: Kluwer Academic Publishers, 496p, 1992.
- Posthuma P, Beem AL, de Geus EJC, van Baal GCM, von Hjelmberg JB, Iachine I, Boomsma DI: Theory and Practice in Quantitative Genetics. *Twin Research* 6:361-376, 2003.
- Eaves LJ, Chen S, Neale M, Maes HH, Silberg J: Questions, Models and Methods in Psychiatric Genetics, in *Psychiatric Genetics* (Review of Psychiatry Vol 24), Kendler KS & Eaves LJ (Eds). Washington, DC: American Psychiatric Publishing, Inc., 2005.
- Maes HH: The ACE model, in *Encyclopedia for Behavioral Statistics* (Wiley Series in Probability and Statistics), Purcell S (Volume Editor). John Wiley & Sons, Inc., 2005.
- Neale MC: Biometrical Models in Behavioral Genetics, in *Handbook of Behavior Genetics*, Yong-Kyu, K. (Volume Editor). Springer, 2009.
- Evans DM, Frazer IH, Martin NG: Genetic and environmental causes of variation in basal levels of blood cells, *Twin Research* 2: 250-257, 1999.



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## Genetic and environmental causes of variation in basal levels of blood cells

David M Evans<sup>1</sup>, Ian H Frazer<sup>2</sup> and Nicholas G Martin<sup>1</sup>

# Calculate Correlations

---

- add calculations to openMx scripts

- as part of script (calculated with every iteration)

```
# Create Algebra for Maximum Likelihood Estimates of Twin Correlations
```

```
matI      <- mxMatrix( type="Iden", nrow=ntv, ncol=ntv, name="I" )
```

```
corMZ     <- mxAlgebra( solve(sqrt(I*covMZ)) %&% covMZ, name="corMZ" )
```

```
corDZ     <- mxAlgebra( solve(sqrt(I*covDZ)) %&% covDZ, name="corDZ" )
```

→ formula to calculate correlations

- after script has been run

```
# Create Algebra for Maximum Likelihood Estimates of Twin Correlations
```

```
I         <- diag(1, 2, 2)
```

```
corMZ     <- mxEval( solve(sqrt(I*covMZ)) %&% covMZ, fitSAT$MZ )
```

```
corDZ     <- mxEval( solve(sqrt(I*covDZ)) %&% covDZ, fitSAT$DZ )
```