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LD Score – new methods for heritability

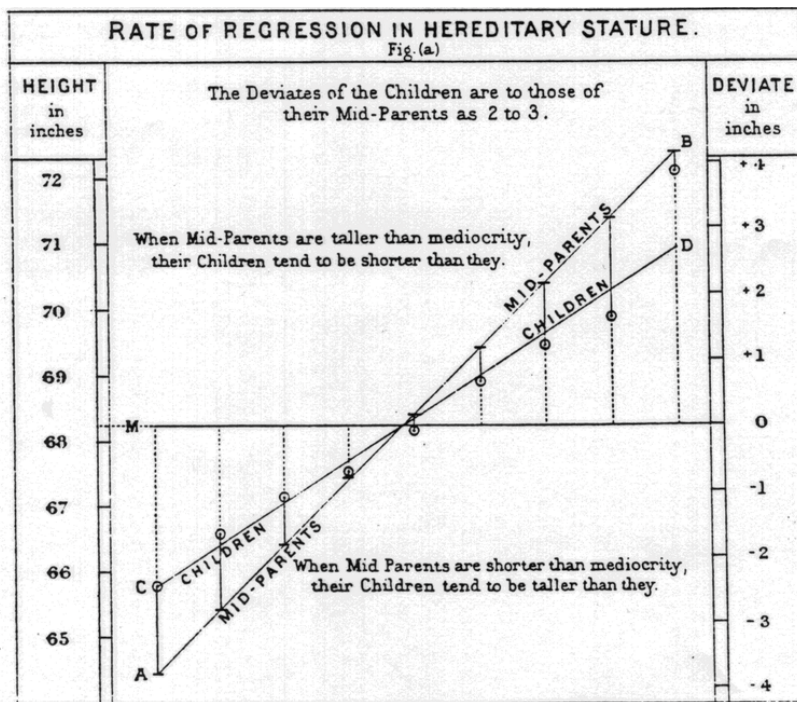
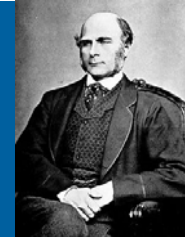
Benjamin Neale, Ph.D.

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Stanley Center for Psychiatric Research & Program in Medical and Population Genetics, Broad Institute

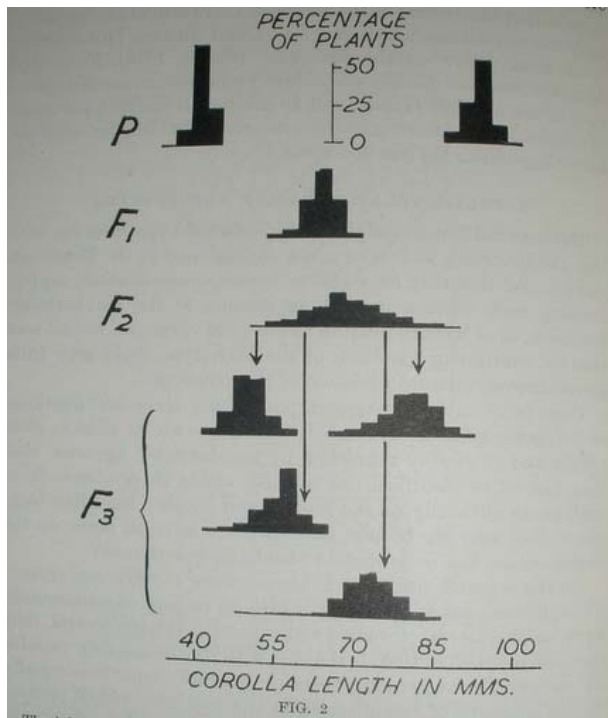


Galton



- Children resemble parents
- Origin of term “regression”

East 1915: Inheritance of corolla length in *Nicotiana Longiflora*



- Breeding experiments in plants clearly demonstrate polygenic inheritance

Neo-Darwinist reconciliation

RA Fisher



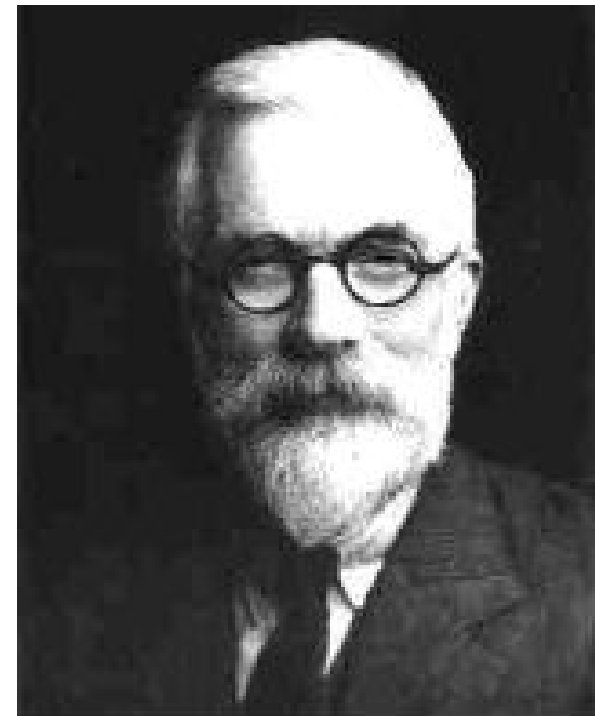
XV.—**The Correlation between Relatives on the Supposition of Mendelian Inheritance.** By **R. A. Fisher**, B.A. *Communicated by Professor J. ARTHUR THOMSON.* (With Four Figures in Text.)

(MS. received June 15, 1918. Read July 8, 1918. Issued separately October 1, 1918.)

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Several attempts have already been made to interpret the well-established results of biometry in accordance with the Mendelian scheme of inheritance. It is here attempted to ascertain the biometrical properties of a population of a more general type than has hitherto been examined, inheritance in which follows this



LD Score regression



With thanks



Brendan Bulik-Sullivan



Hilary Finucane



Po-Ru Loh



Mark Daly



Alkes Price

How does LD shape association?



LD Score regression distinguishes confounding from polygenicity in genome-wide association studies

Brendan K Bulik-Sullivan, Po-Ru Loh, Hilary K Finucane, Stephan Ripke, Jian Yang, Schizophrenia Working Group of the Psychiatric Genomics Consortium, Nick Patterson, Mark J Daly, Alkes L Price & Benjamin M Neale

Affiliations | Contributions | Corresponding author

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How does LD shape association?



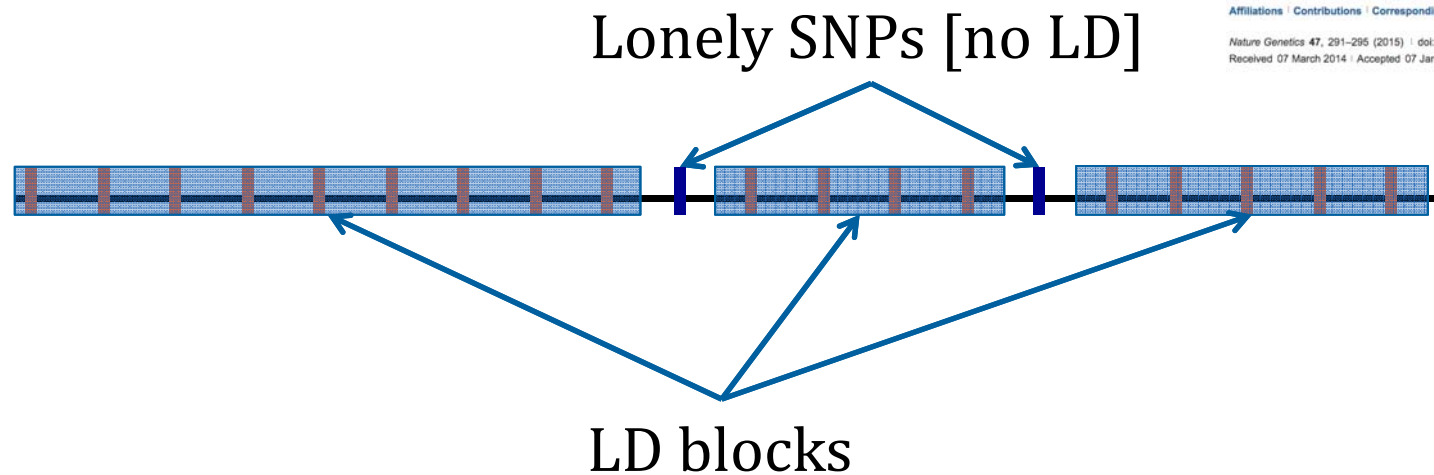
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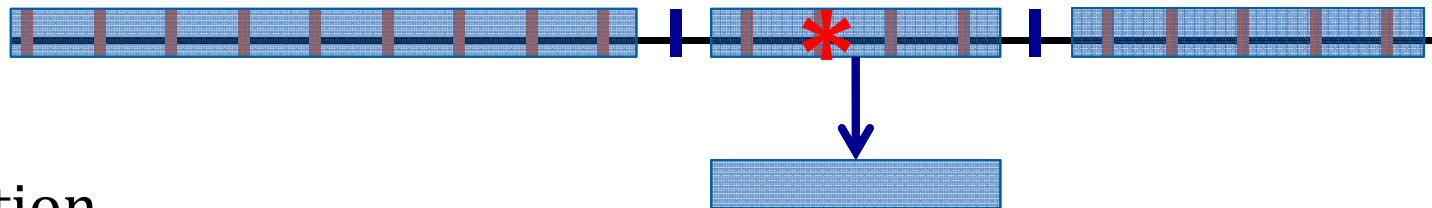
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- LD blocks
- * Causal variants

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Association

All markers correlated with a causal variant show association

How does LD shape association?



- Lonely SNPs [no LD]
- LD blocks
- Causal variants

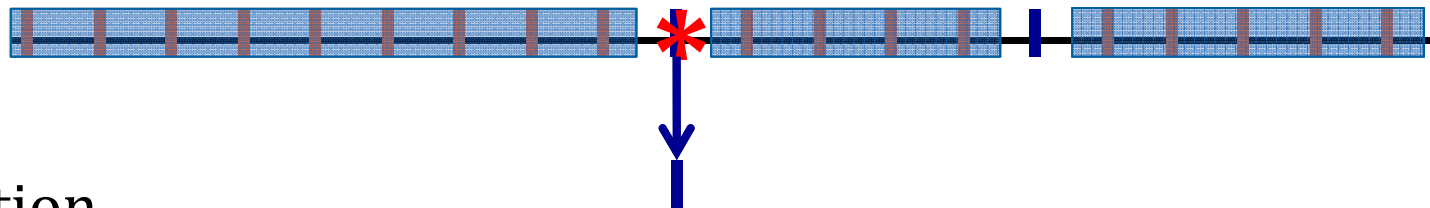
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Association

Lonely SNPs only show association if they are causal

What happens under polygenicity?



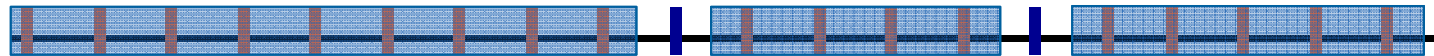
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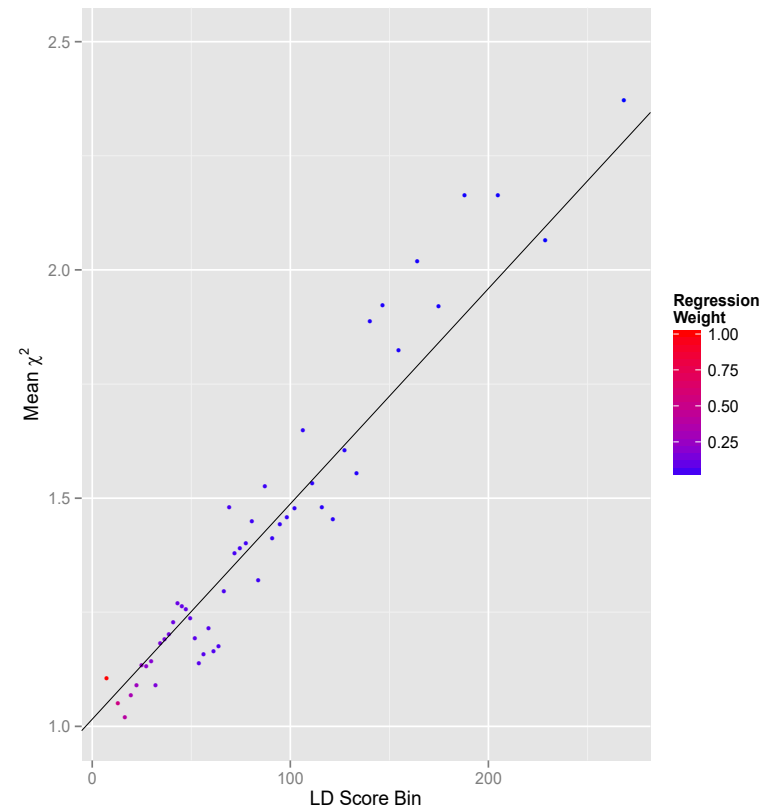
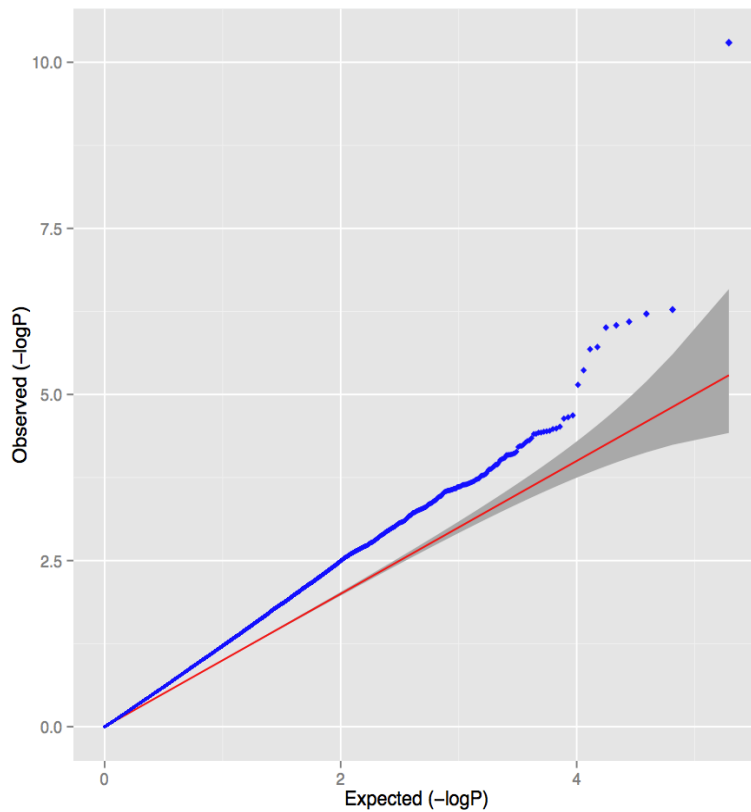


Assuming a uniform prior, we see SNPs with more LD friends showing more association

The more you tag, the more likely you are to tag a causal variant

Simulated polygenic architecture

Lambda = 1.30 LD score intercept = 1.02



What happens under stratification?



- Lonely SNPs [no LD]
- LD blocks
- * Causal variants

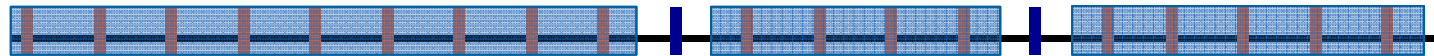
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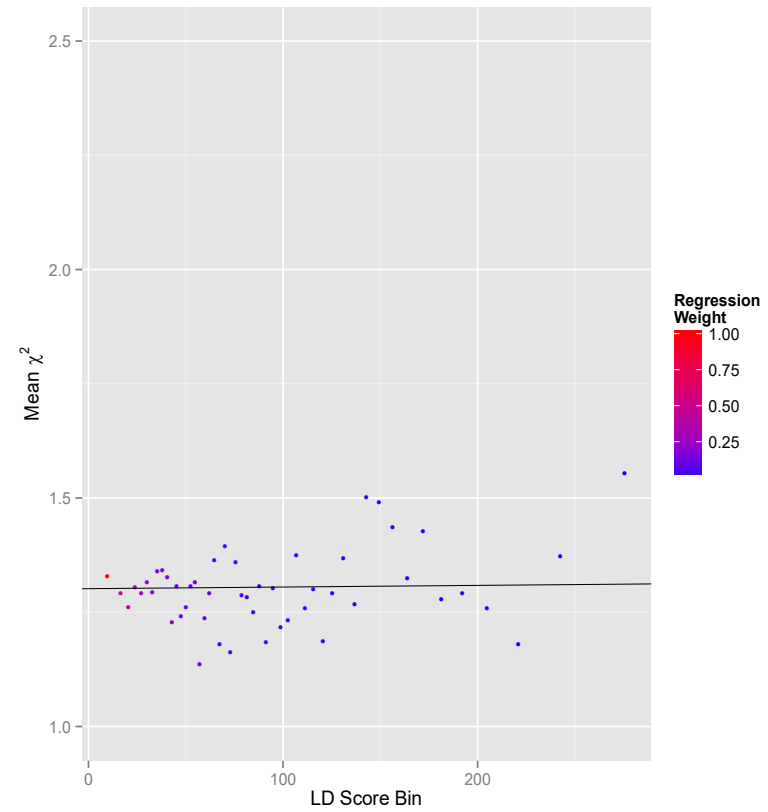
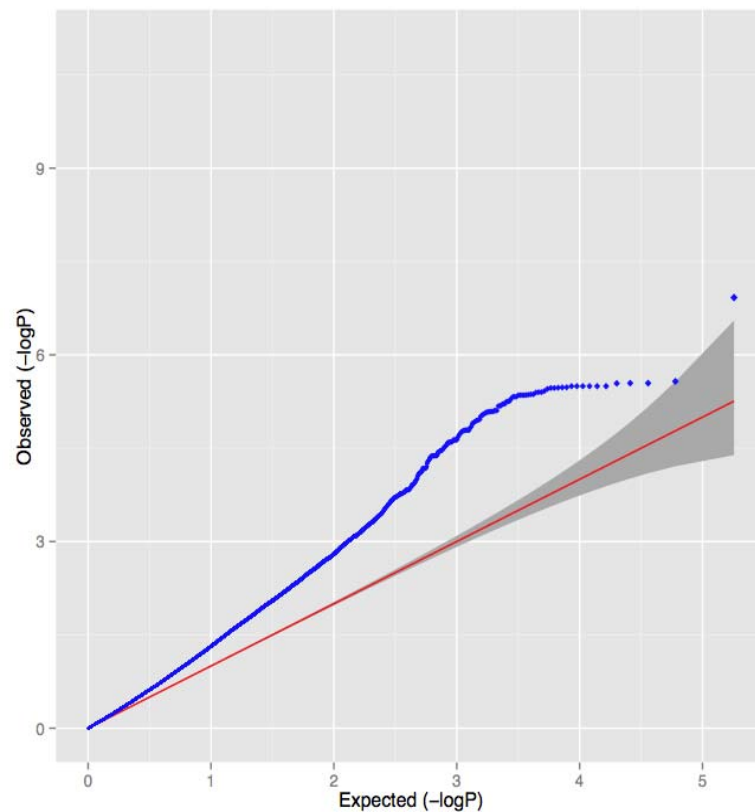
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Under pure drift we expect LD to have no relationship to differences in allele frequencies between populations

UK controls versus Sweden controls

Lambda = 1.30 LD score intercept = 1.32



PGC Schizophrenia

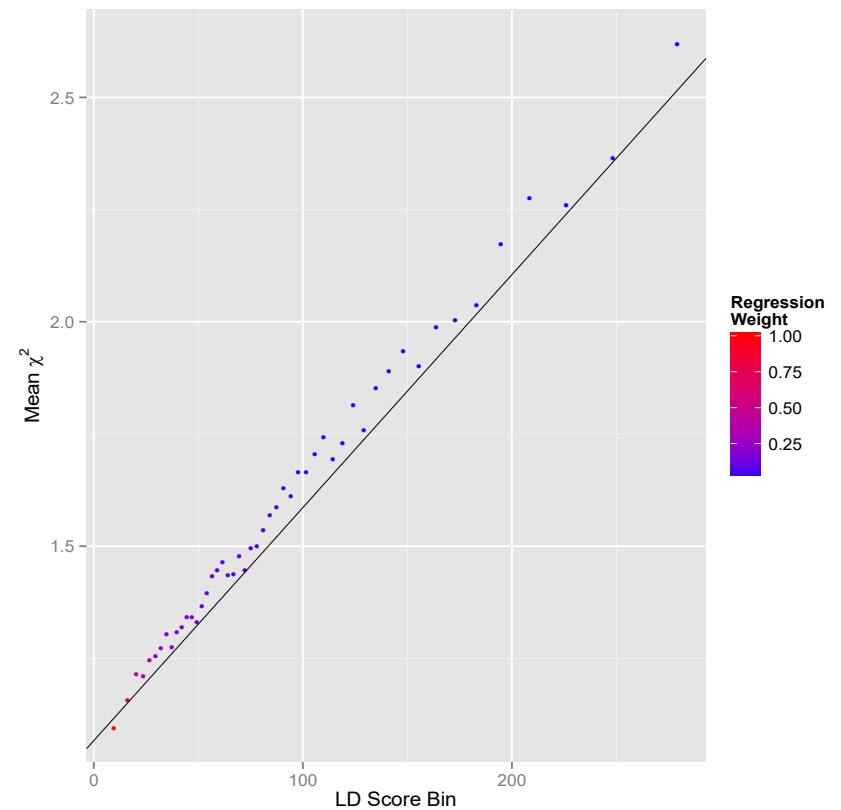


Lambda = 1.48

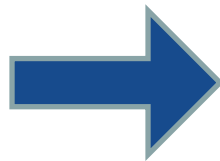
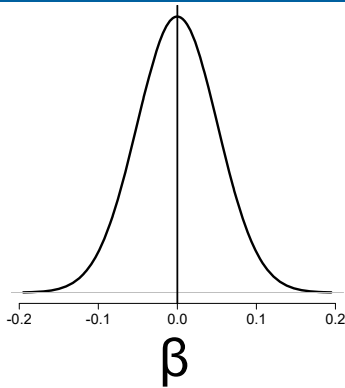
Intercept = 1.06

Slope p -value $< 10^{-300}$

Overwhelming majority of inflation is consistent with polygenic architecture



LD Score regression



Draw polygenic effects from $N(0, h^2/m)$, var =



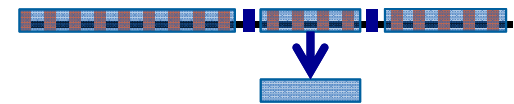
What is the $E[\chi^2]$ for variant j ?

$$E[\chi_j^2] = 1 + Na + \frac{h_g^2 N}{M} l_j \quad \text{New estimator of heritability}$$

where N =sample size, M =# of SNPs, a =inflation due to confounding, h^2_g is heritability (total obs.) and l_j is the *LD Score*

Bulik-Sullivan et al. Nature Genetics 2015
Yang et al. EHG 2011

$$l_j = \sum_{k=j} r_{jk}^2$$



Brainstorm Project



Verner Anttila



Aiden Corvin

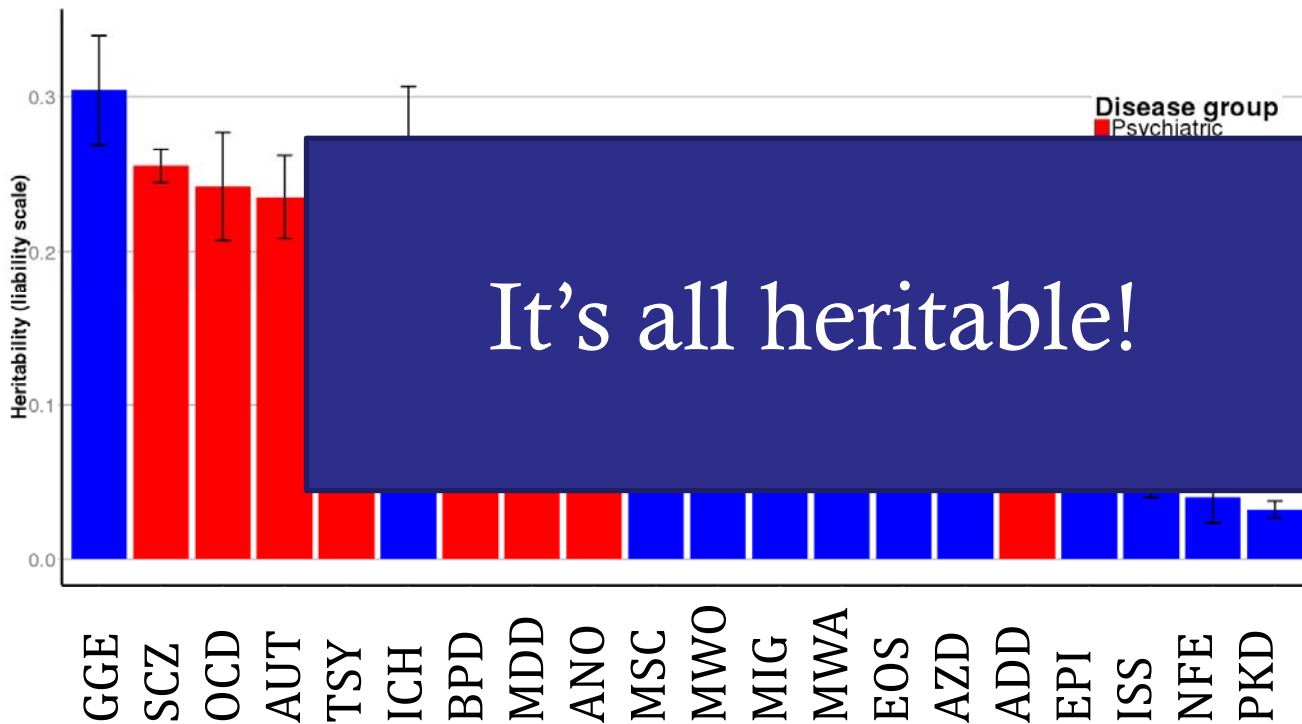


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Alessandro Biffi

Jeremiah Scharf
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Padhraig Gormley
Zhi Wei
Rainer Malik
Hailiang Huang
Andrea Byrnes

Dongmei Yu
Laramie Duncan
Kai-How Farh
Namrata Gupta
Miriam Raffeld
...and many, many others
in their respective study groups

Univariate heritability from common variation



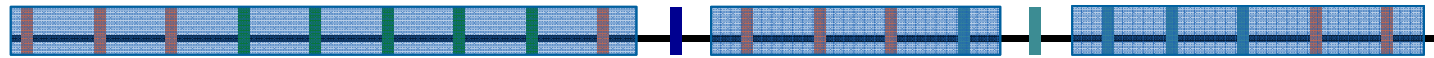
- GGE = Generalized Epilepsy
- SCZ = Schizophrenia
- OCD = Obsessive Compulsive Disorder
- AUT = Autism
- TSY = Tourette's Syndrome
- ICH = Intracerebral Hemorrhage
- BPD = Bipolar Disorder
- MDD = Major Depressive Disorder
- ANO = Anorexia Nervosa
- MSC = Multiple Sclerosis
- MWO = Migraine without Aura
- MIG = Migraine
- MWA = Migraine with Aura
- EOS = Early Onset Stroke
- AZD = Alzheimer's Disease
- ADD = Attention Deficit/Hyperactivity
- EPI = Epilepsy (all)
- ISS = Ischemic Stroke
- NFE = Non-acquired focal epilepsy
- PKD = Parkinson's Disease

Key extension 1

Functional partitioning



- █ Lonely SNPs [no LD]
- ▒ LD blocks
- * Causal variants
- █ DHS
- █ Coding



LD Score	9	1	4	1	5
DHS Score	5	0	0	0	0
Coding Score	0	0	1	1	3

Finucane et al. 2015 Nat Gen

$$l_j = \sum_{k \in C} r_{jk}^2$$



Mark	Source/reference
Coding, 3' UTR, 5' UTR, Promoter, Intron	UCSC; Gusev et al., in press AJHG
Digital Genomic Footprint, TFBS	ENCODE; Gusev et al., in press AJHG
CTCF binding site, Promoter Flanking, Repressed, Transcribed, TSS, Enhancer, Weak Enhancer	ENCODE; Hoffman et al., 2012 Nucleic Acids Research
DHS, fetal DHS, H3K4me1, H3K4me3, H3K9ac	Trynka et al., 2013 Nature Genetics.*
Conserved	Lindblad-Toh et al., 2011 Nature
FANTOM5 Enhancer	Andersson et al., 2014 Nature
lincRNAs	Cabili et al., 2011 Genes Dev
DHS and DHS promoter	Maurano et al., 2012 Science
H3K27ac	Roadmap; PGC2 2014 Nature

*Post-processed from ENCODE and Roadmap data by S. Raychaudhuri and X. Liu labs

Datasets for GWAS

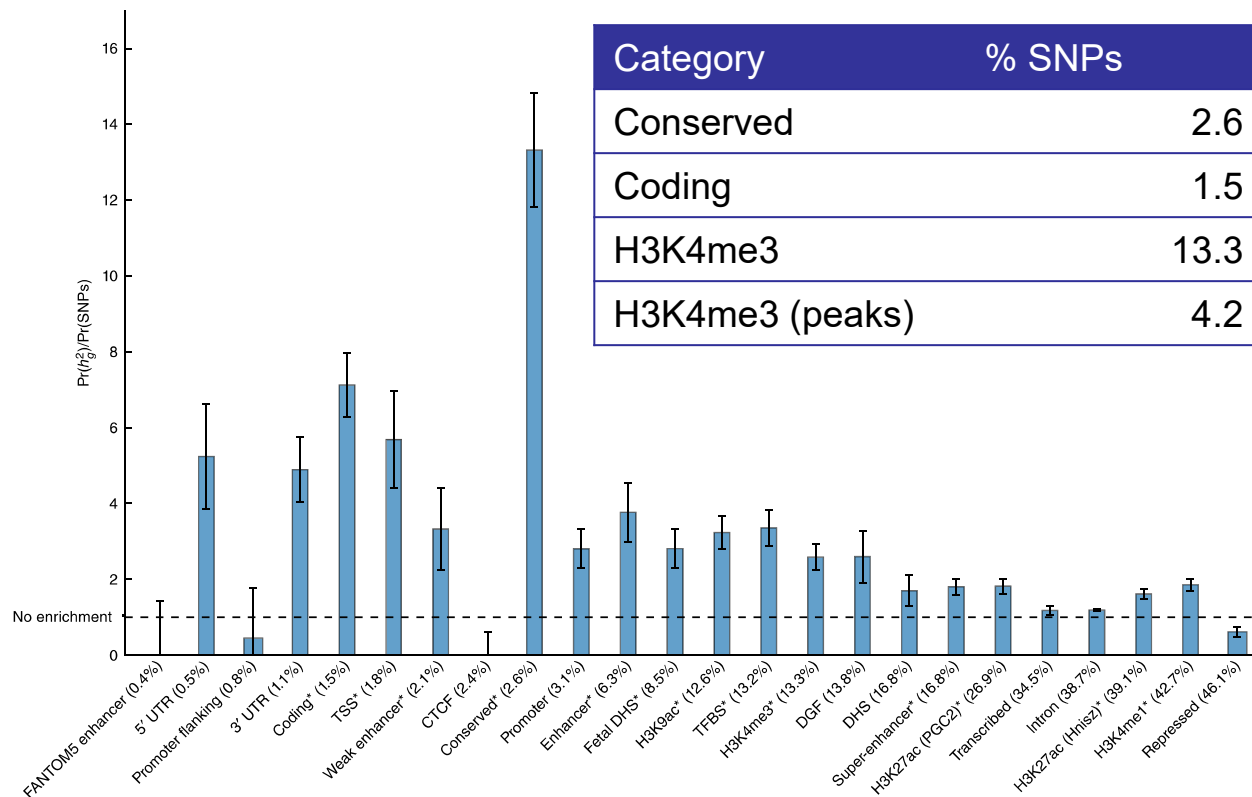
Selected for a $Z > 7$ for h^2



Phenotype	Reference	Phenotype	Reference
Height	Lango Allen, 2010	Schizophrenia	PGC, 2014
BMI	Speliotes, 2010	Bipolar	Sklar, 2011
Age of menarche	Perry, 2014	Anorexia	Boraska, 2014
LDL	Teslovich, 2010	Education years	Rietveld, 2013
HDL	Teslovich, 2010	Ever smoked	TAG, 2010
Triglycerides	Teslovich, 2010	Rheumatoid Arth	Okada, 2014
CAD	Schunkert, 2011	Crohn's Disease	Jostins, 2012
T2D	Morris, 2012	Ulcerative Colitis	Jostins, 2012
Fasting Glucose	Manning, 2012		

Average enrichments per class

Collapsed results across 17 traits

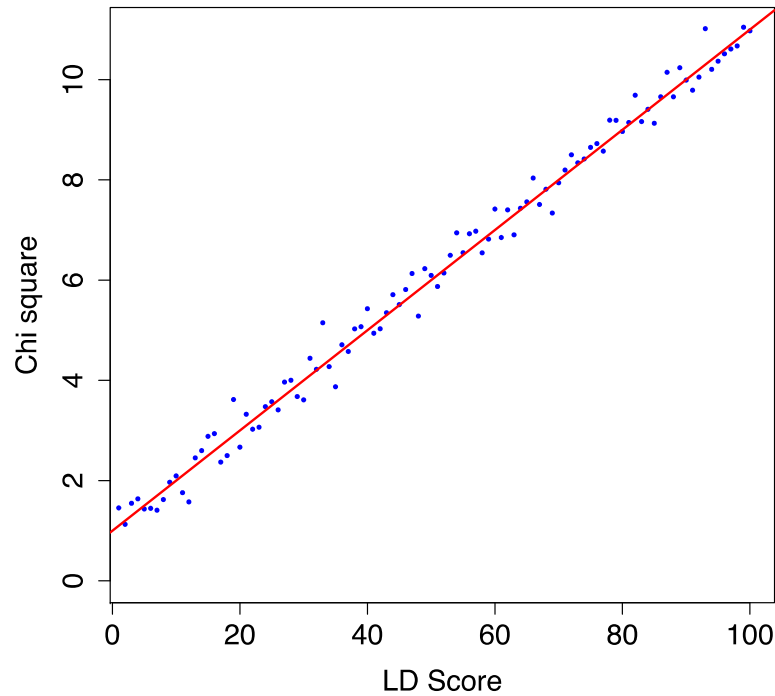


Category	% SNPs	% h ²	Enrichment
Conserved	2.6	34.7	13.4x
Coding	1.5	10.4	7.0x
H3K4me3	13.3	34.4	2.6x
H3K4me3 (peaks)	4.2	15.8	3.8x

LD Score regression Genetic correlation

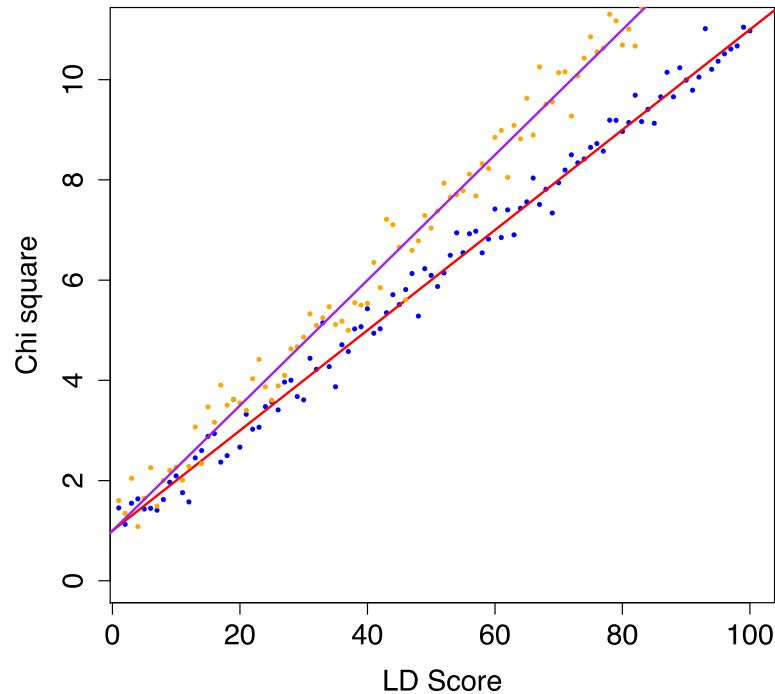


Trait 1



Slope estimates heritability

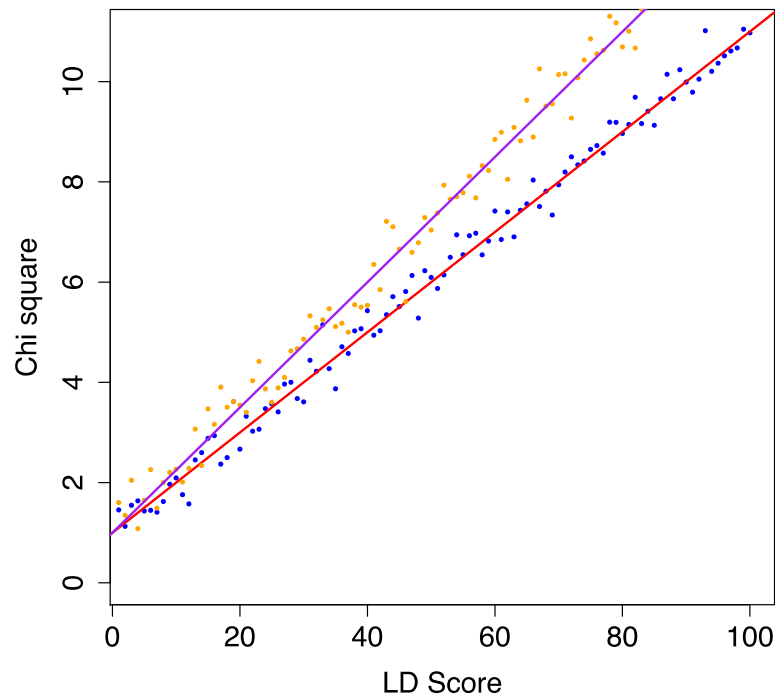
LD Score regression Genetic correlation



Trait 1
Trait 2

We can a second trait and
obtain two heritability
estimates

LD Score regression Genetic correlation

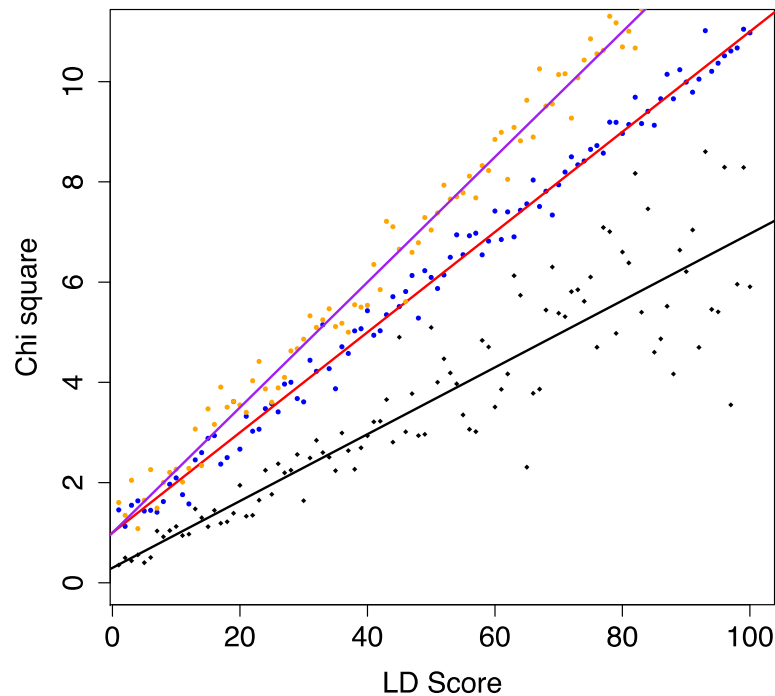


Trait 1
Trait 2

$$Z^*Z = \chi^2$$

So we can estimate genetic covariance from the product of the Z-scores

LD Score regression Genetic correlation



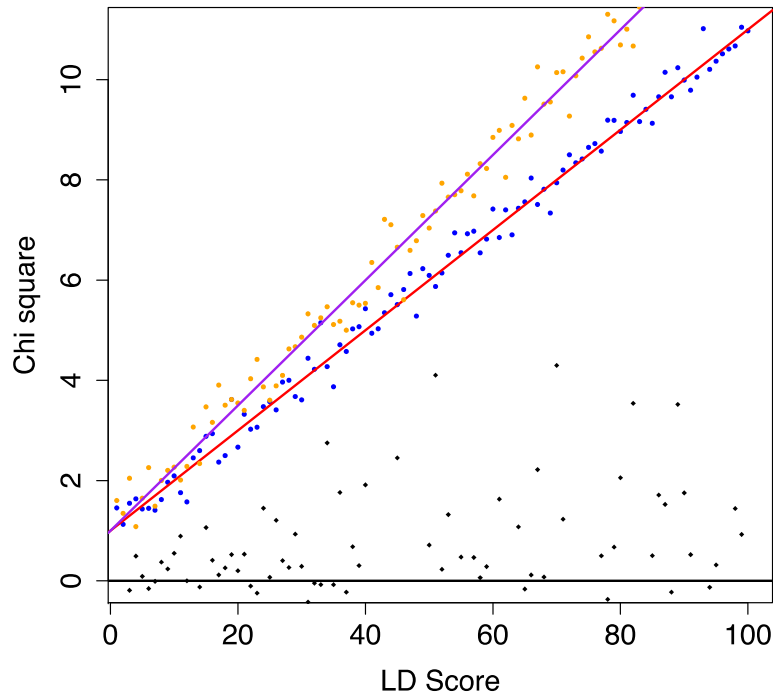
Trait 1
Trait 2
 R_G

$$Z^*Z = \chi^2$$

So we can estimate genetic covariance from the product of the Z-scores for the two traits

$$R_G = 0.5$$

LD Score regression Genetic correlation

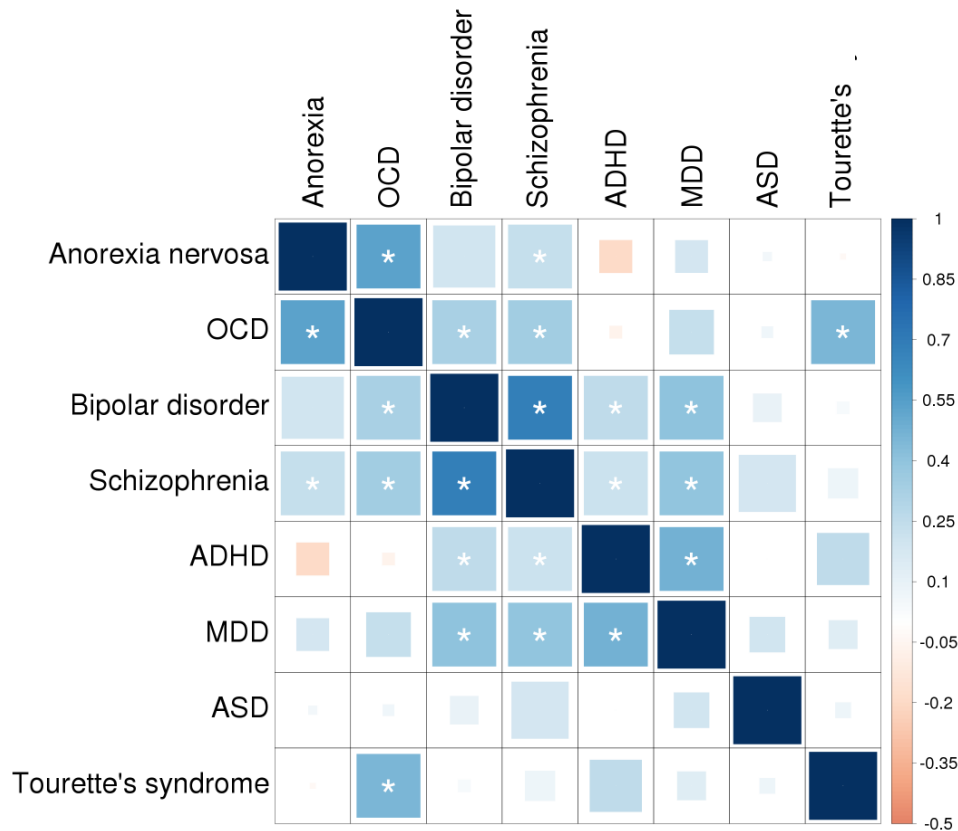


Trait 1
Trait 2
 R_G

Here $R_G = 0$

This approach is robust to
sample overlap as all variants
are equally inflated

Within psychiatry



Broad sharing of common genetic risk factors across psychiatric illness

Risk factors do not respect traditional boundaries

* denotes significant correlation

Conclusions



- Direct estimation of heritability from GWAS is possible
- Heritability is an arbiter of relative importance for classes of variation
- Heritability can be used to elucidate the relationships between different phenotypes