Denotes He-man

Denotes practical

Power and p-values

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Statisticians Found One Thing They Can Agree On: It's Time To Stop Misusing P-Values

By CHRISTIE ASCHWANDEN

p-values are in the press

In February, 2014, George Cobb, Professor Emeritus of Mathematics and Statistics at Mount Holyoke College, posed these questions to an ASA discussion forum:

> Q: Why do so many colleges and grad schools teach $p = .05$?
>
> A: Because that's still what the scientific community and journal editors use.
>
> Q: Why do so many people still use $p = 0.05$?
>
> A: Because that's what they were taught in college or grad school.

What we've been teaching

- A way to ask if the data are consistent with a null model

What exactly is a p-value?

- The baseline model for comparison, usually no effect [e.g. no heritability]

What's a null model?

- Distrust of his aunt's claims of being able to discriminate between milk in first or tea in first

Whose fault is it anyway?

alternative vs null

some effect no effect

Hypothesis testing

Statistics

Truth

	Reject H_0	Fail to reject H_0
H_0 is true	α	$1-\alpha$
H_a is true	$1-\beta$	β

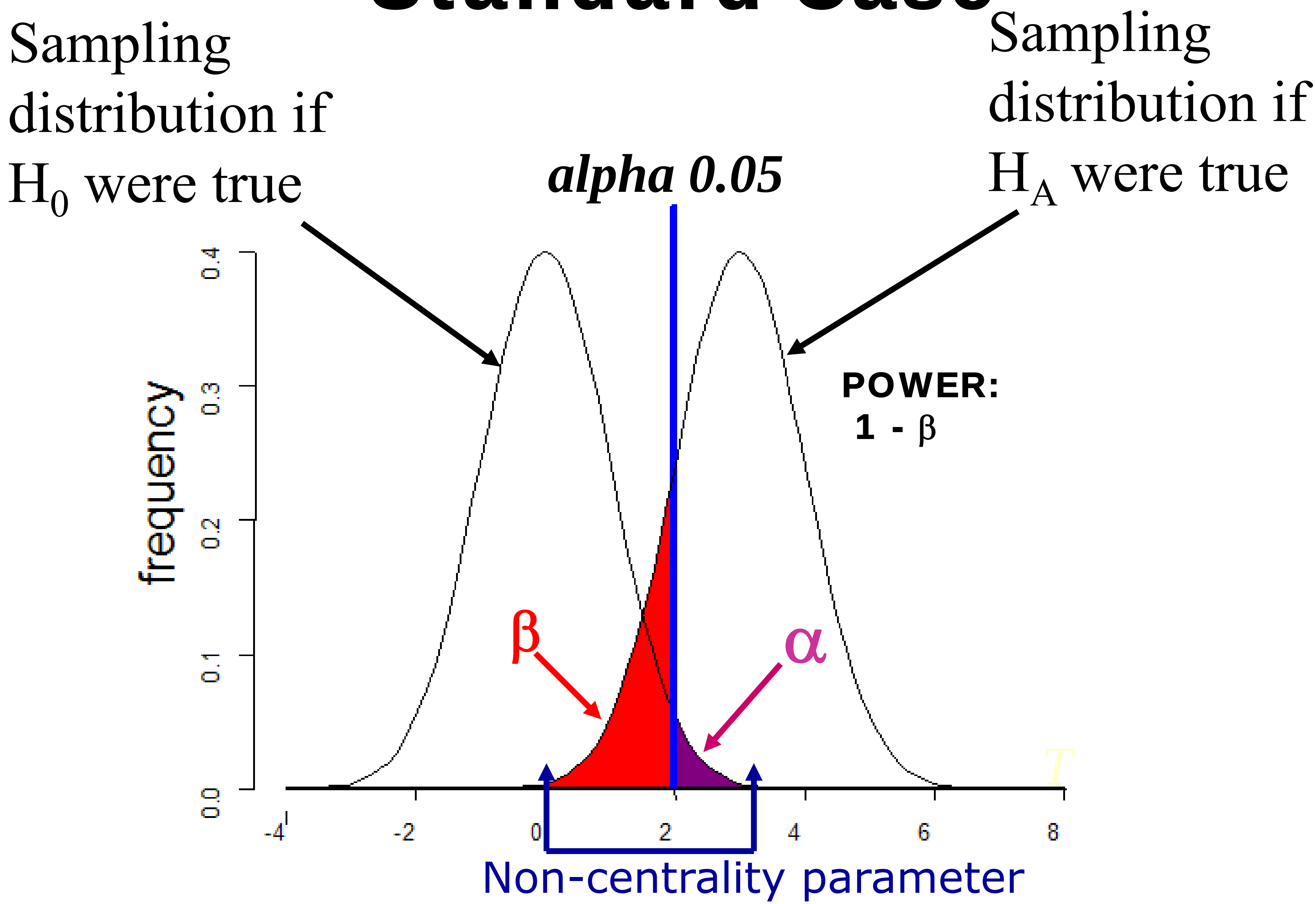
α=type 1 error rate

β=type 2 error rate

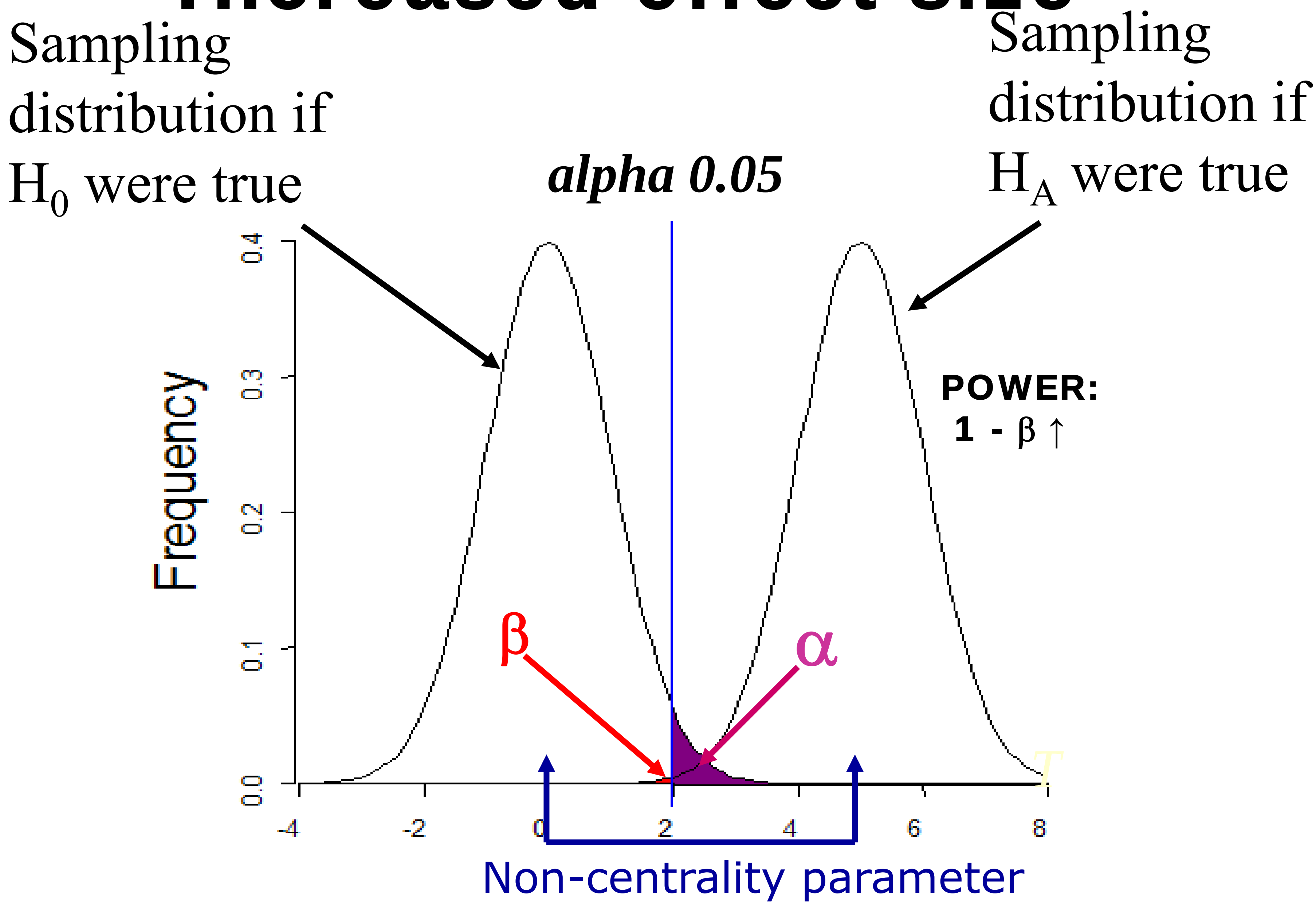
$1-\beta$=statistical power

Possible scenarios

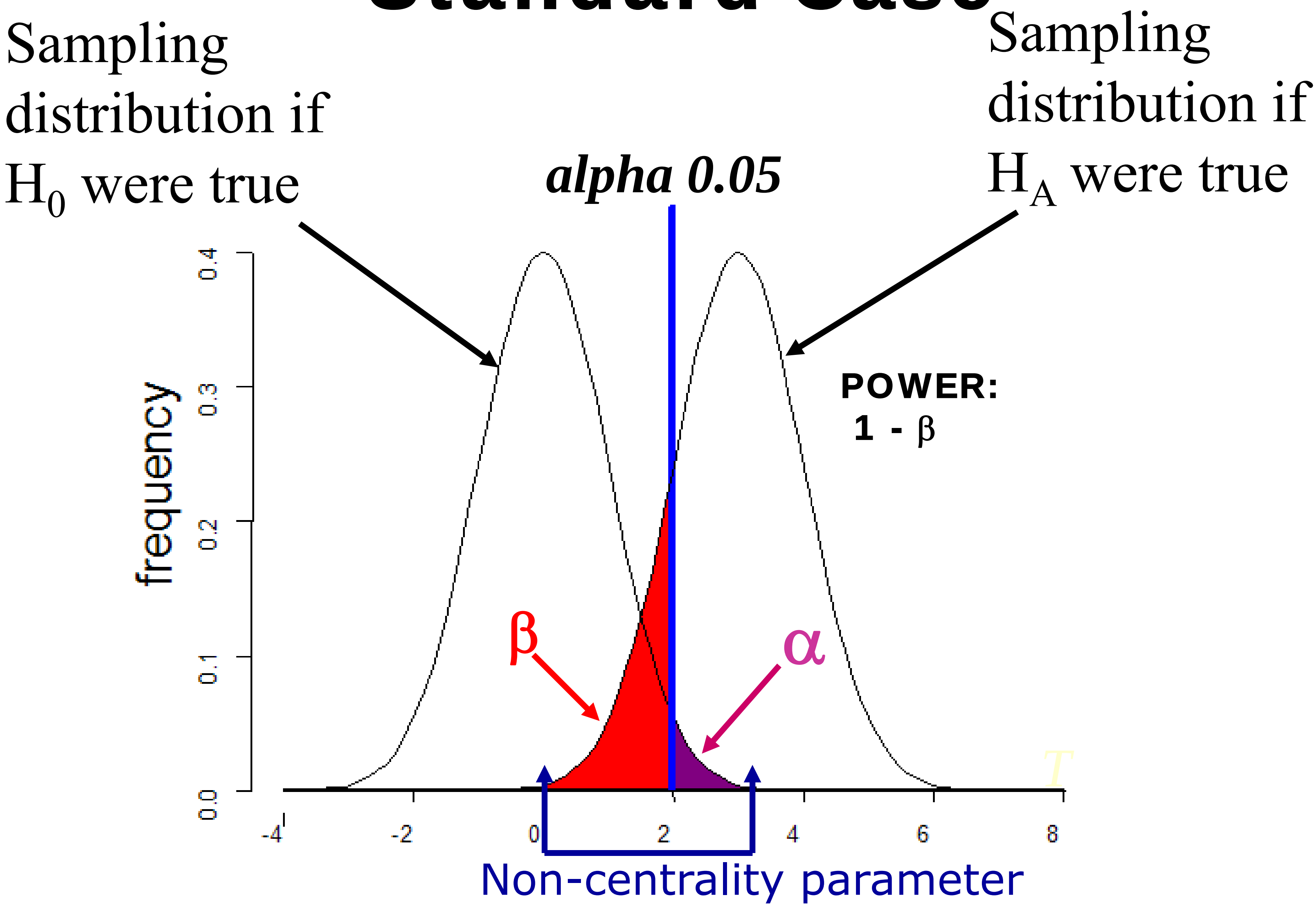
Standard Case



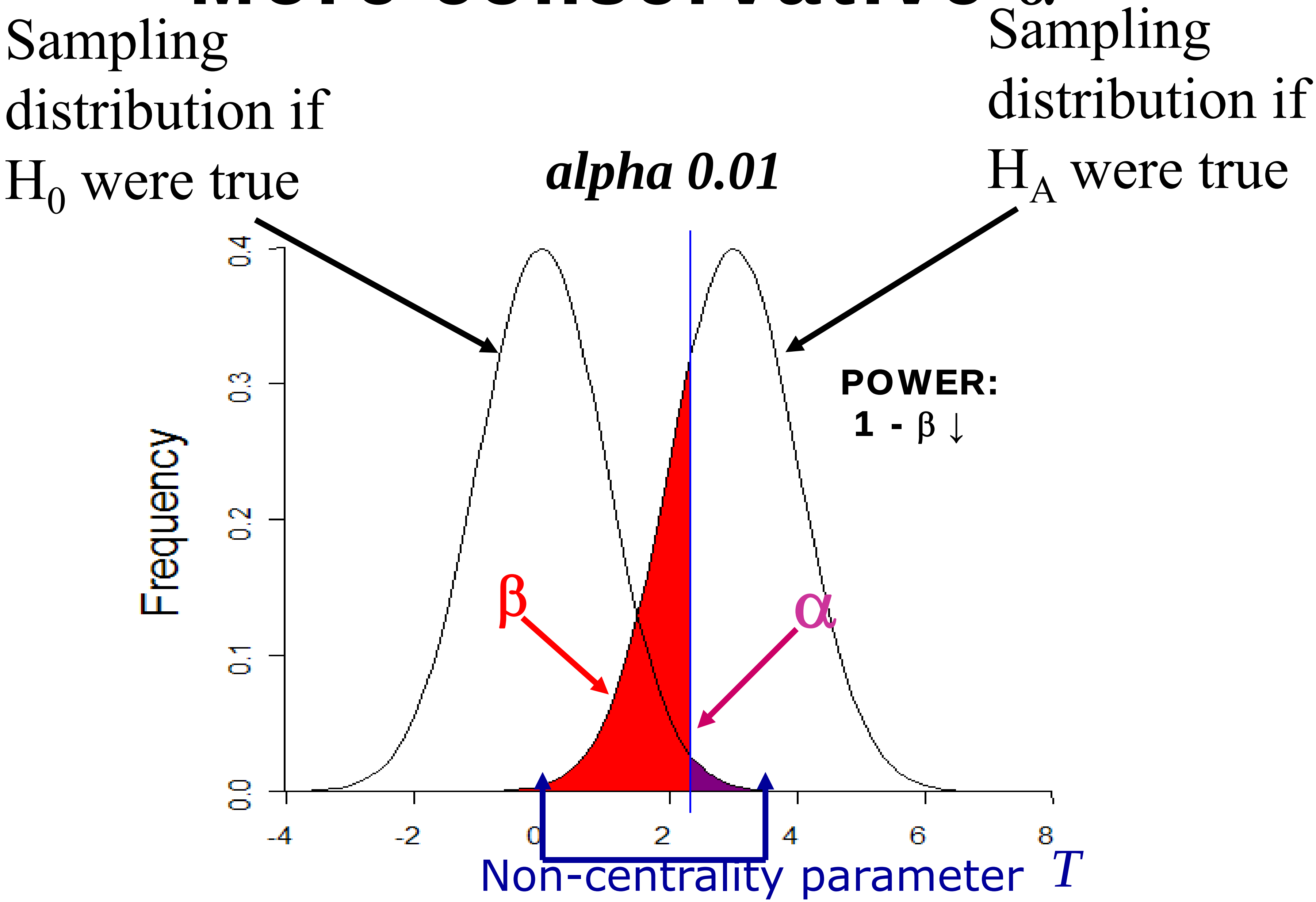
Increased effect size



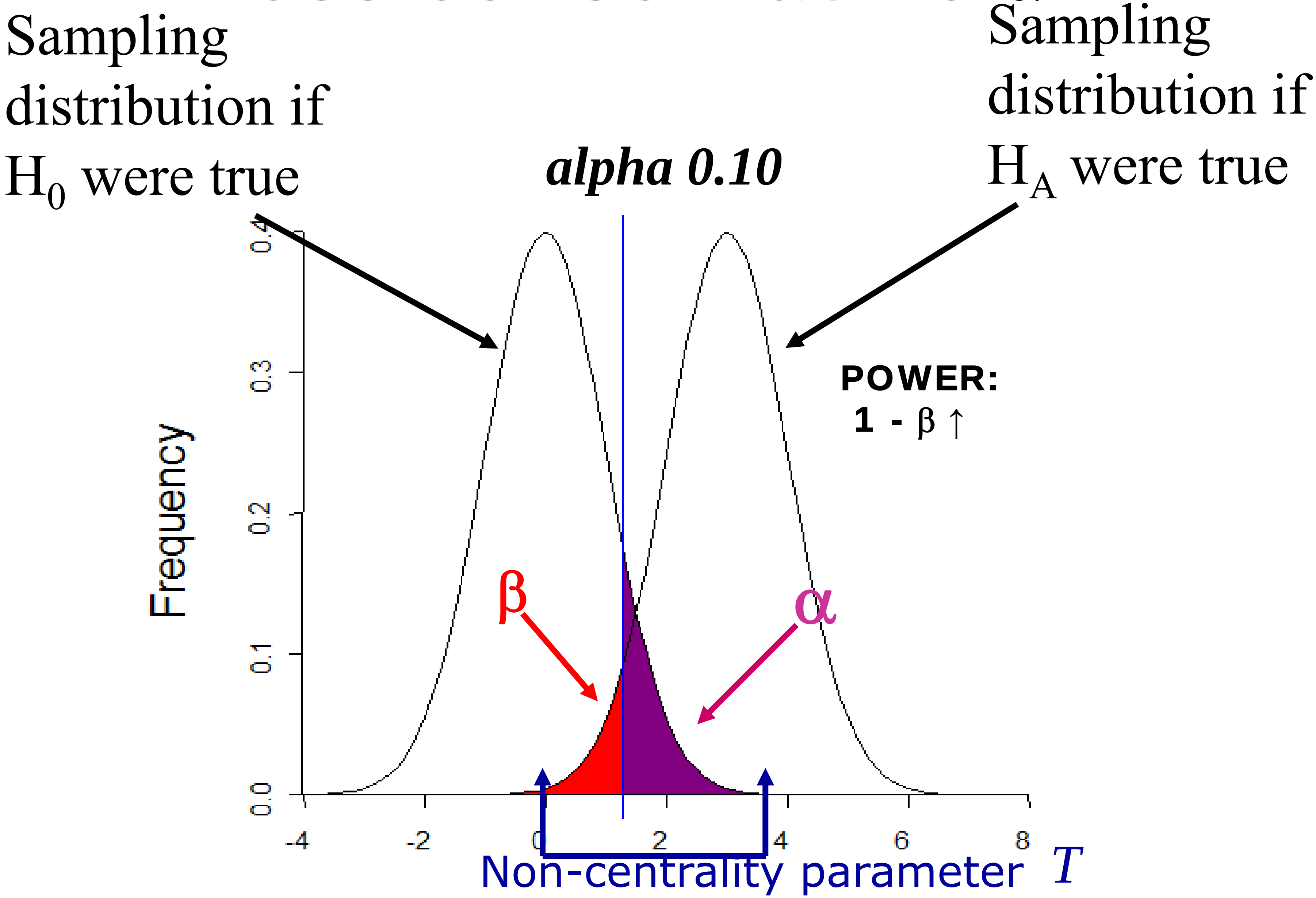
Standard Case



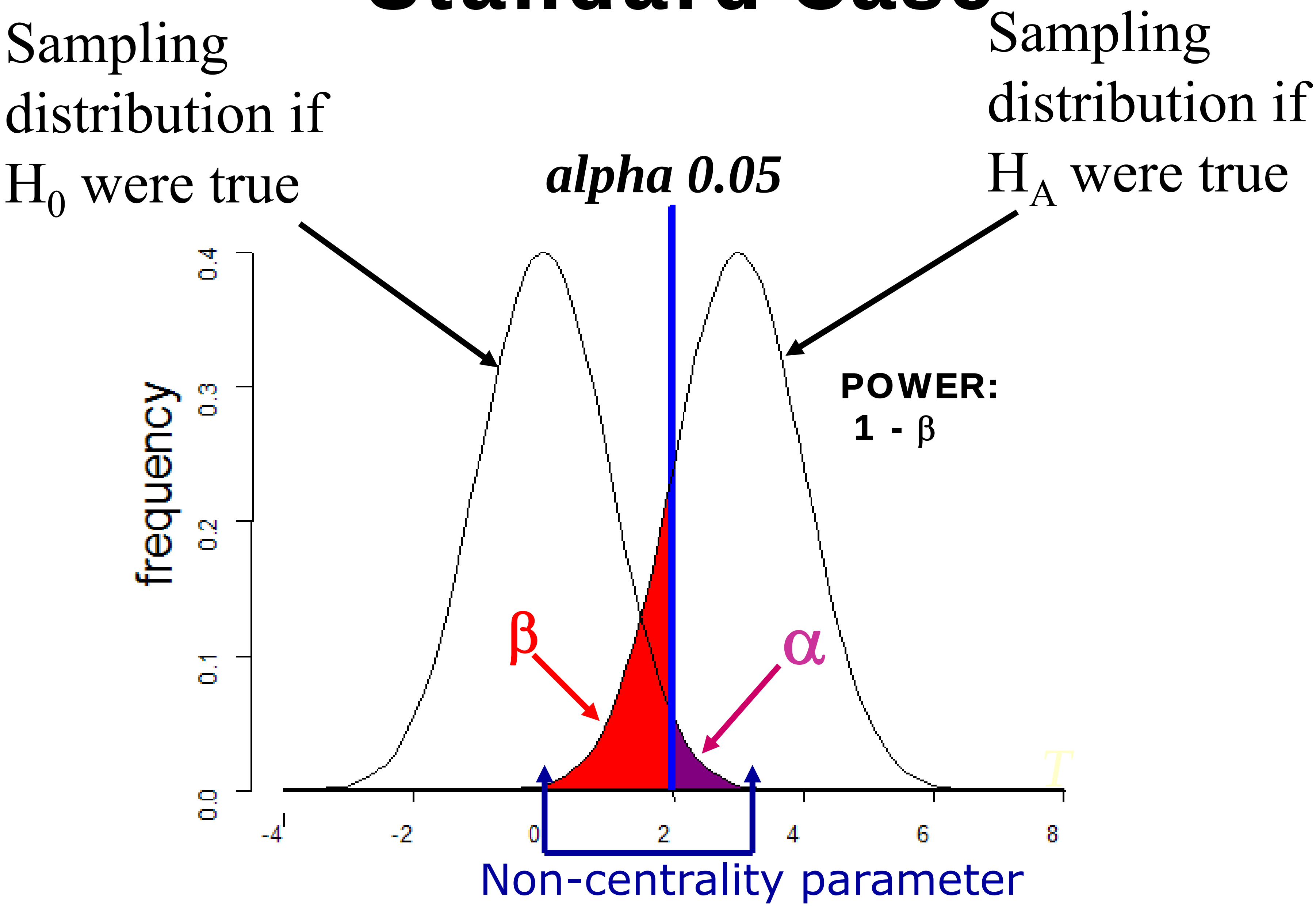
More conservative α



Less conservative α



Standard Case

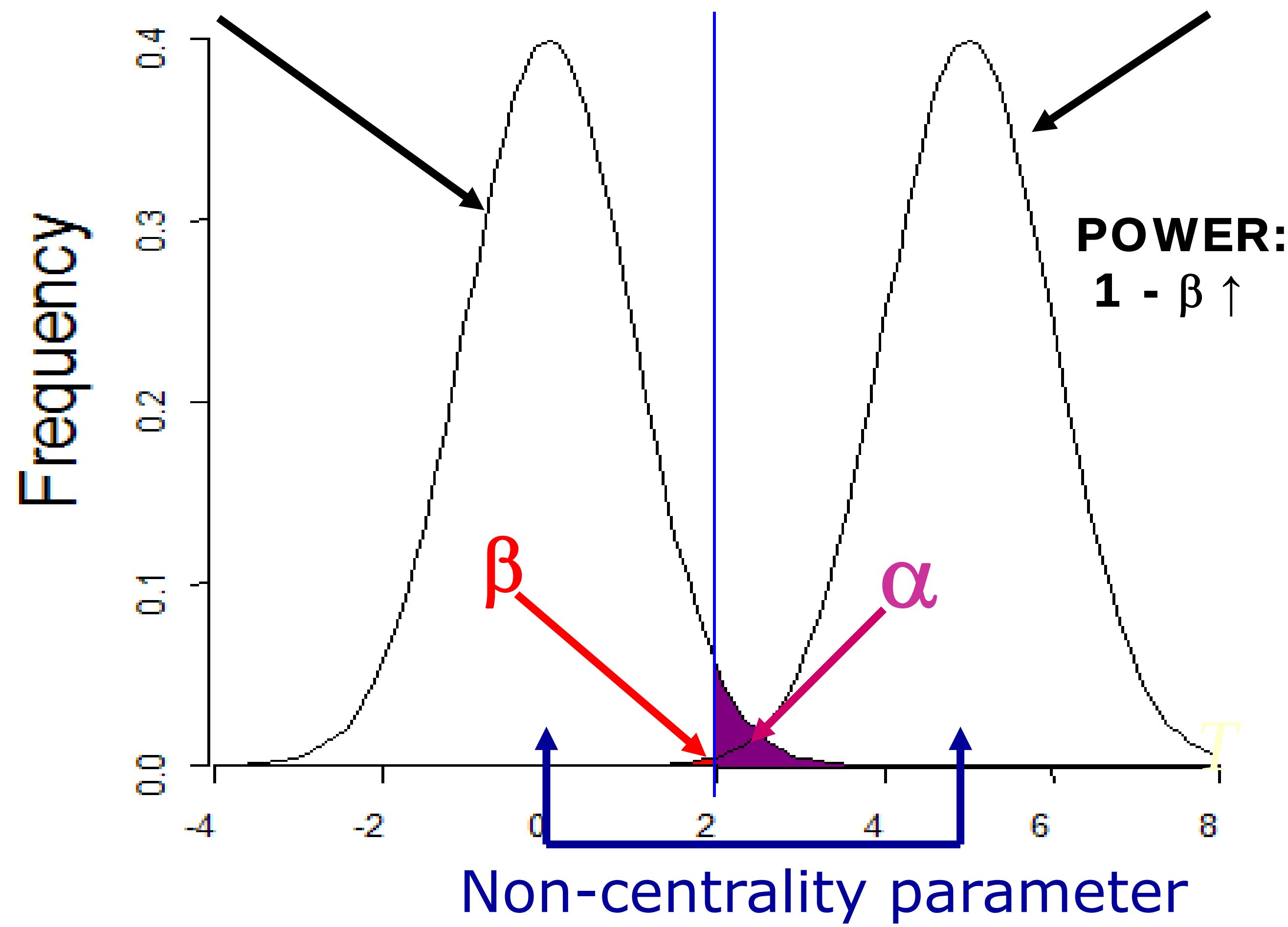


Increased sample size

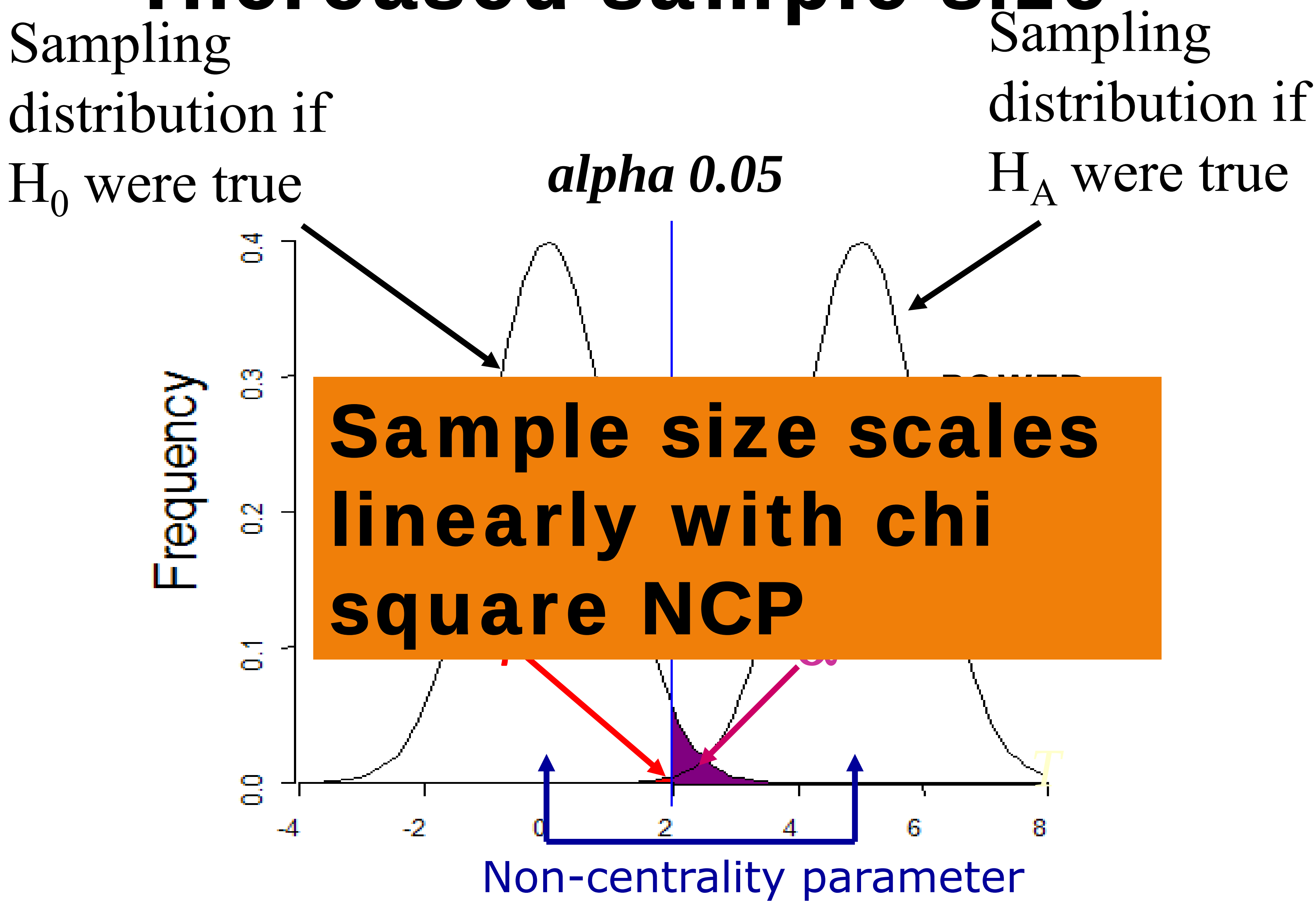
Sampling distribution if H_0 were true

Sampling distribution if H_A were true

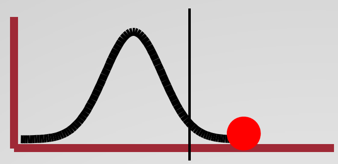
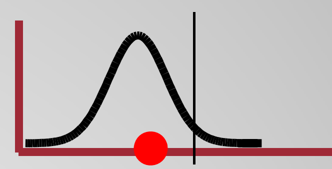
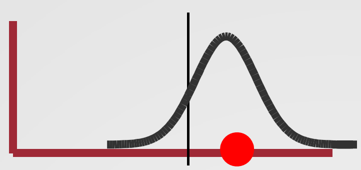
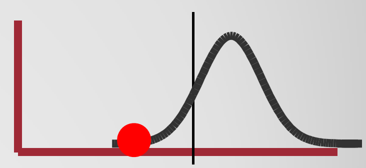
alpha 0.05



Increased sample size



Statistical Analysis

Truth	Rejection of H_0	Non-rejection of H_0
H_0 true	Type I error at rate α 	Nonsignificant result $(1-\alpha)$ 
H_A true	Significant result $(1-\beta)$ 	Type II error at rate β 

- Definitions of power
- The probability that the test will reject the null hypothesis if the alternative hypothesis is true

- The chance the your statistical test will yield a significant result when the effect you are testing exists

What is power?

- We are going to simulate a normal distribution using R

- We can do this with a single line of code, but let’s break it up

Practical 1

- R has functions for many distributions
- Normal, χ^2, gamma, beta (others)
- Let's start by looking at the random normal function: rnorm()

Simulation functions

R Help

Normal {stats} R Documentation

The Normal Distribution

Description

Density, distribution function, quantile function and random generation for the normal distribution with mean equal to `mean` and standard deviation equal to `sd`.

Usage

```
dnorm(x, mean = 0, sd = 1, log = FALSE)
pnorm(q, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
qnorm(p, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
rnorm(n, mean = 0, sd = 1)
```

Arguments

`x,q`	vector of quantiles.
`p`	vector of probabilities.
`n`	number of observations. If `length(n) > 1`, the length is taken to be the number required.
`mean`	vector of means.
`sd`	vector of standard deviations.

In R: ?rnorm

rnorm Documentation

rnorm syntax

- rnorm(n, mean = 0, sd = 1)

Function name

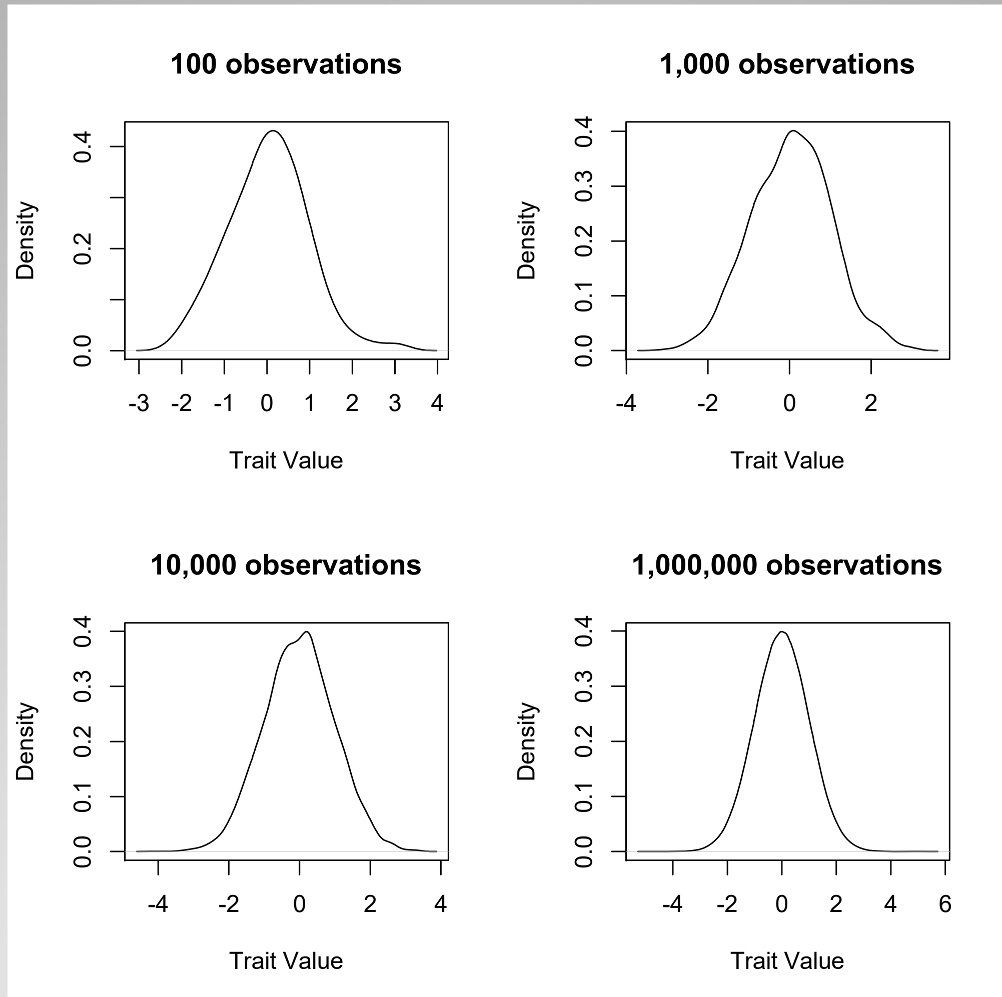
Number of observations to simulate

Mean of distribution with default value

Standard deviation of distribution with default value

- This script will plot 4 samples from the normal distribution
- Look for changes in shape
- Thoughts?

R script: Norm_dist_sim.R



One I made earlier

- Sampling variance
  - We saw that the 'normal' distribution from 100 observations looks stranger than for 1,000,000 observations
- Where else may this sampling variance happen?
- How certain are we that we have created a good distribution?

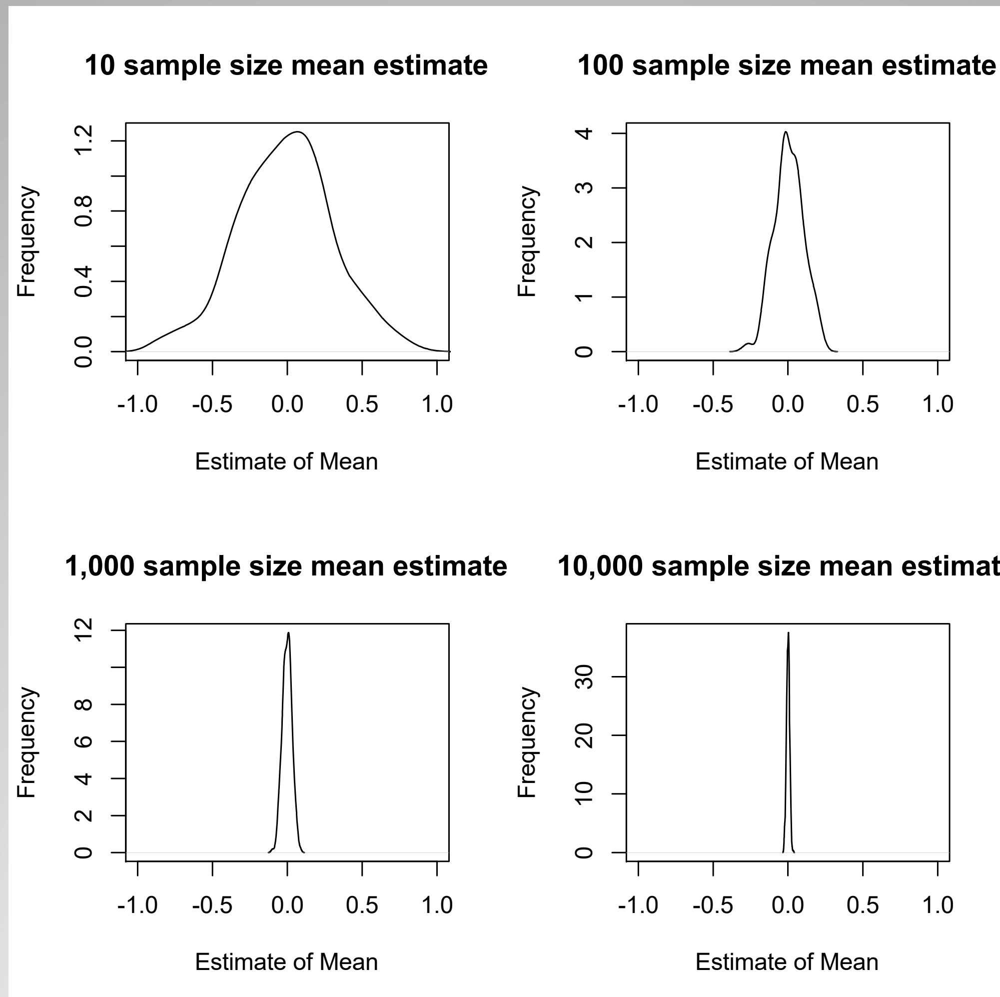
Concepts

- Rather than just simulating the normal distribution, let's simulate what our estimate of a mean looks like as a function of sample size
- We will run the R script mean_estimate_sim.R

Mean estimation

- This script will plot 4 samples from the normal distribution
- Look for changes in shape
- Thoughts?

R script: mean_estimate_sim.R



One I made earlier

- We see an inverse relationship between sample size and the variance of the estimate
- This variability in the estimate can be calculated from theory
- $SE_x = s/\sqrt{n}$
- SE_x is the standard error, s is the sample standard deviation, and n is the sample size

Standard Error

The sampling variability in my estimate affects my ability to declare a parameter as significant (or significantly different)

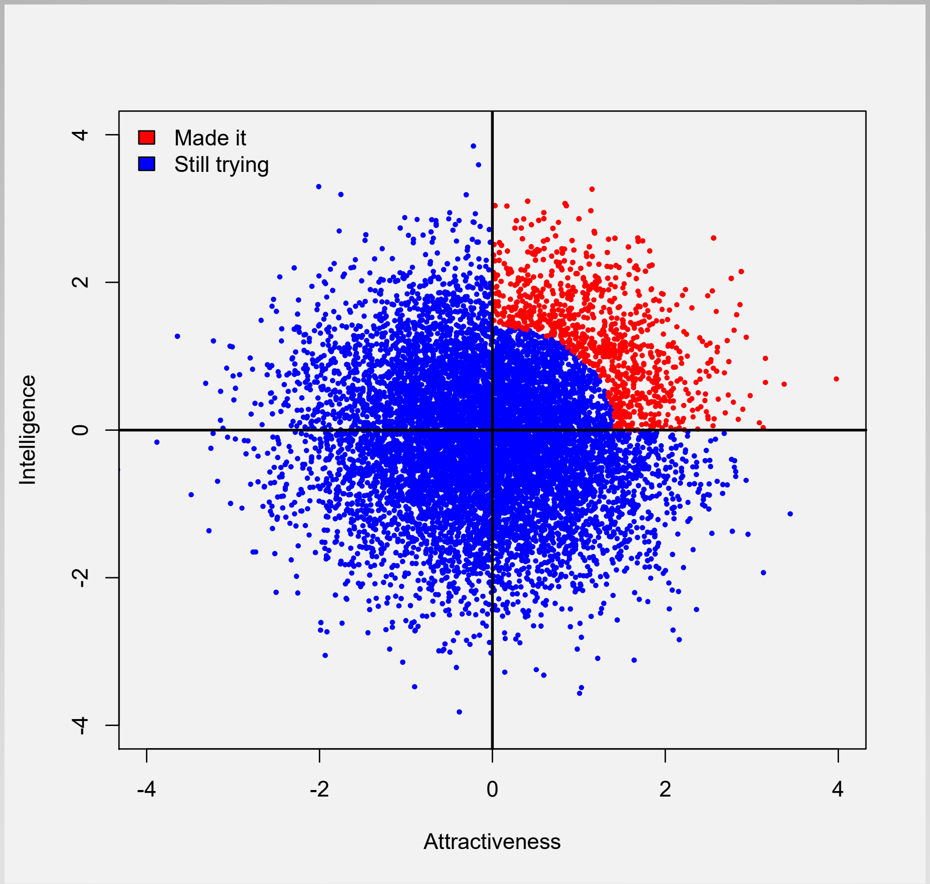
Key Concept 1

Power definition again

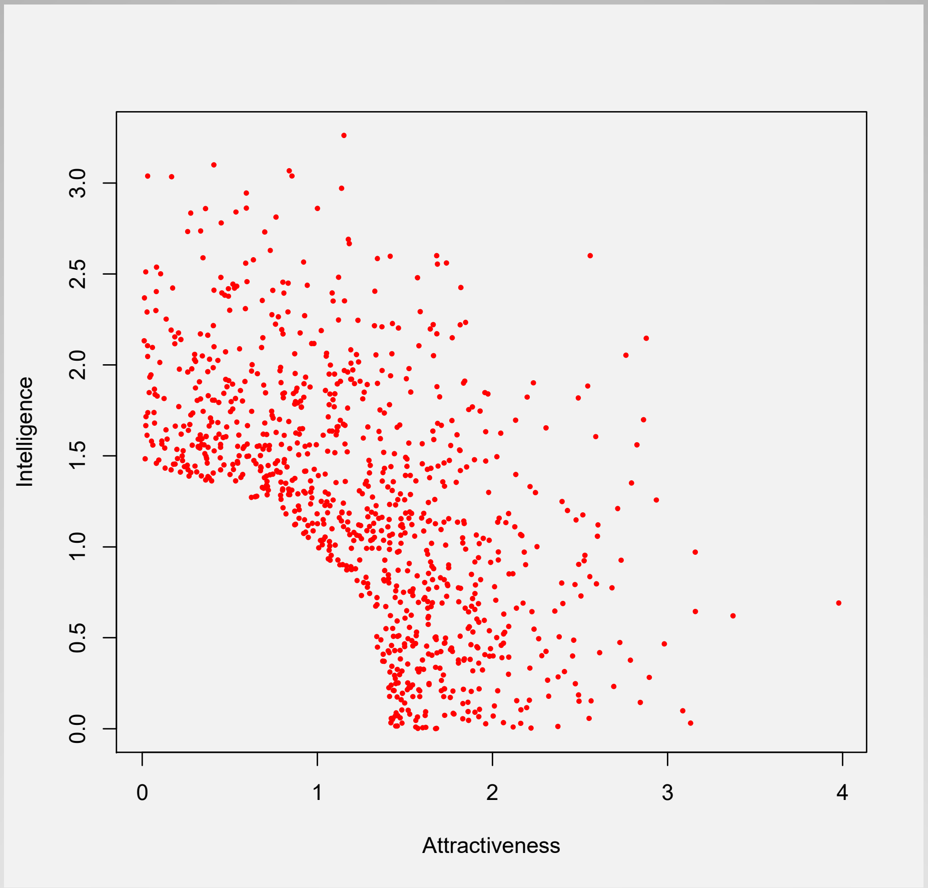
The probability that the test will reject the null hypothesis if the alternative hypothesis is true

Ascertainment

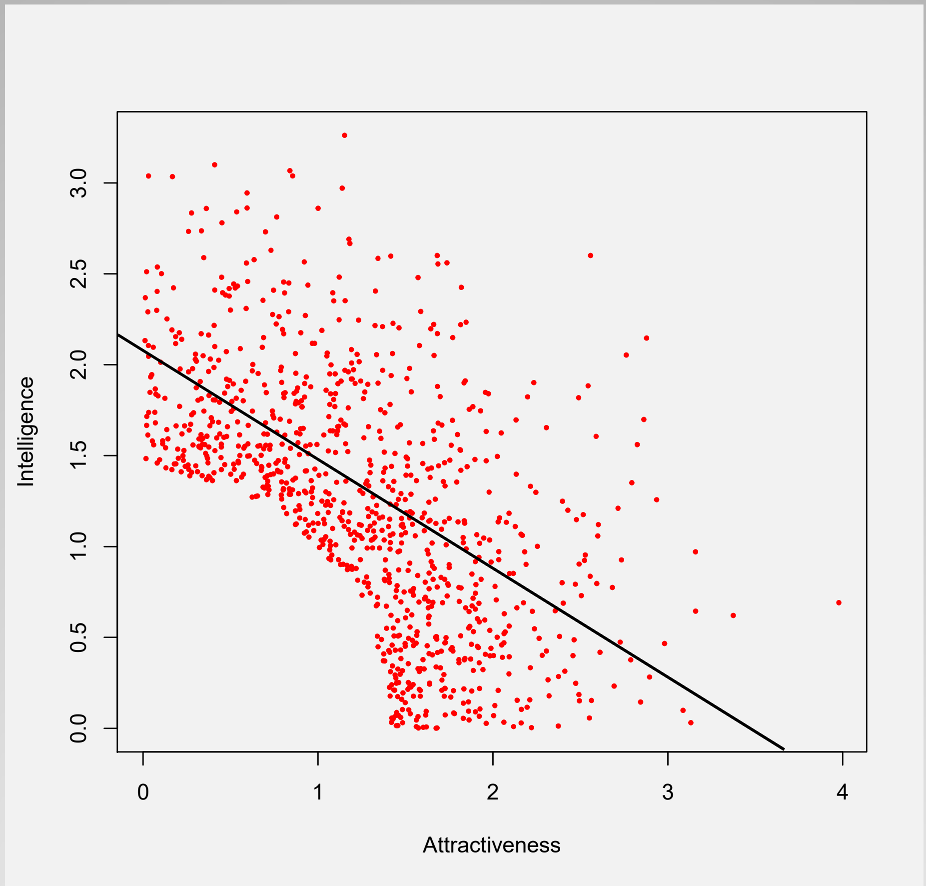
Why being picky can be good and bad



Bivariate plot for actors in Hollywood



Bivariate plot for actors who "made it" in Hollywood



P<2e-16

Bivariate plot for actors who "made it" in Hollywood

- Again – you’re meant to say something
- I’m waiting…

What happened?

- Bias in your parameter estimates
  - Bias is a difference between the “true value” and the estimated value
- Can apply across a range of scenarios
  - Bias estimates of means, variances, covariances, betas etc.

Ascertainment

- For testing means, ascertainment increases power
- For characterizing variance:covariance structure, ascertainment can lead to bias

When might we want to ascertain?

- For testing means, ascertainment increases power
- For characterizing variance:covariance structure, ascertainment can lead to bias

Mapping Mendelian Factors Underlying Quantitative Traits Using RFLP Linkage Maps

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When might we want to ascertain?

- Power calculations using NCP
- We create the model
  - specifying our effect sizes
- We then simulate data
  - empirical = T means that the simulated data matches the specifications [within some error]
- The chi square can then be used to generate power

Practical!